

# **ELLIPSOMETRY OF SEMICONDUCTORS UNDER THERMAL AND LASER EXCITATION**

Ph.D. dissertation defense

**Carola Emminger  
Advisor: Dr. Stefan Zollner**

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**Department of Physics  
New Mexico State University**



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# MOTIVATION

- **Group IV** (e.g. Ge, Si) and **group III-V** (e.g. GaAs, GaSb, InAs, InSb) semiconductors: important materials for optoelectronic devices
- Group IV photonics applications – examples:
  - Ge-on-Si photodetectors
  - Si-Ge-Sn and Ge-Sn alloys: mid-infrared detectors, photovoltaics, room temperature lasers
- Knowledge on **optical constants** (experiment and theory) is important for simulations and the development of optoelectronic devices.
- **Spectroscopic ellipsometry**: optical contact-free measurement technique; used to determine:
  - Optical constants (complex dielectric function, refractive index)
  - Thickness of a thin layer
  - Information on surface roughness, composition, strain, doping concentration, etc.
- **Femtosecond pump-probe ellipsometry**: study the effects of an ultrashort laser pulse, carrier concentration/doping, scattering etc.

# OUTLINE

## **Introduction:**

- Spectroscopic ellipsometry
- Critical point analysis using digital filtering

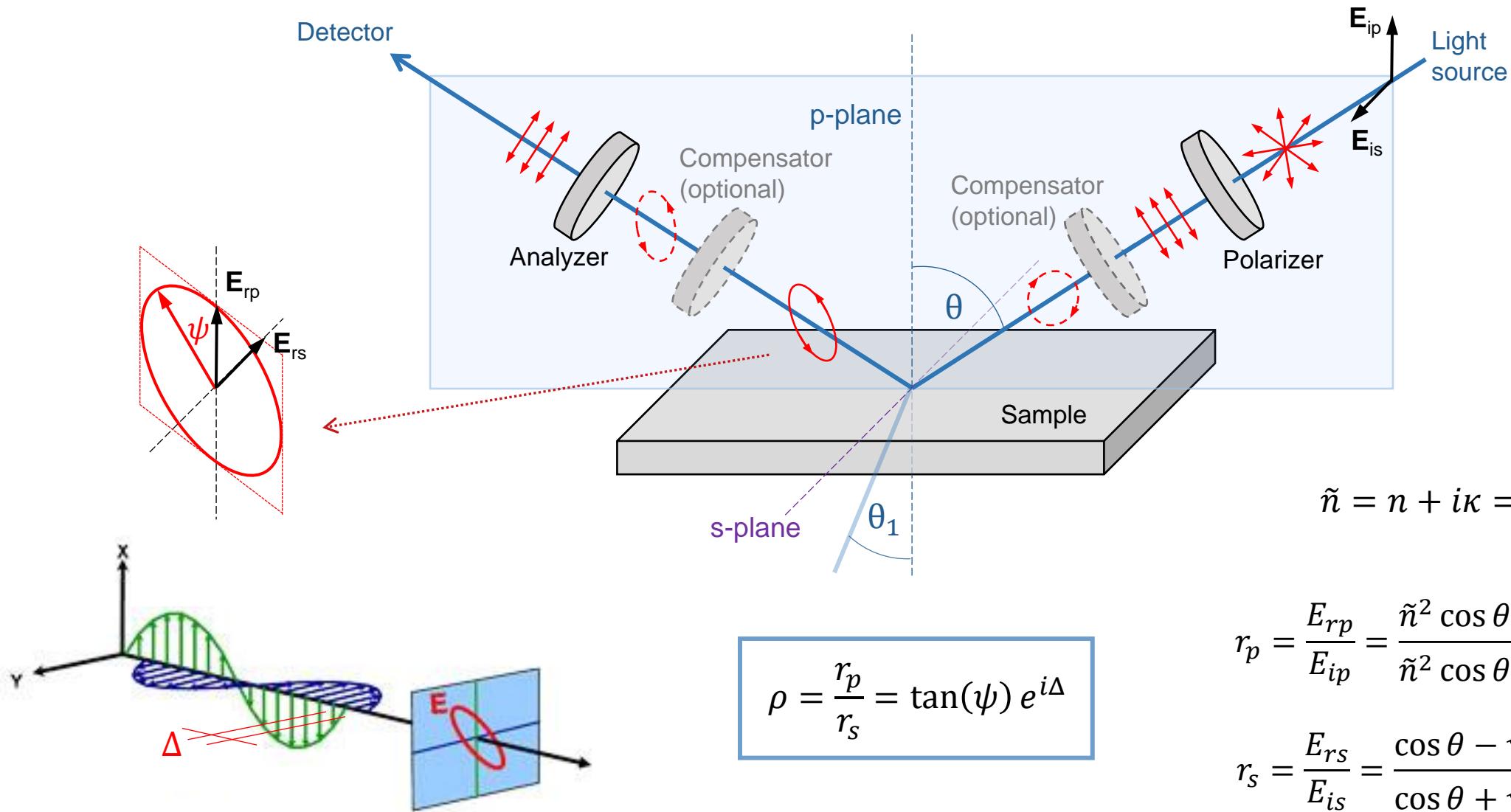
## **Part 1: Excitonic effects at the direct band gap of Ge**

- Hulthén-Tanguy model with parameters from  $k\cdot p$  theory
- Energy and broadening as functions of temperature

## **Part 2: Transient critical point parameters of Ge and Si from femtosecond pump-probe ellipsometry**

- Critical point parameters as functions of time delay
- Coherent phonon oscillations

# Spectroscopic Ellipsometry



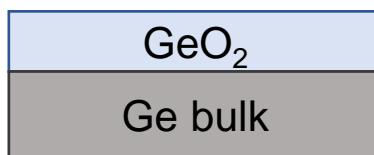


[www.jawoollam.com](http://www.jawoollam.com)

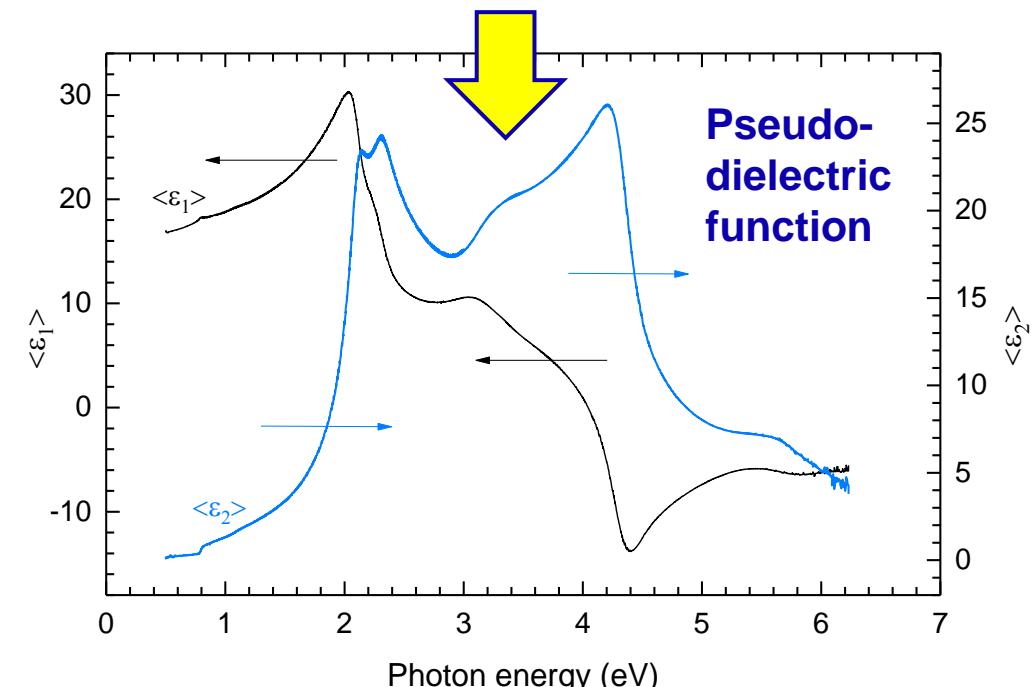
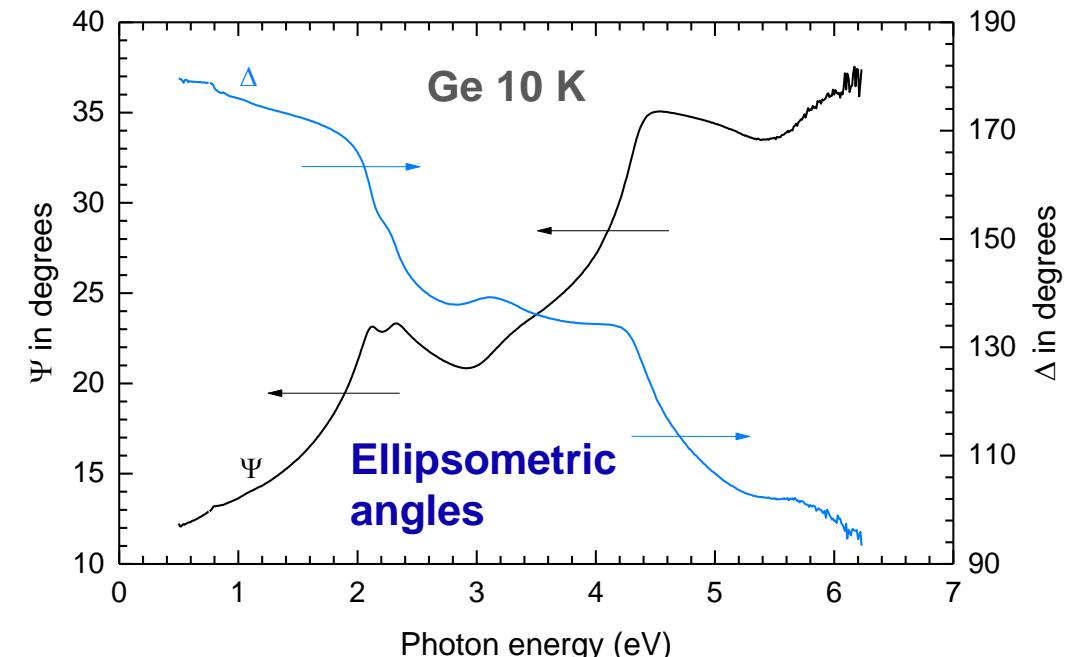
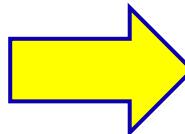
Two-layer model  
(Ge substrate + native oxide)  
Parametric semiconductor model  
=> dielectric function  $\epsilon$

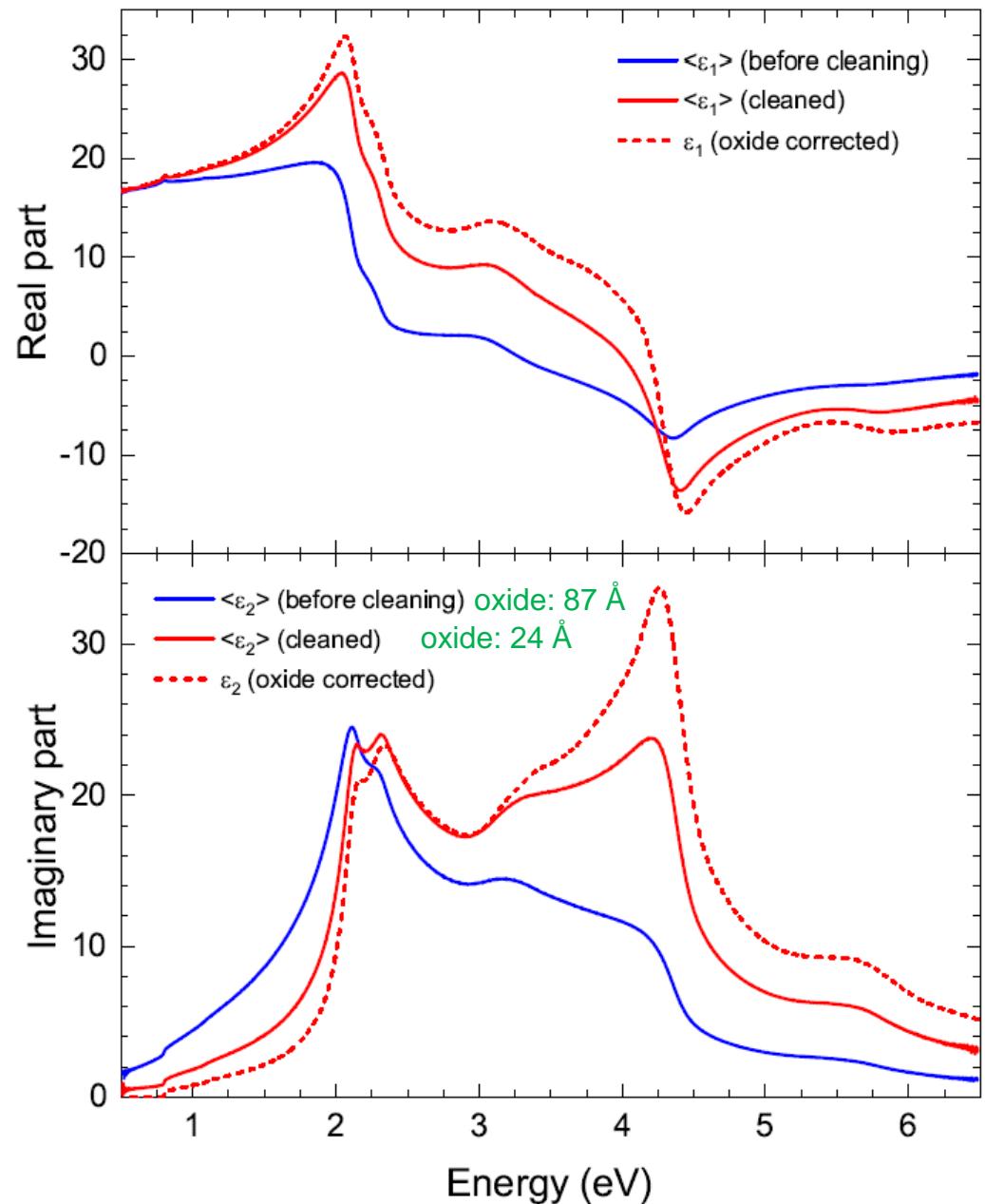
Dielectric function  
 $\epsilon_1 + i\epsilon_2$

Native oxide  
layer correction

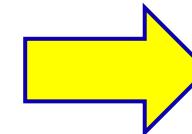


$$\rho = \tan(\psi) e^{i\Delta}$$

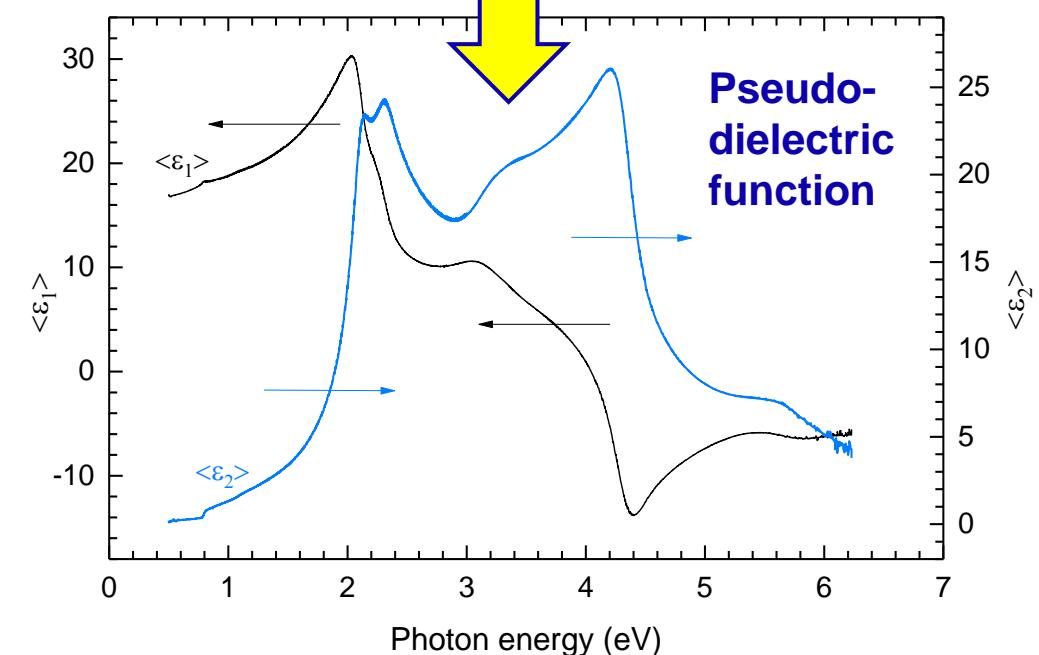
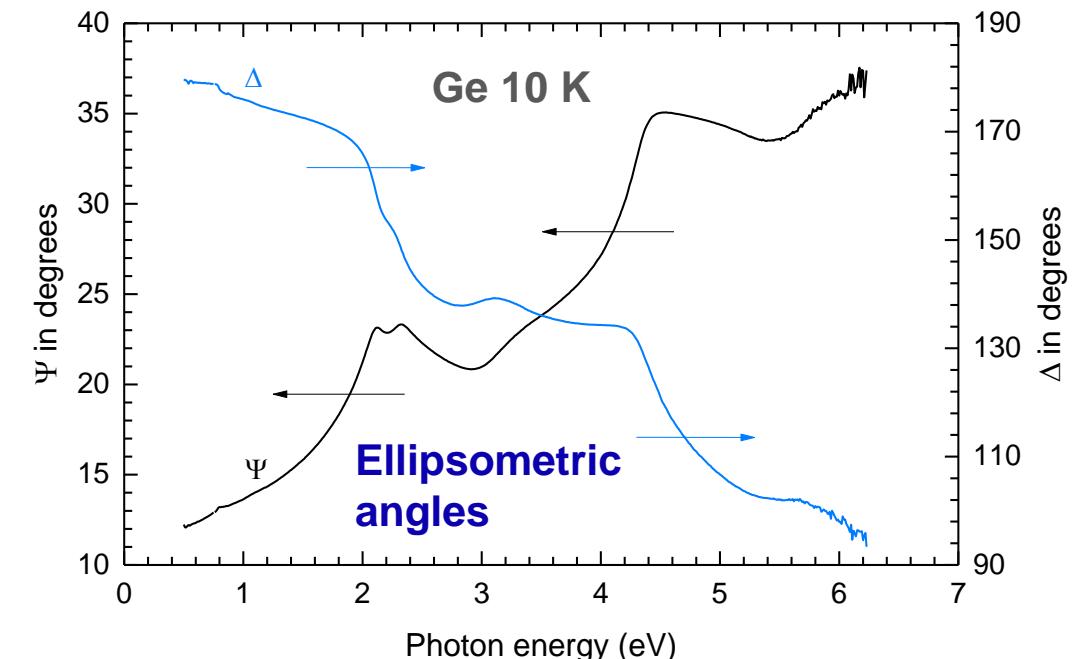


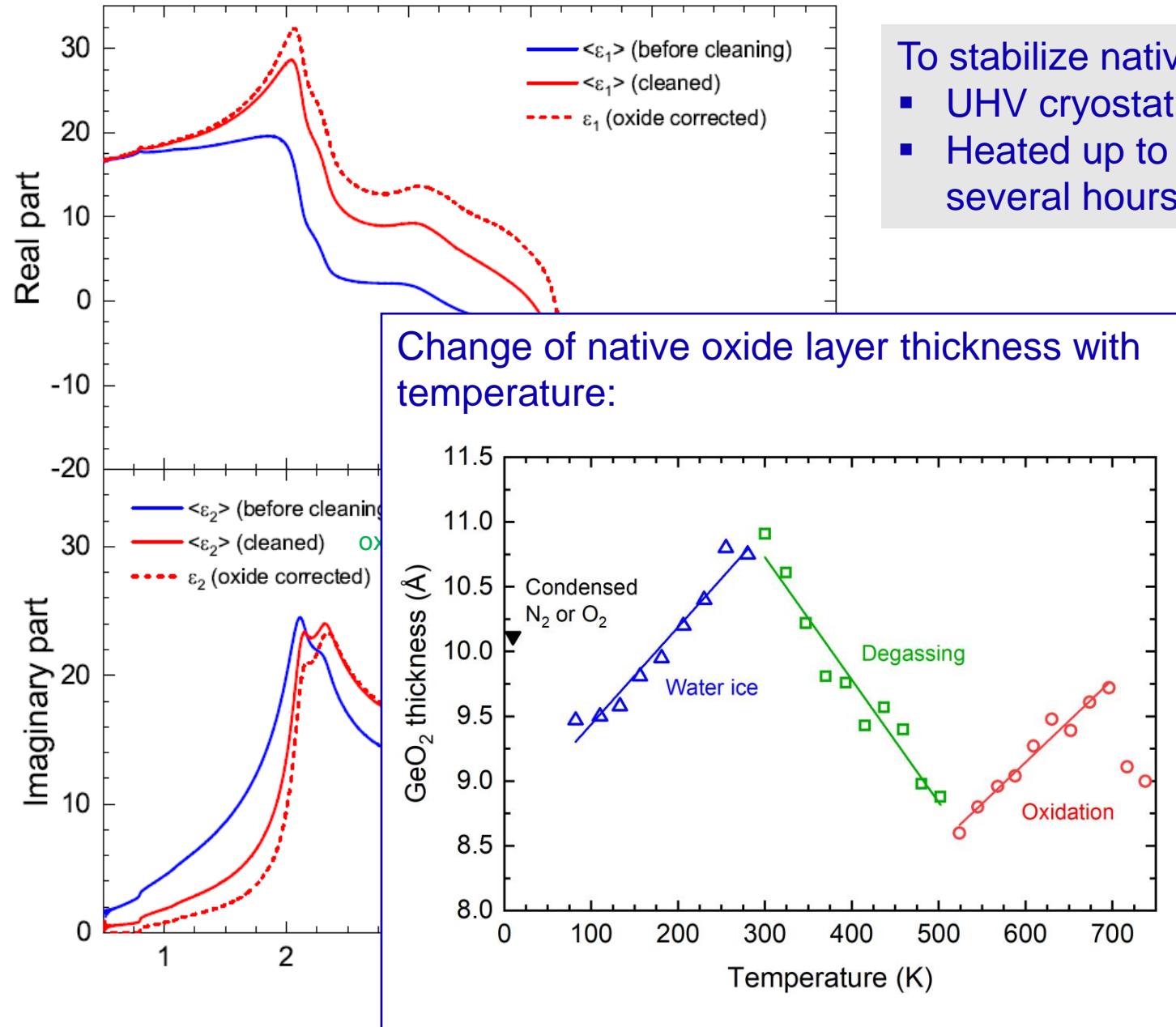


$$\rho = \tan(\psi) e^{i\Delta}$$



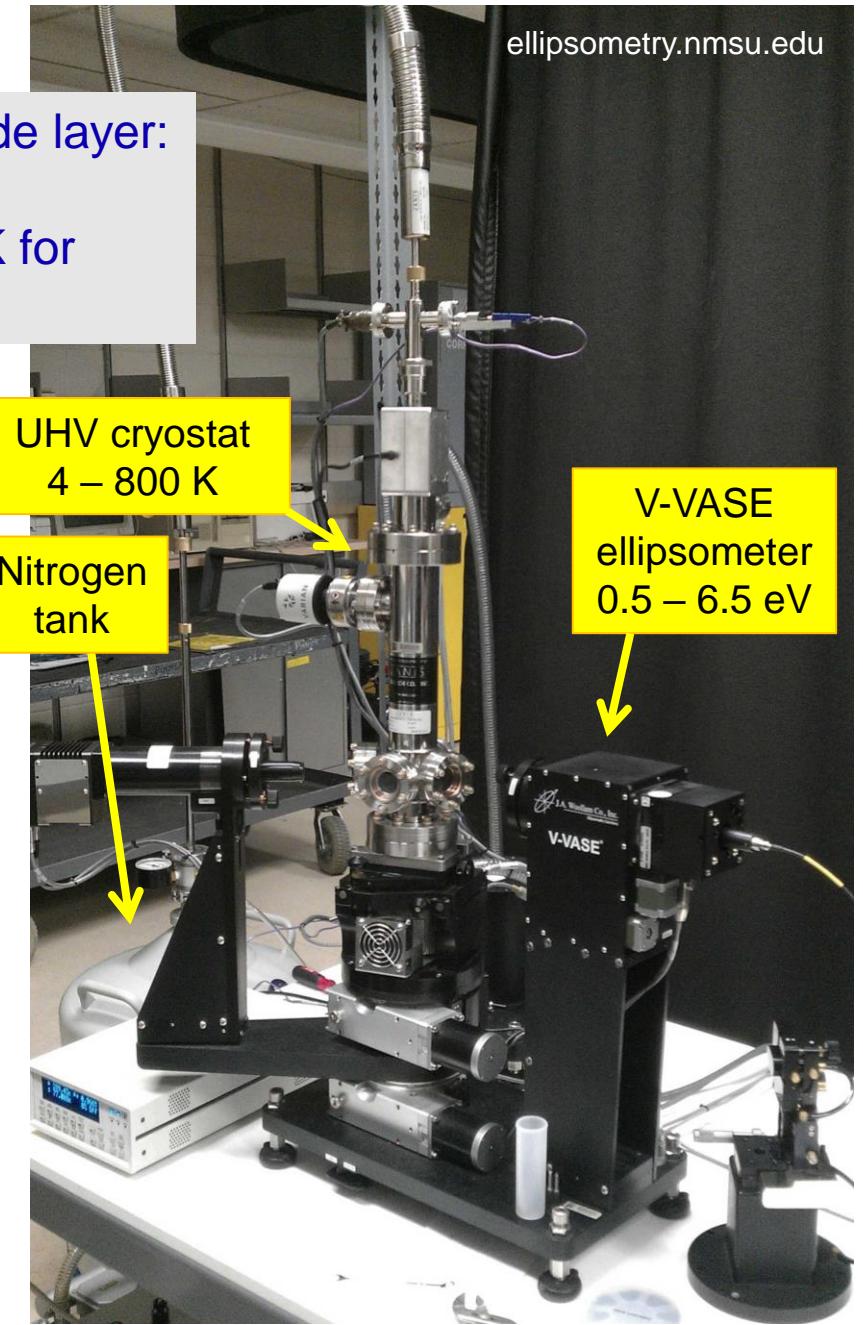
Native oxide  
layer correction





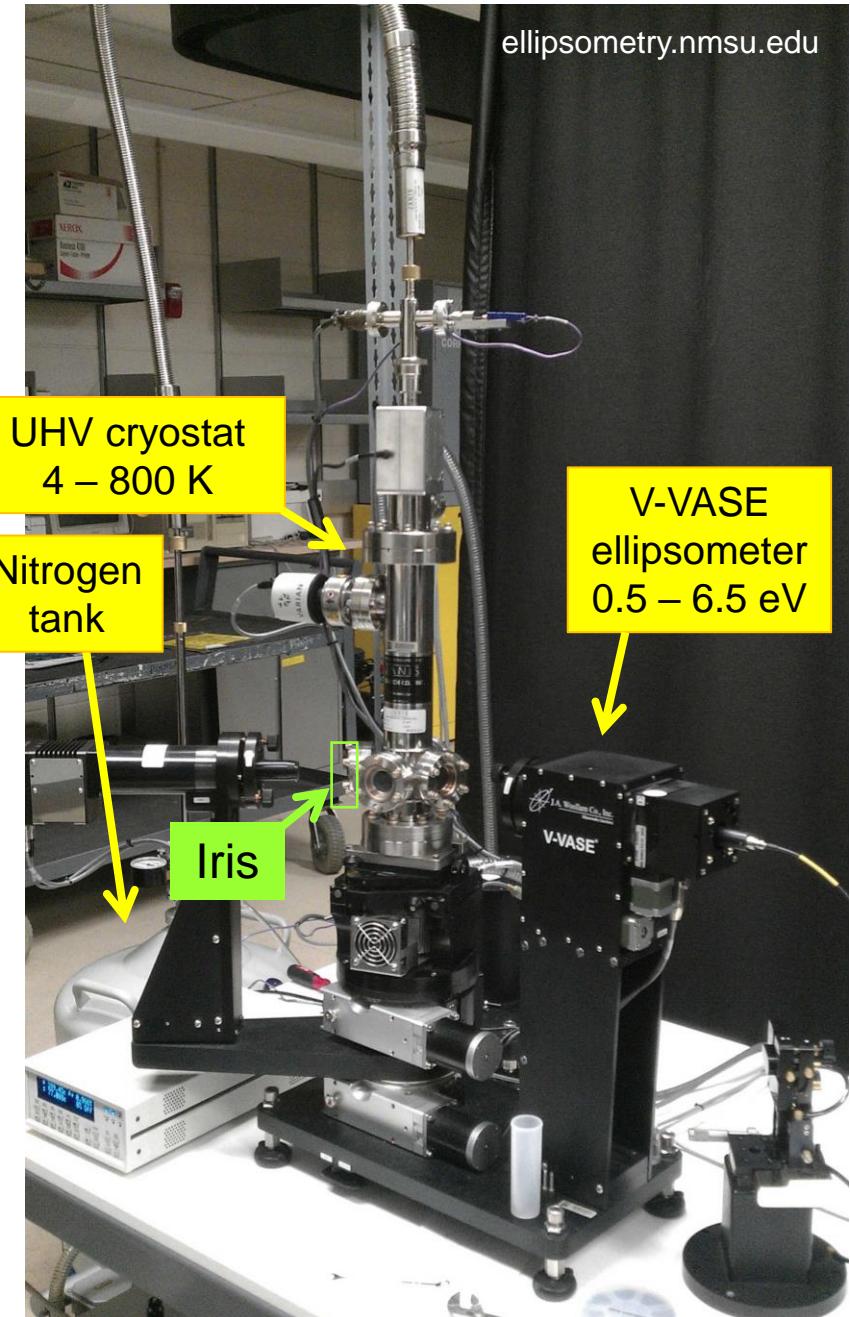
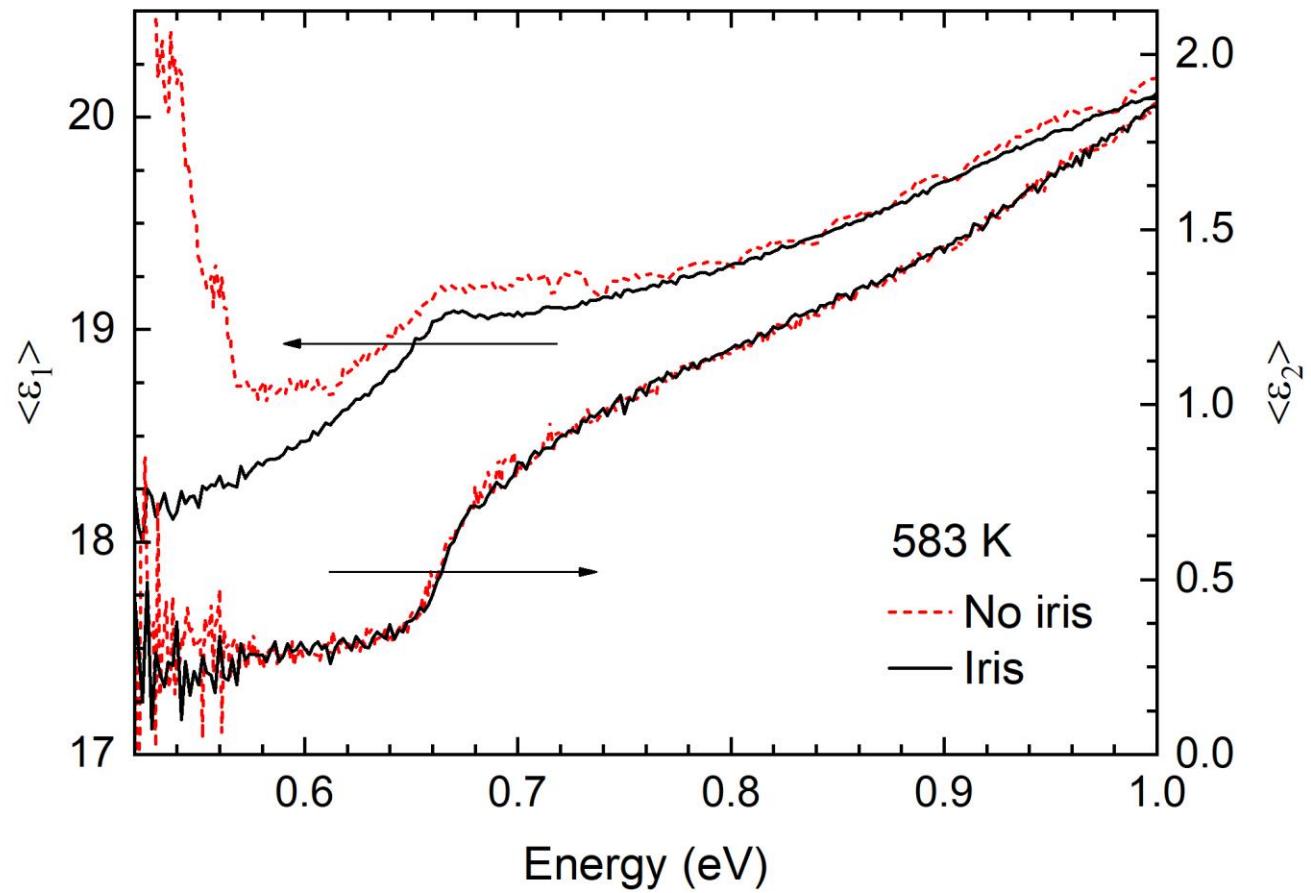
To stabilize native oxide layer:

- UHV cryostat
- Heated up to 700 K for several hours



# Black body radiation

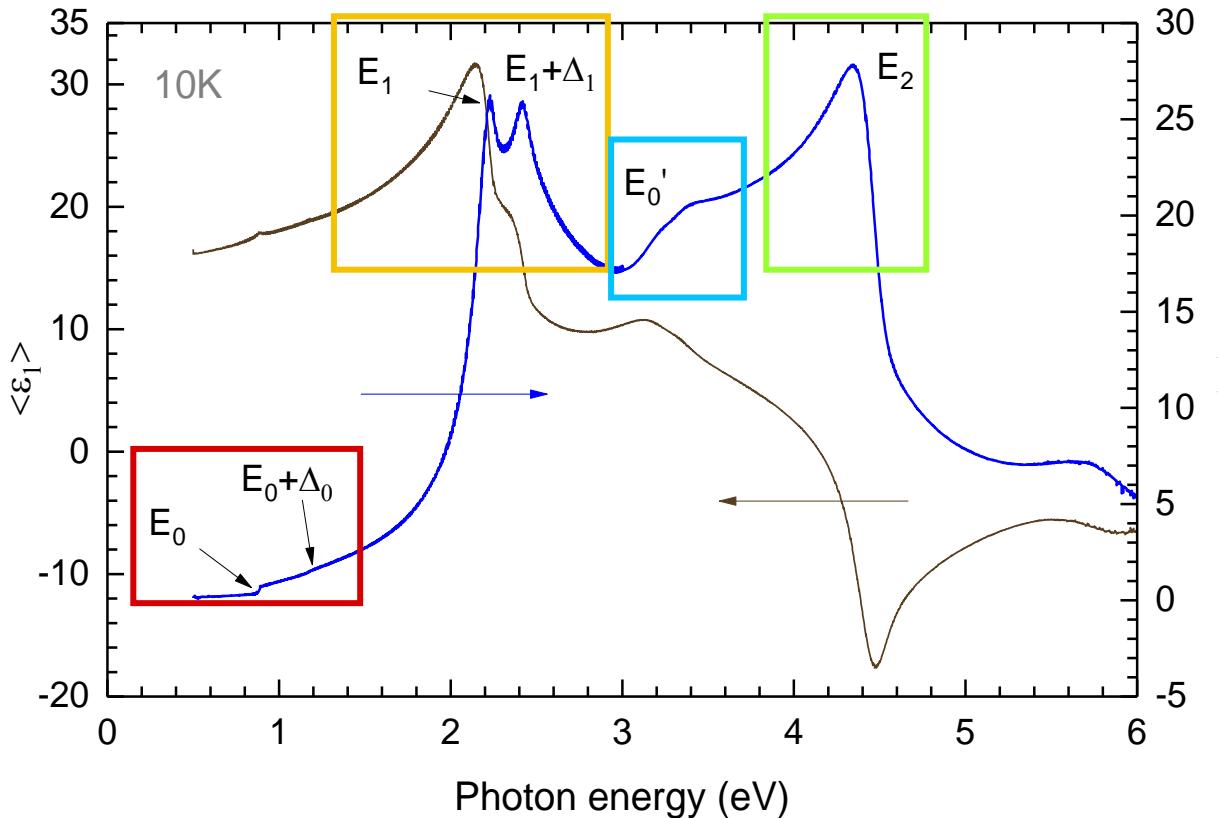
At higher temperatures: Distortions due to black body radiation  
⇒ Can be improved by placing an iris at the exit window of the cryostat



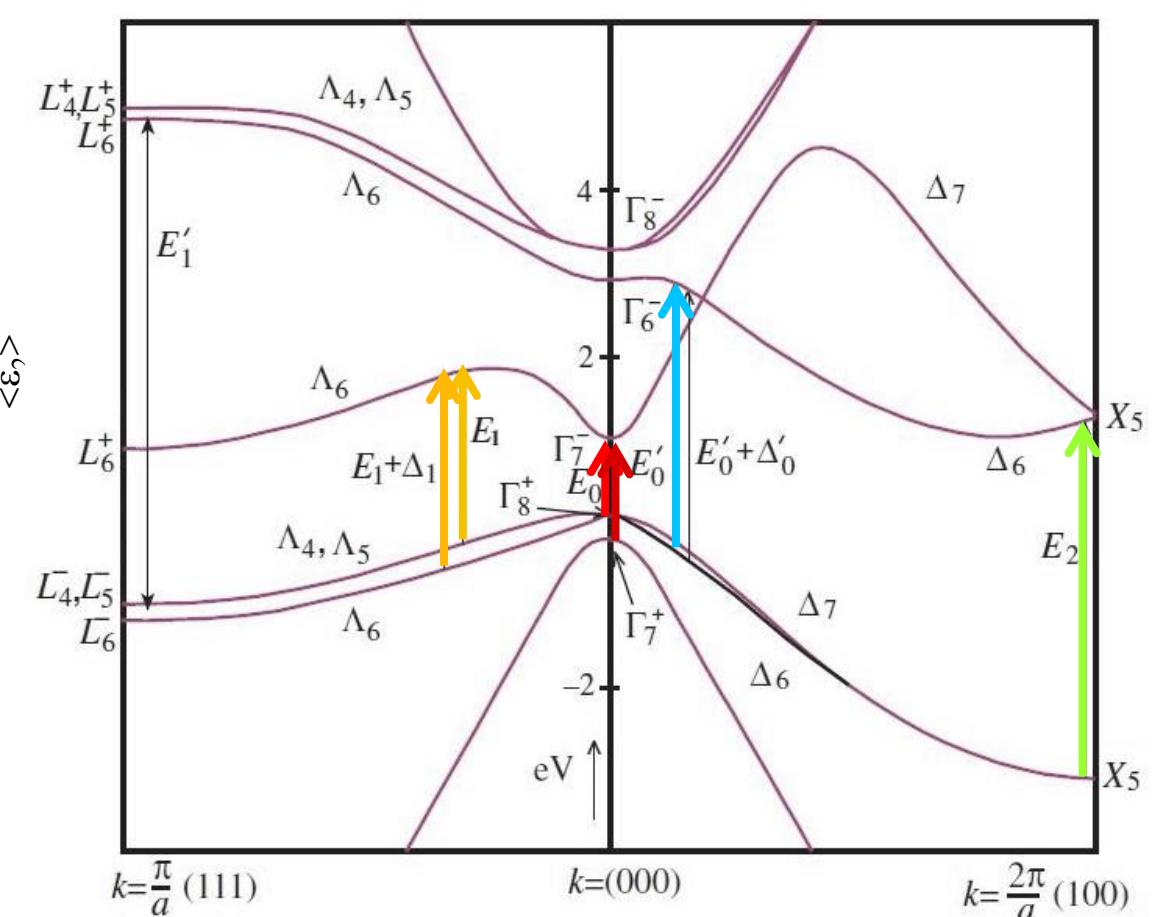
# Critical points of Ge

- Structures in the dielectric function due to interband transitions
- Joint density of states – Van Hove singularities

$$D_j(E_{CV}) = \frac{1}{4\pi^3} \int \frac{dS_k}{|\nabla_k(E_{CV})|}$$



- Critical point analysis: Second derivative of dielectric function to suppress non-resonant background



P. Y. Yu and M. Cardona: *Fundamentals of Semiconductors: Physics and Materials Properties*. (Springer-Verlag, Berlin, 2010)

# Critical point analysis using linear filters

- Linear filter method (Le et al. 2019) can be used for:
  - Scale change (energy  $\leftrightarrow$  wavelength)
  - Interpolation and filtering of the dielectric function
  - Calculation of second derivatives of the dielectric function

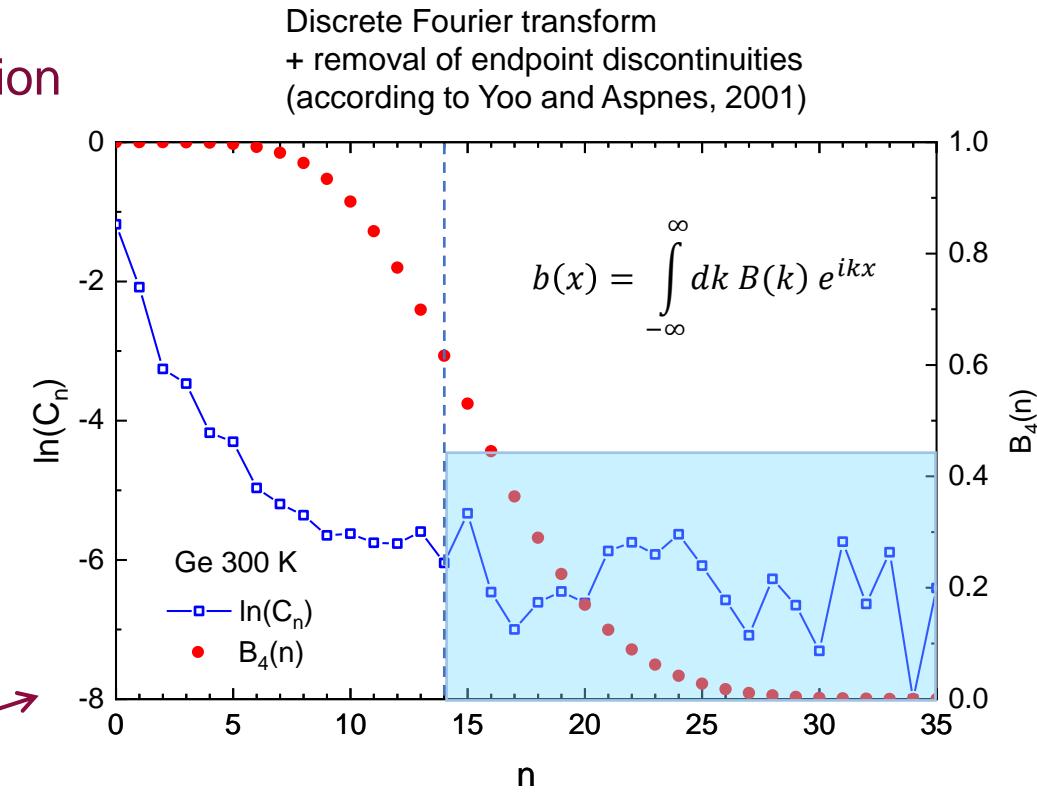
- Direct space convolution  $\bar{f}(E) = \int_{-\infty}^{\infty} dE' f(E') b_M(E - E')$

with Extended Gauss (EG) filters

$$b_M(x) = \left(1 - \frac{a}{1!} \frac{d}{da} + \frac{a^2}{2!} \frac{d^2}{da^2} - \dots + (-1)^M \frac{a^M}{M!} \frac{d^M}{da^M}\right) \frac{a^{-1/2}}{2\sqrt{\pi}} e^{-x^2/4a}$$

$$a = 1/\Delta k^2 = \Delta E^2$$

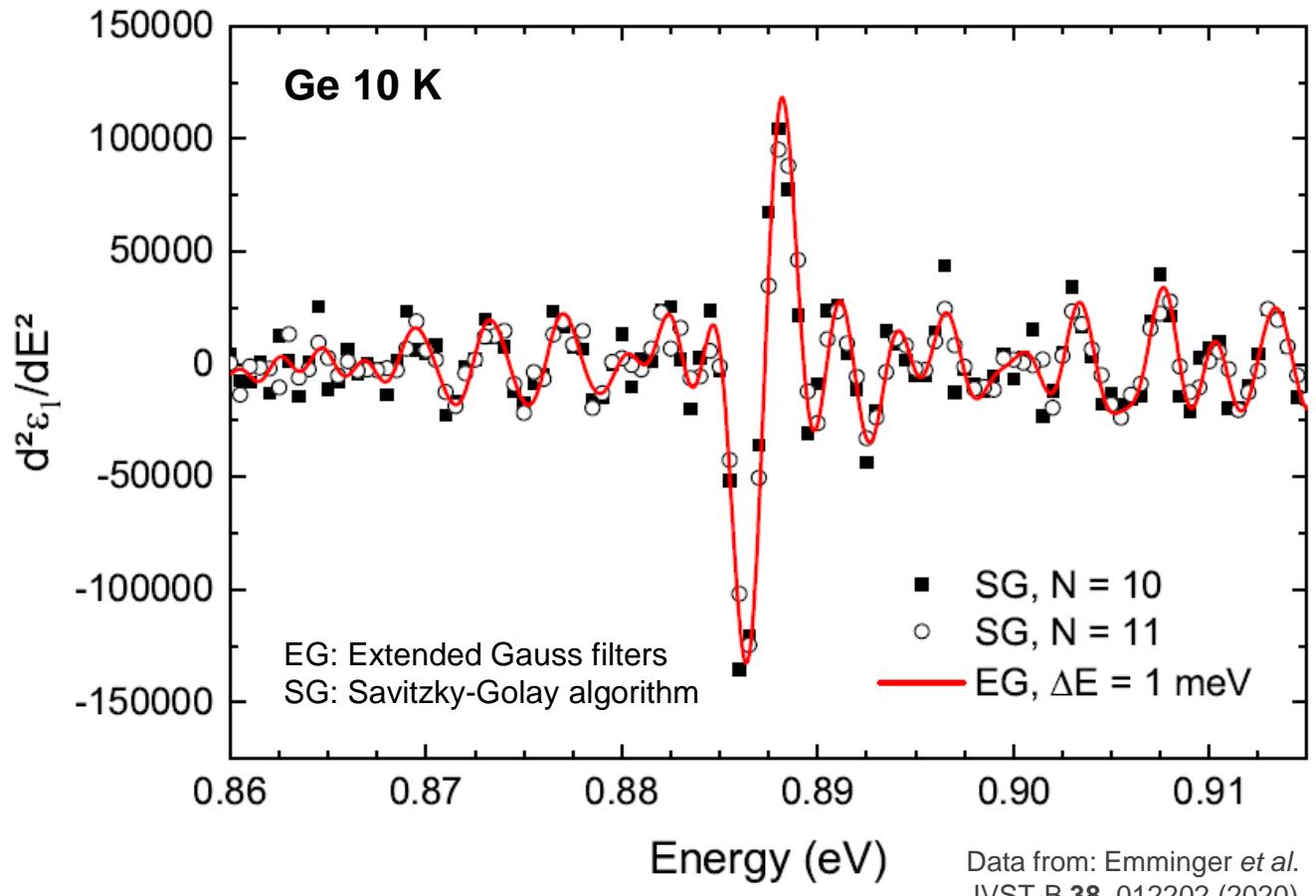
- Filter width  $\Delta E$  chosen according to white noise onset



# Calculation of the second derivatives

Second derivative of  $\epsilon$  using EG-filters for  $M = 4$  for data sets with equidistant energy steps  $\Delta E'$ :

$$\frac{d^2\bar{\epsilon}(E)}{dE^2} \approx \frac{\Delta E'}{49152\sqrt{\pi}\Delta E^{13}} \sum_{j=-\infty}^{\infty} \epsilon(E_j) \left( (E - E_j)^{10} - 106(E - E_j)^8 \Delta E^2 + 3608(E - E_j)^6 \Delta E^4 - 45936(E - E_j)^4 \Delta E^6 + 188496(E - E_j)^2 \Delta E^8 - 110880 \Delta E^{10} \right) e^{-\frac{(E-E_j)^2}{4\Delta E^2}}$$



Data from: Emminger *et al.*  
JVST-B **38**, 012202 (2020).

## **Part 1: Excitonic effects at the direct band gap of Ge**

# Choice of lineshape for direct band gap

$$\epsilon(E) = B - Ae^{i\varphi}(E - E_g + i\Gamma)^\mu$$

## Which lineshape describes the band gap best?

- Three dimensional lineshape: Square root-like dependence on energy

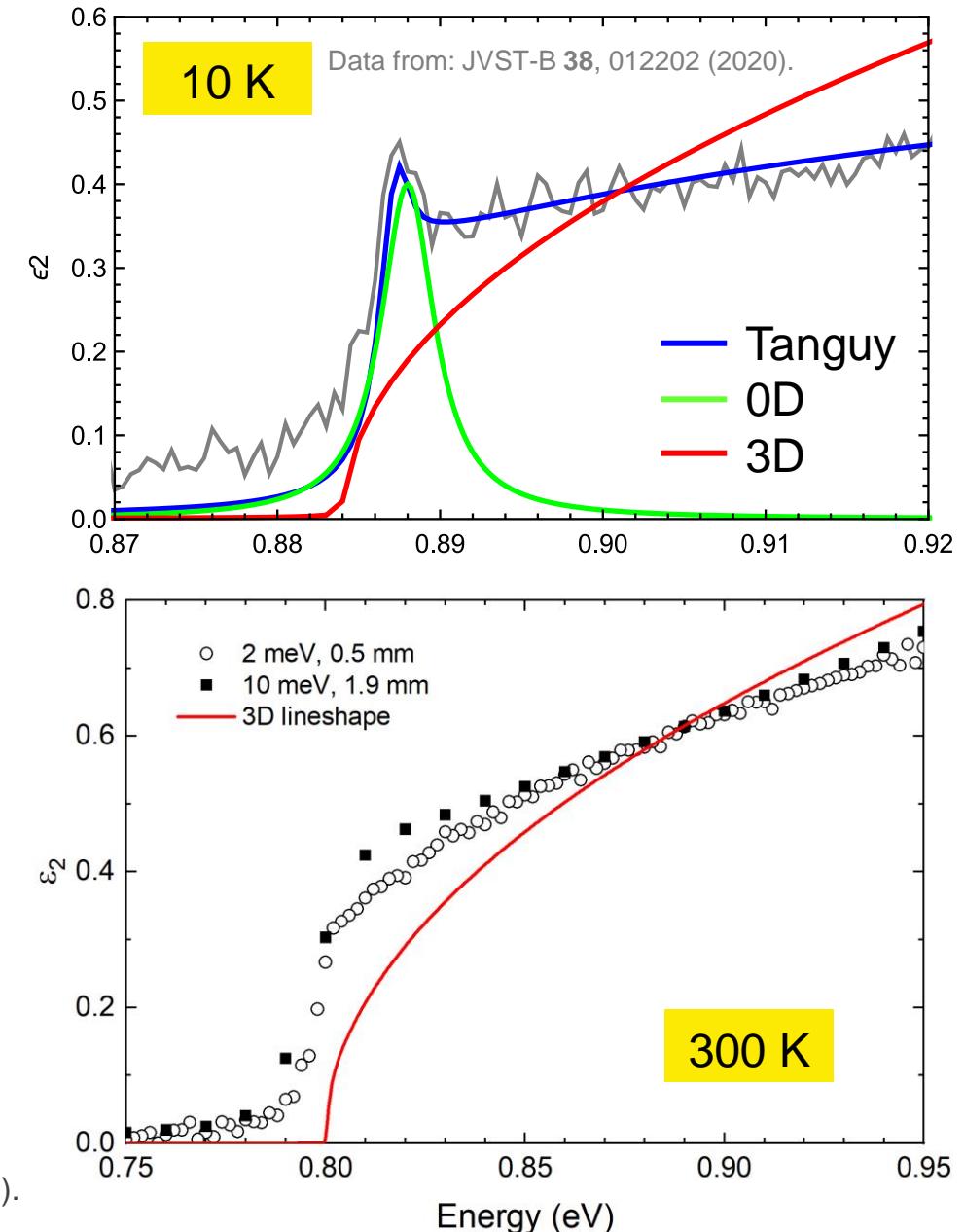
$$\epsilon_{3D}(E) = B + Ae^{i\varphi}\sqrt{E - E_g + i\Gamma}$$

- Lorentzian (0D) lineshape

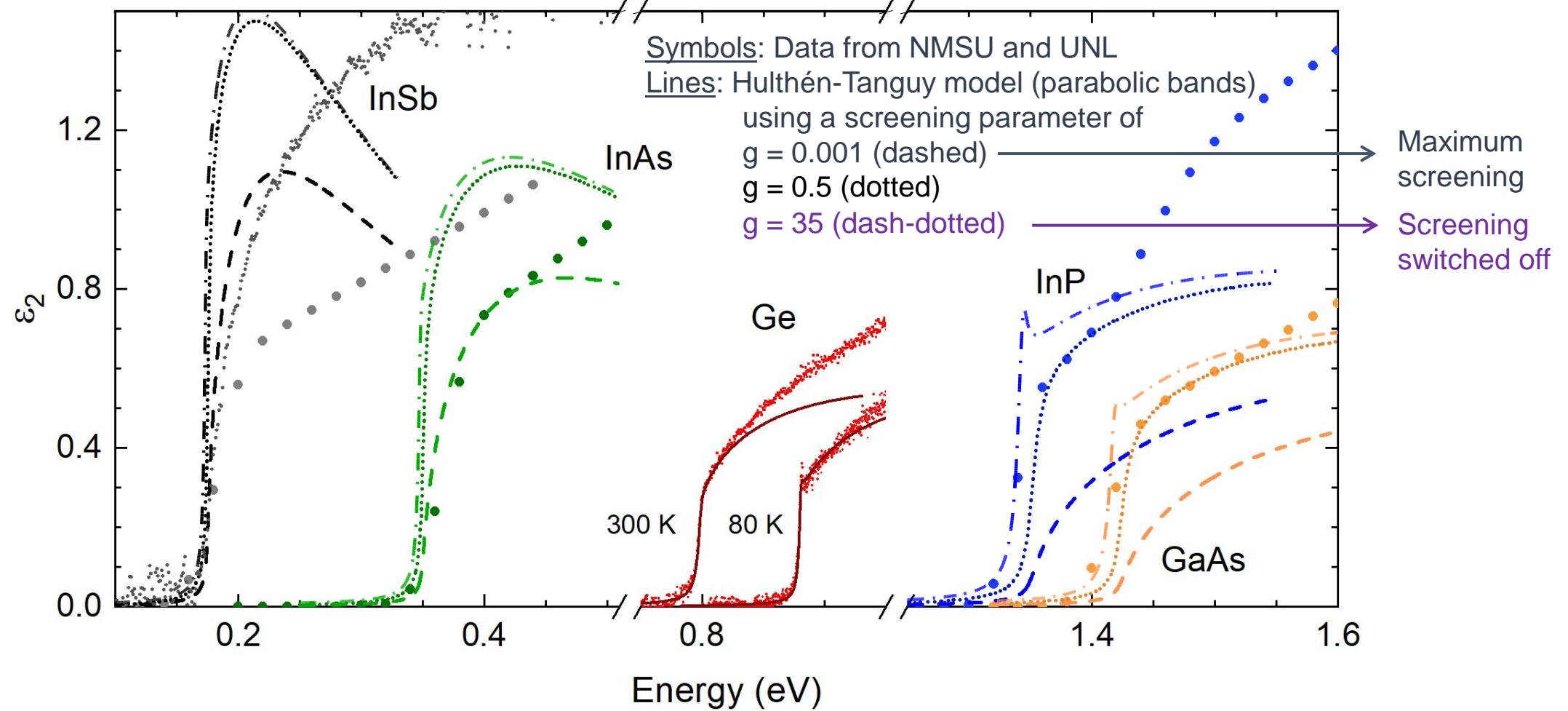
$$\epsilon_{0D}(E) = B + \frac{Ae^{i\varphi}}{E - E_g + i\Gamma}$$

$A$  .... amplitude  
 $E_g$  ... threshold energy  
 $\Gamma$  .... broadening  
 $\varphi$  .... phase angle

- Hulthén-Tanguy lineshape (blue lines): excitonic effects taken into account  
=> **much better agreement**



# Motivation: Model of the direct band gap of various semiconductors



Model: C. Tanguy, Phys. Rev. B **60**, 10660 (1999)

Parameters: P. Lawaetz, Phys. Rev. B **4**, 3461 (1971).

L. Pavesi and F. Piazza, Phys. Rev. B **44**, 9052 (1991).

S. Zollner J. Appl. Phys. **90**, 515 (2001).

S. Zollner, S. Gopalan, and M. Cardona, Solid State Commun. **77**, 485 (1991).

## Next steps:

- Improve model (warping, non-parabolicity, screening)
- Detailed measurements → better data

# Hulthén-Tanguy model to consider excitonic effects

$$\epsilon(E) = \frac{A\sqrt{R}}{(E + i\gamma)^2} [\tilde{g}(\xi(E + i\Gamma)) + \tilde{g}(\xi(-E - i\Gamma)) - 2\tilde{g}(\xi(0))]$$

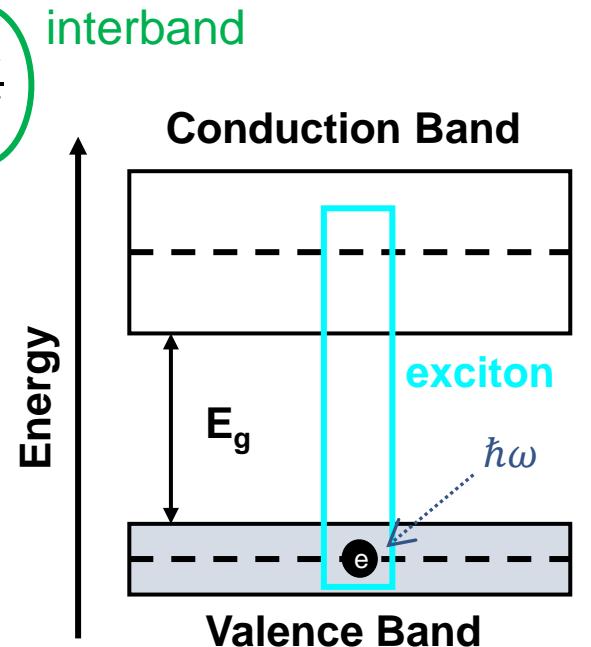
$$\tilde{g}(\xi) = -2\psi\left(\frac{g}{\xi}\right) - \frac{\xi}{g} - \frac{2\psi(1-\xi)}{2\psi(1-\xi) - \frac{1}{\xi}}$$

= 0 for  $g \rightarrow \infty$

unbound      bound      interband

$$\xi(z) = \frac{2}{\left(\frac{E_0 - z}{R}\right)^{1/2} + \left(\frac{E_0 - z}{R} + \frac{4}{g}\right)^{1/2}}$$

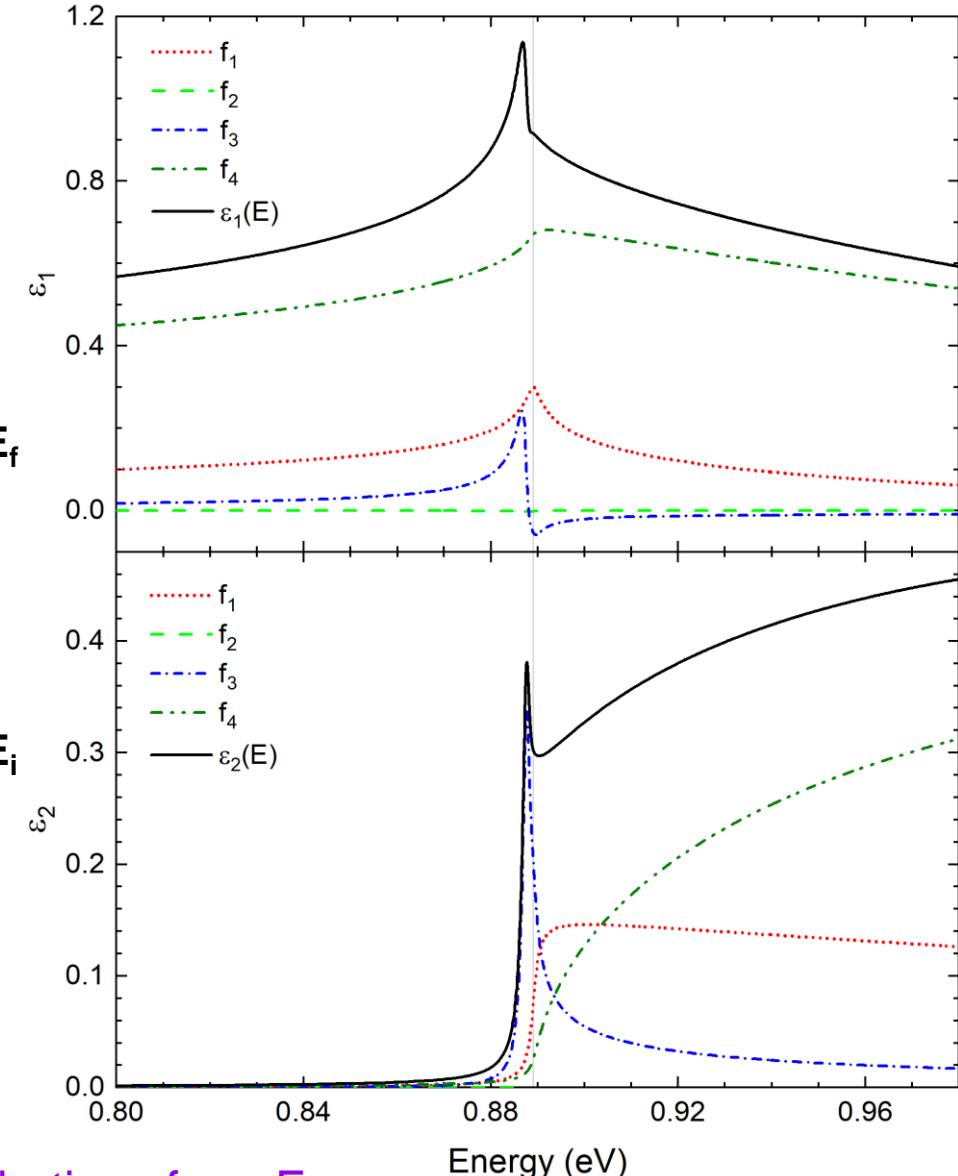
$$\psi(x) = \frac{d \ln \Gamma(x)}{dx}$$
 (Digamma function)



Heavy hole (hh) and light hole (lh):

$$\epsilon(E) = \epsilon_{hh}(E) + \epsilon_{lh}(E) + 1 + \frac{A_1}{1 - B_1 E^2}$$

Sellmeier term to consider contributions from  $E_1$



# Parameters from $k \cdot p$ theory

- Heavy (hh) and light hole (lh) contributions:  $\epsilon(E) = \epsilon_{hh}(E) + \epsilon_{lh}(E) + 1 + \frac{A_1}{1-B_1E^2}$
  - Amplitude:  $A_{hh/lh} = \frac{e^2 \sqrt{m_0}}{\sqrt{2\pi}\epsilon_0\hbar} \mu_{hh/lh}^{3/2} \frac{E_P}{3}$  with  $E_P = \frac{2P^2}{m_0} \approx 26 \text{ eV}$
  - Excitonic binding energy:  $R_{hh/lh} = \frac{\mu_{hh/lh}}{\epsilon_{st}^2} 13.6 \text{ eV}$  ( $R_{hh} \approx 2 \text{ meV}$  and  $R_{lh} \approx 1 \text{ meV}$  at 4 K)
  - Reduced masses:  $\frac{1}{\mu_{hh/lh}} = \frac{1}{m_{hh/lh}} + \frac{1}{m_{e\Gamma}}$
  - Electron effective mass:  $\frac{m_0}{m_{e\Gamma}} = 1 + \frac{E_P}{3} \left[ \frac{2}{E_0} + \frac{1}{E_0 + \Delta_0} \right]$
  - Hole effective masses:  $\frac{m_0}{m_{hh/lh}} = \frac{1}{\hbar^2} \left[ -A \pm \sqrt{B^2 + \frac{C^2}{5}} \right]$
  - DKK parameters:  $A = \frac{1}{3} [F + 2G + 2M] + 1$   
 $B = \frac{1}{3} [F + 2G - M]$   
 $C = \frac{1}{3} [(F - G + M)^2 - (F + 2G - M)^2]$
- Fit parameters:  
 $E_0, \gamma, (A_1, B_1)$
- Calculated  
parameters:  
 $A_{hh/lh}$  and  $R_{hh/lh}$
- $F(T) = -\frac{E_{P,4K} \left( \frac{a_{4K}}{a(T)} \right)}{E_0(T)}$
- $M(T) = -\frac{E_{Q,4K} \left( \frac{a_{4K}}{a(T)} \right)}{E'_0(T)}$
- $G(T) = -G_{4K} \left( \frac{a_{4K}}{a(T)} \right)$

C. Tanguy, Phys. Rev. B **60**, 10660 (1999).

M. Cardona, J. Phys. Chem. Solids **24**, 1543 (1963).

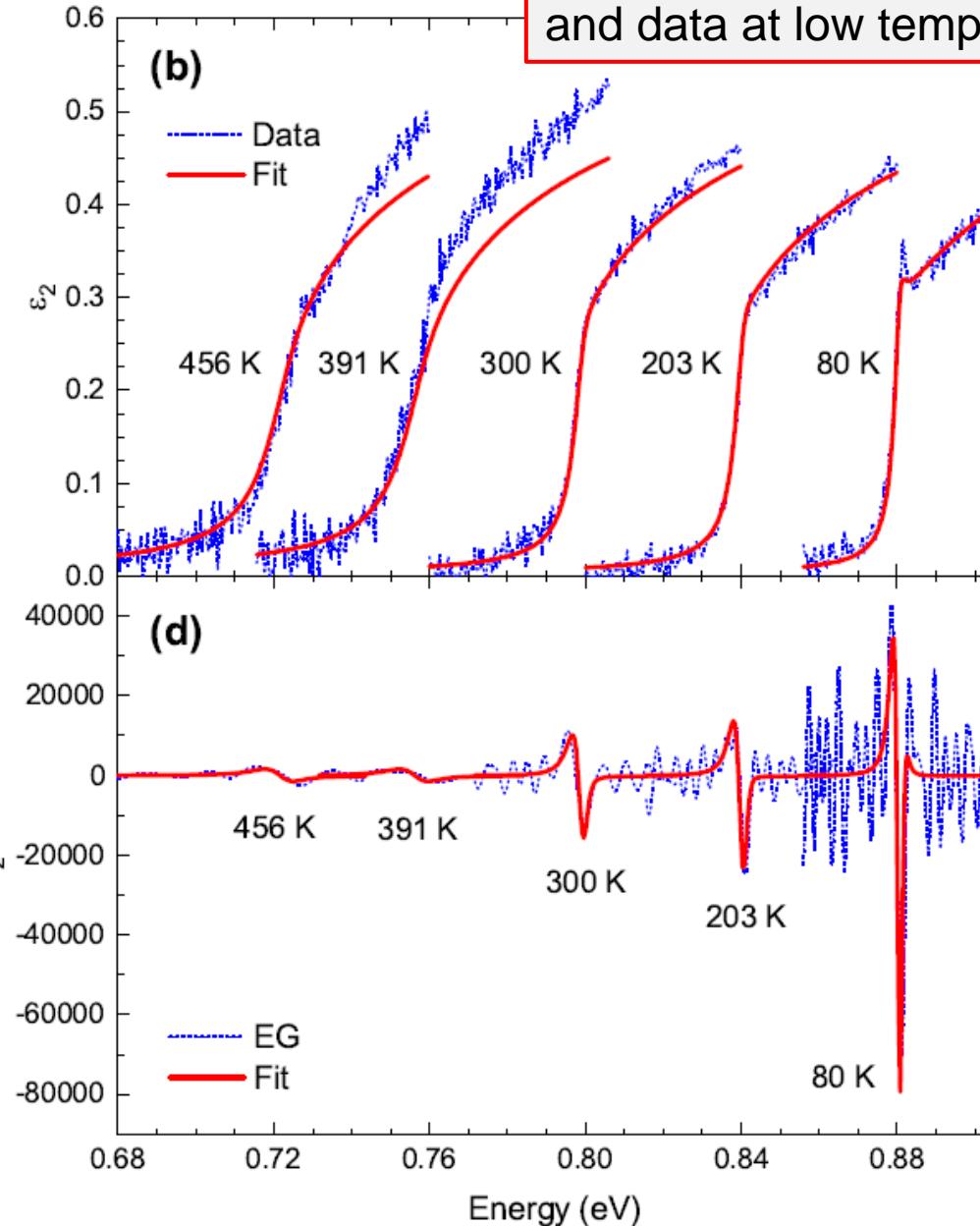
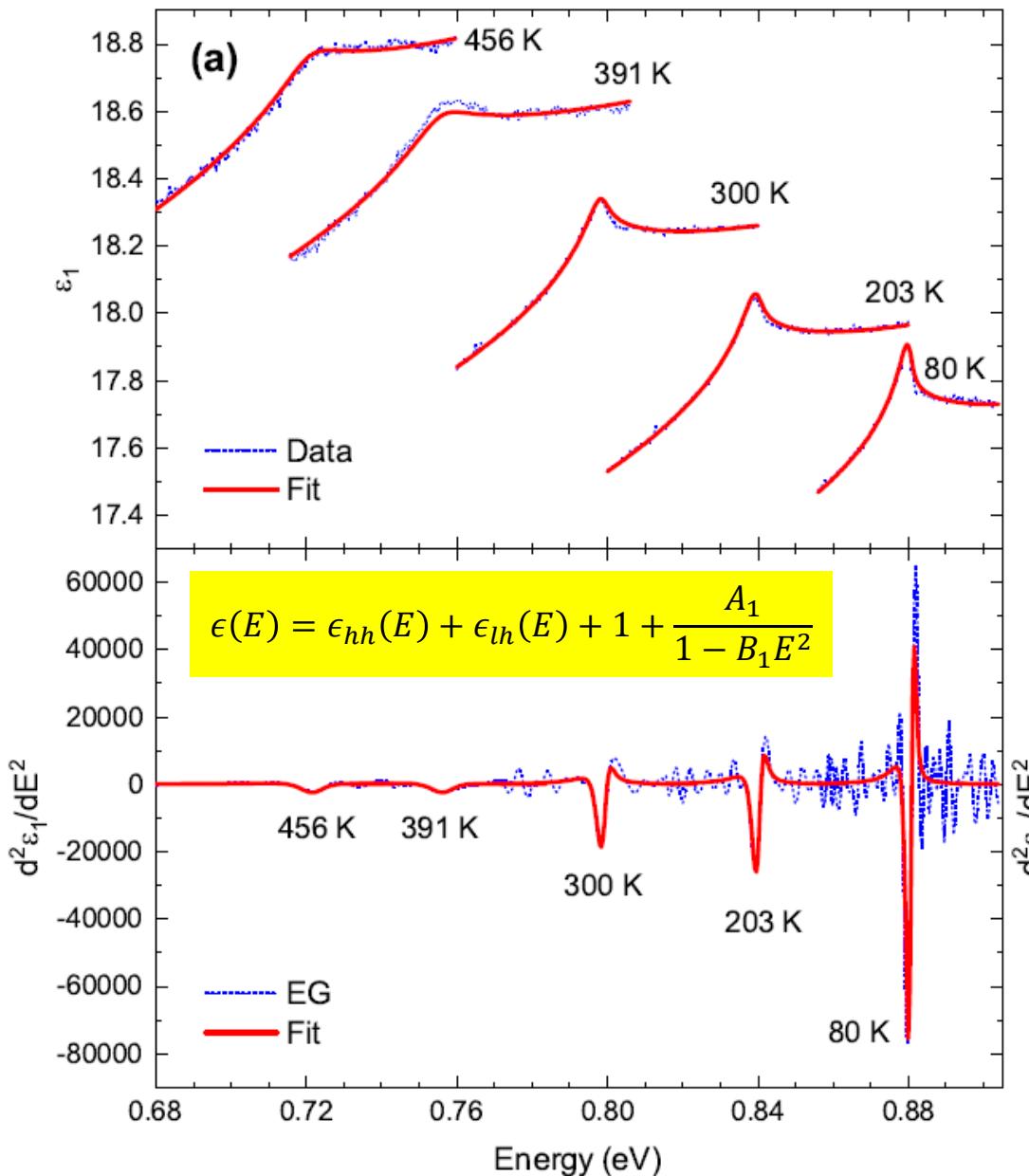
C. Persson and U. Linddefelt, J. Appl. Phys. **82**, 5496 (1997).

G. Dresselhaus, A. F. Kip, and C. Kittel, Phys. Rev. **98**, 368 (1955).

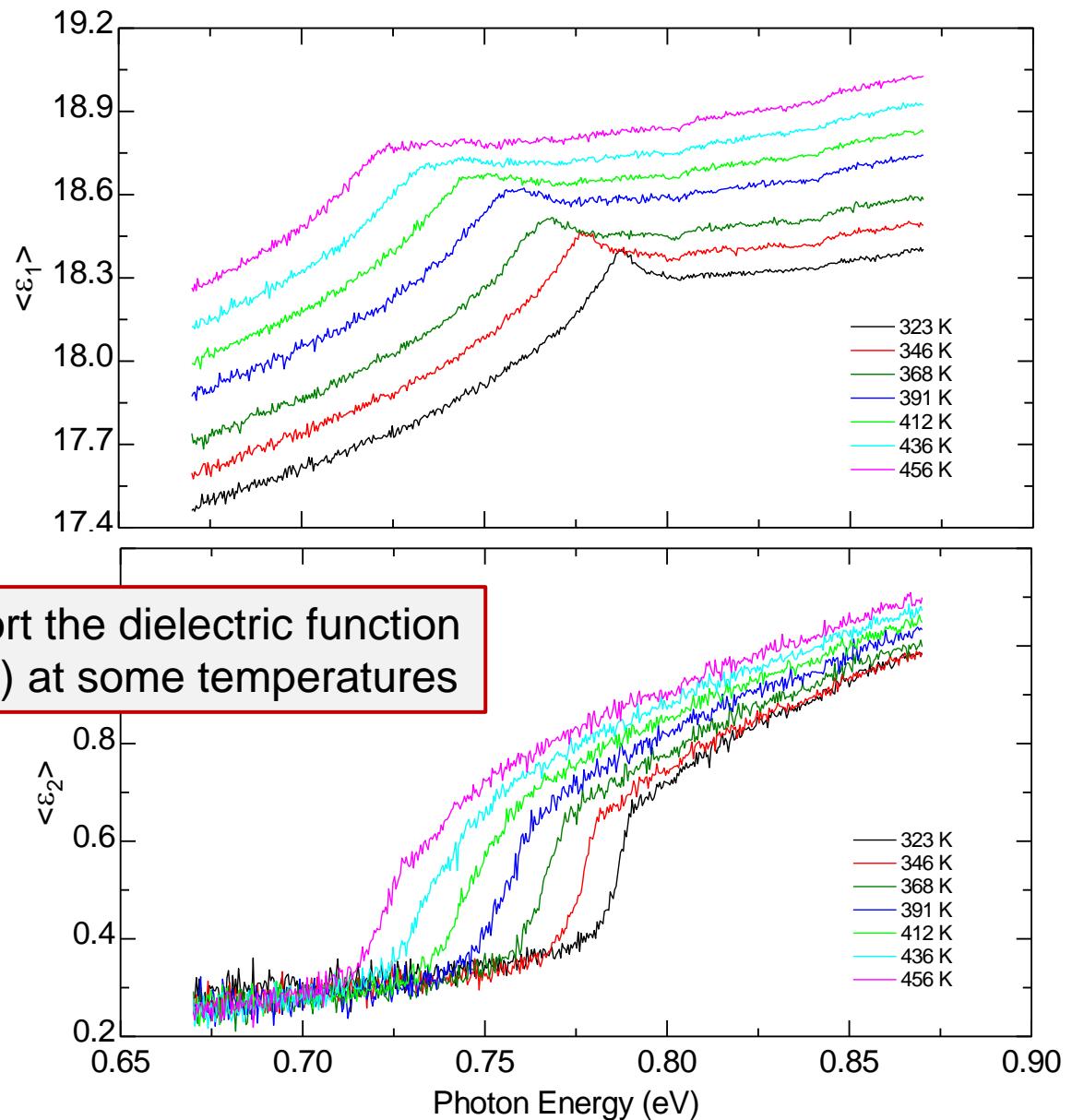
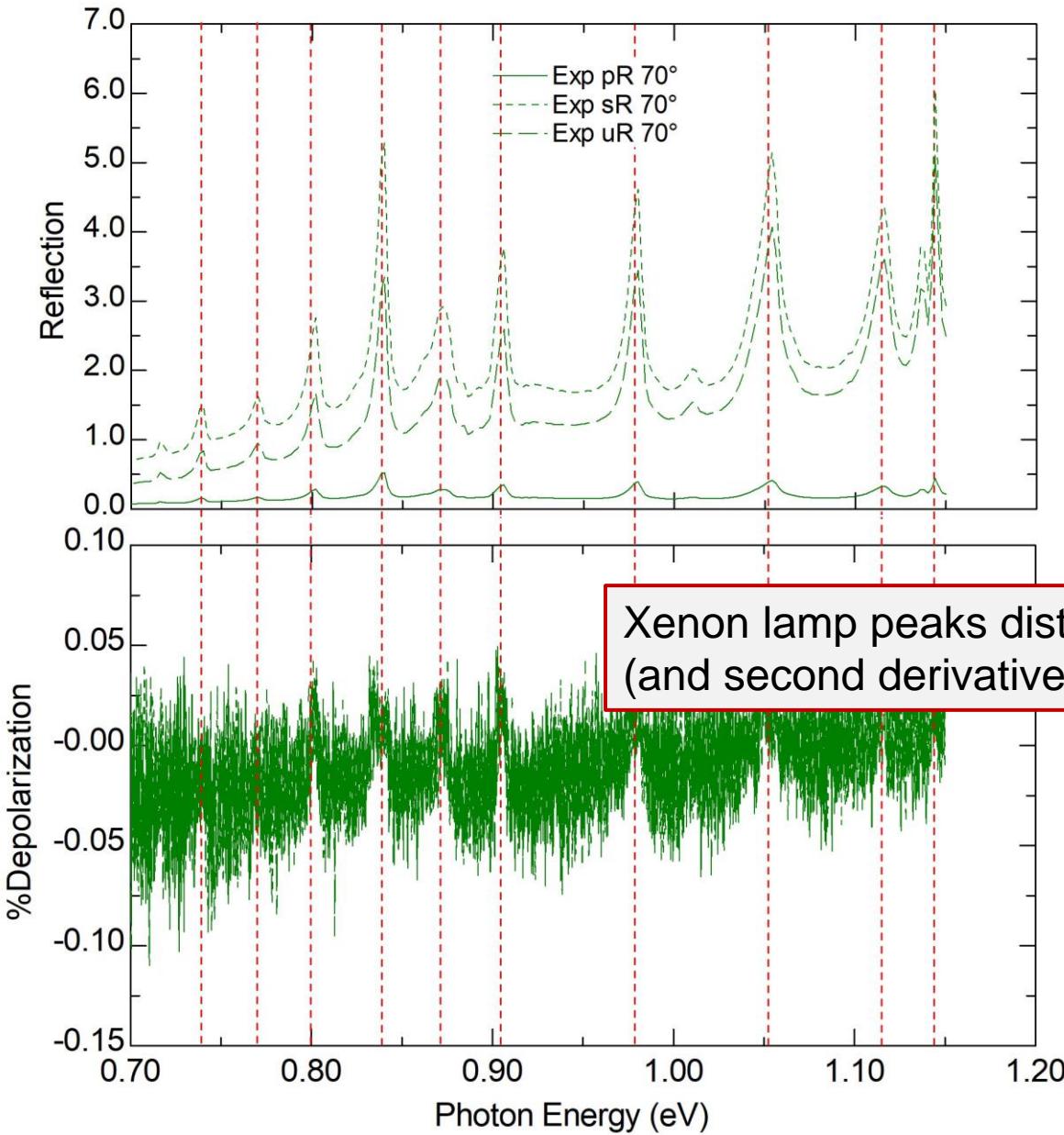
J. Menéndez, D. J. Lockwood, J. C. Zwinkels, M. Noël, Phys. Rev. B **98**, 165207 (2018).

P. Yu and M. Cardona, *Fundamentals of Semiconductors*, (Springer, Heidelberg, 2010).

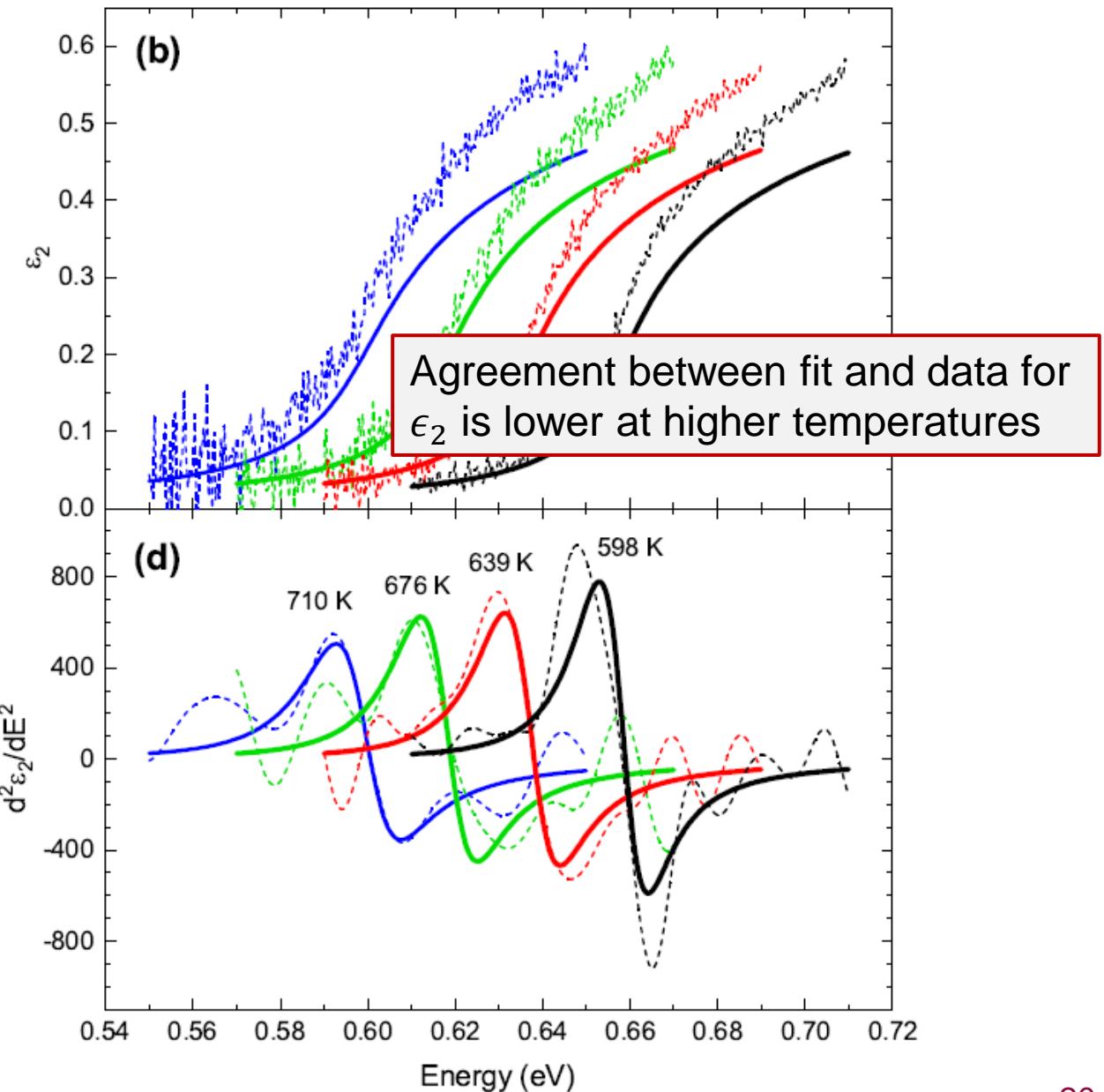
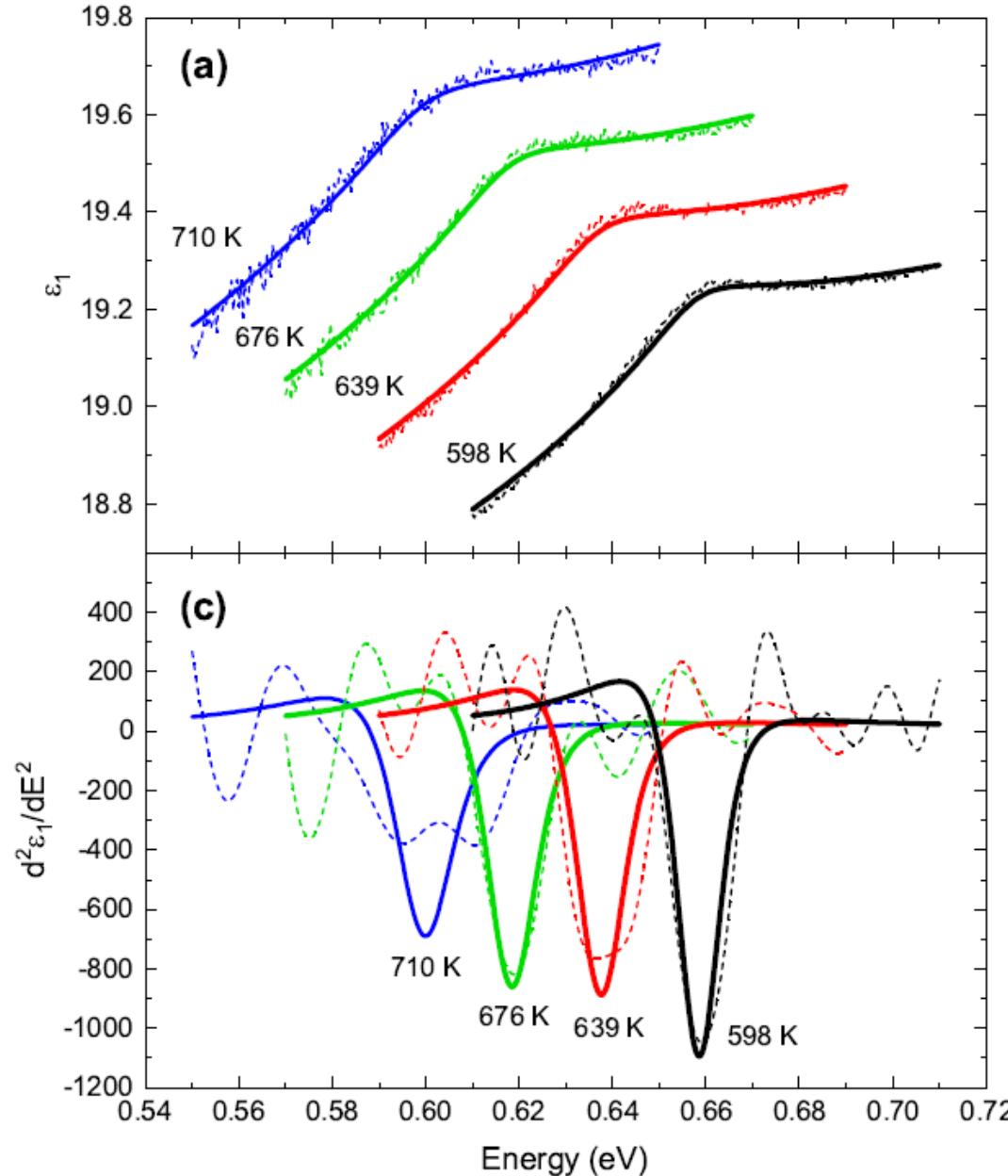
# Fit results for Ge



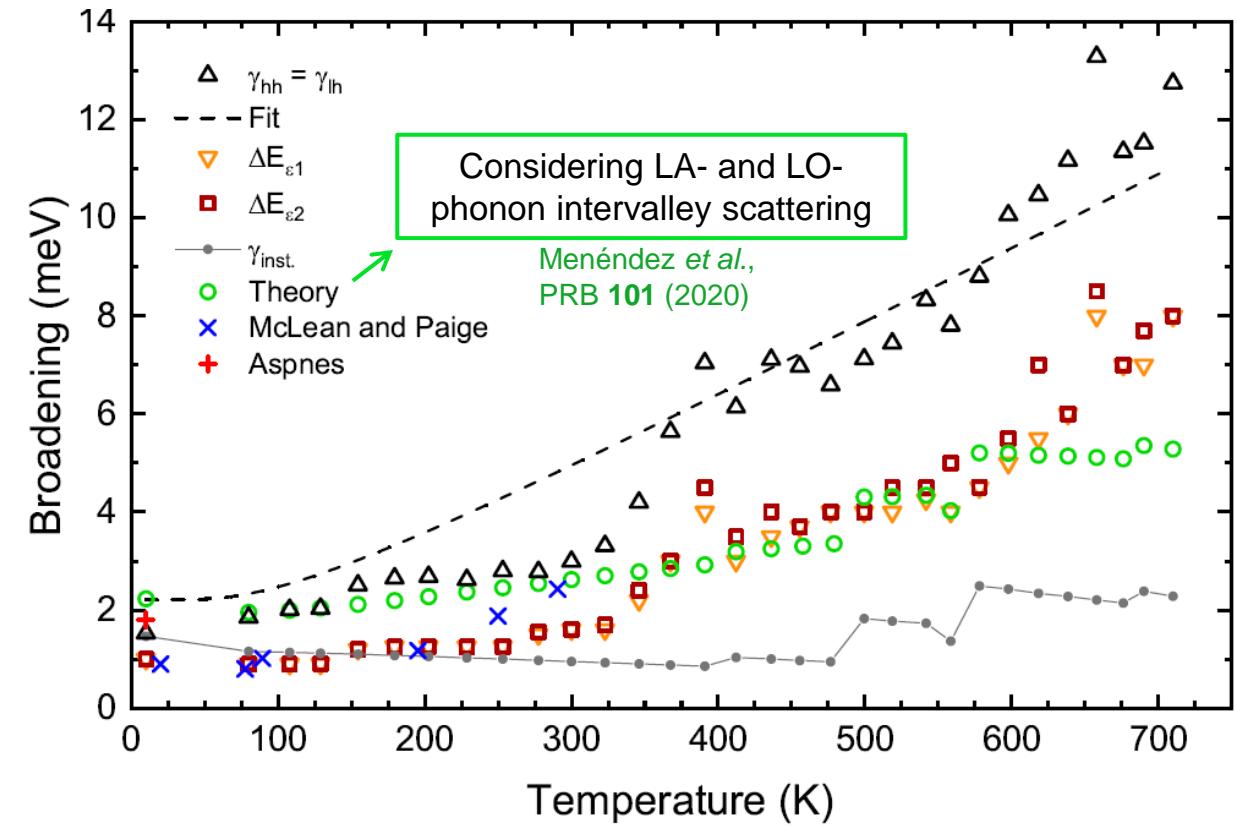
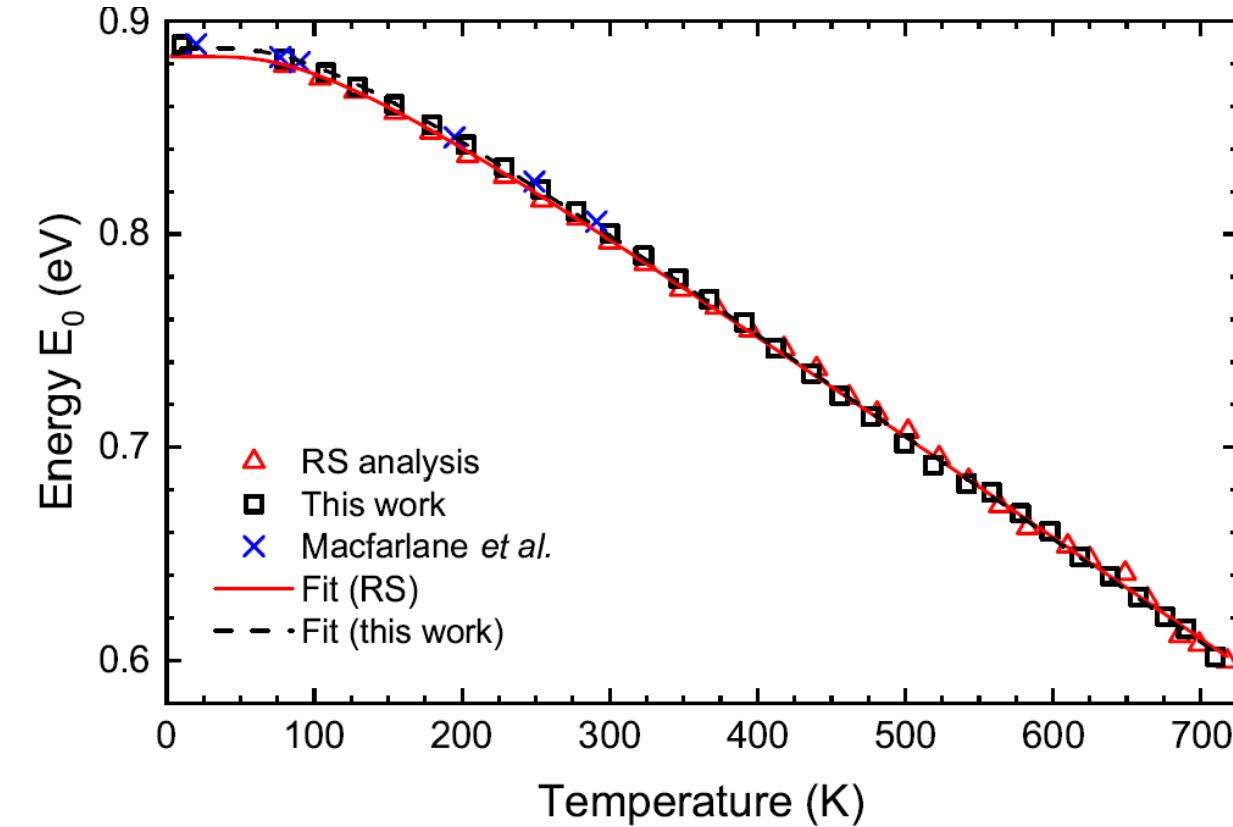
# Distortions due to xenon lamp



# Fit results at high temperatures



# Temperature dependence of the energy and broadening of $E_0$



$$E(T) = E_a - E_b \left[ \frac{2}{e^{\frac{E_{ph}}{kT}} - 1} + 1 \right] \Rightarrow E_{ph} = 25 \pm 1 \text{ meV}$$

$$\gamma(T) = \gamma_a + \gamma_b \left[ \frac{2}{e^{\frac{E_{ph}}{kT}} - 1} + 1 \right]$$

L. Viña, S. Logothetidis, M. Cardona, Phys. Rev. B **30**, 1979 (1984).

C. Emminger, F. Abadizaman, N.S. Samarasingha, T.E. Tiwald, S. Zollner, J. Vac. Sci. Technol. B **38**, 012202 (2020).

G. G. Macfarlane, T. P. McLean, J. E. Quarrington, and V. Roberts, Proc. Phys. Soc. **71**, 863 (1958).

T. P. McLean and E. G. S. Paige, J. Phys. Chem. Solids **23**, 822 (1962).

# Intravalley and intervalley scattering rates

Electron-LA phonon intervalley (Conwell 1967):

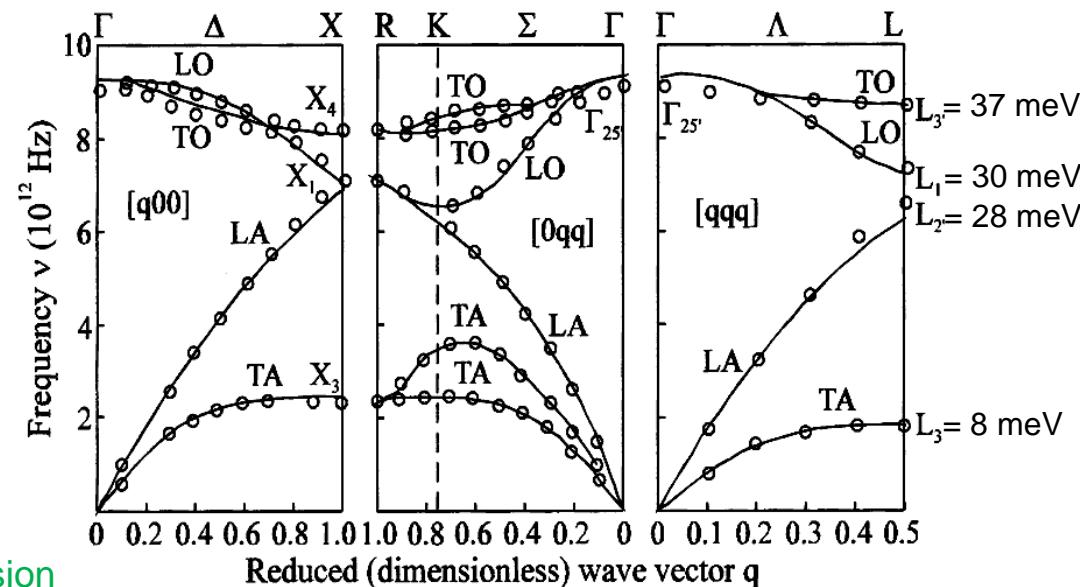
$$\tau_{\Gamma L}^{-1} = N_V \frac{D_{\Gamma L}^2 m_{\text{eff}}^{3/2}}{\sqrt{2\pi\hbar^2\rho E_{\text{ph}}}} \left[ N_{\text{ph}} \sqrt{\Delta E + E_{\text{ph}}} + (1 + 2N_{\text{ph}}) \sqrt{\Delta E - E_{\text{ph}}} \right]$$

$D_{\Gamma L} = 3 \text{ eV} - 6.5 \text{ eV}$  ... T-dep. DP (Zollner 1990)

$$m_{\text{eff}} = (m_l m_t)^{1/3} = (1.6 \cdot 0.08^2)^{1/3} m_0 = 0.22 m_0$$

$$N_V = 4$$

$N_{\text{ph}}$  phonon occupation factor  
=> absorption + emission



Electron-LA phonon intravalley scattering:

$$\tau_{\text{ac}}^{-1} = \frac{\sqrt{2}E_1^2 m_{e\Gamma}^{3/2} k_B T}{\pi\hbar^4 \rho v_s^2} \sqrt{E_k} \longrightarrow 0 \text{ if } E_k = 0 \text{ (we use: } E_k = 10 \text{ meV)}$$

$$\gamma = \hbar/(2\tau)$$

$E_1 = 11.4 \text{ eV}$  ... deformation potential (DP)

$v_s = 5.4 \times 10^3 \text{ m/s}$  ... sound velocity

Hole-optical phonon intravalley scattering:

$$\tau_{\text{op},h}^{-1} = \frac{D_0^2 m_h^{3/2}}{\sqrt{2\pi\hbar^2\rho} \sqrt{E_{\text{ph}}}} N_{\text{ph}}$$

only absorption for  $E_k = 0$

$d_0 = 37 \text{ eV}$  ... DP (Pötz and Vogl 1981)

$$D_0 = d_0/a = 7.53 \text{ eV/Å}$$

	$\tau_{\text{ac}}$ (fs)	$\gamma_{\text{ac}}$ (meV)	$\tau_{\text{op,hh}}$ (fs)	$\gamma_{\text{op,hh}}$ (meV)	$\tau_{\text{op,lh}}$ (fs)	$\gamma_{\text{op,lh}}$ (meV)	$\tau_{\Gamma L}$ (fs)	$\gamma_{\Gamma L}$ (meV)
10 K	$4 \times 10^5$	$8 \times 10^{-4}$	$3 \times 10^{21}$	$1 \times 10^{-19}$	$1 \times 10^{23}$	$3 \times 10^{-21}$	$1 \times 10^3$	0.3
80 K	$5 \times 10^4$	$6 \times 10^{-3}$	$2 \times 10^5$	$2 \times 10^{-3}$	$5 \times 10^6$	$7 \times 10^{-5}$	600	0.6
300 K	$1 \times 10^4$	0.02	$3 \times 10^3$	0.1	$8 \times 10^4$	$4 \times 10^{-3}$	100	3
710 K	$6 \times 10^3$	0.06	700	0.4	$3 \times 10^4$	0.01	60	6

D. K. Ferry, *Semiconductor Transport*, (Tayler & Francis, New York, 2000).

E. M. Conwell, *High Field Transport in Semiconductors* (Academic, New York, 1967).

W. Pötz and P. Vogl, Phys. Rev. B 24, 2025 (1981).

S. Zollner, S. Gopalan, and M. Cardona, Sol. State Comm. 76, 877 (1990).

# Excitonic binding energy

Excitonic binding (Rydberg) energy:  $R_{hh/lh} = \frac{\mu_{hh/lh}}{\epsilon_{st}^2} 13.6 \text{ eV}$

Temperature-dependent due to  $T$  dependence of  $\epsilon_{st}$  and effective masses

Reduced mass:  $\frac{1}{\mu_{hh/lh}} = \frac{1}{m_{hh/lh}} + \frac{1}{m_{e\Gamma}}$

$T$  dependence of the electron effective mass through  $T$ -dependent band gap  $E_0$

$$\frac{m_0}{m_{e\Gamma}} = 1 + \frac{E_P}{3} \left[ \frac{2}{E_0} + \frac{1}{E_0 + \Delta_0} \right]$$

Hole effective masses:  $\frac{m_0}{m_{hh/lh}} = \frac{1}{\hbar^2} \left[ -A \pm \sqrt{B^2 + \frac{C^2}{5}} \right]$

Matrix element do not change much with  $T$

$$E_{P(T)} = E_{P,4K} \left( \frac{a_{4K}}{a(T)} \right)$$

=>  $T$  dependence due to DKK parameters:

$$A = \frac{1}{3}[F + 2G + 2M] + 1$$

$$B = \frac{1}{3}[F + 2G - M]$$

$$C = \frac{1}{3}[(F - G + M)^2 - (F + 2G - M)^2]$$

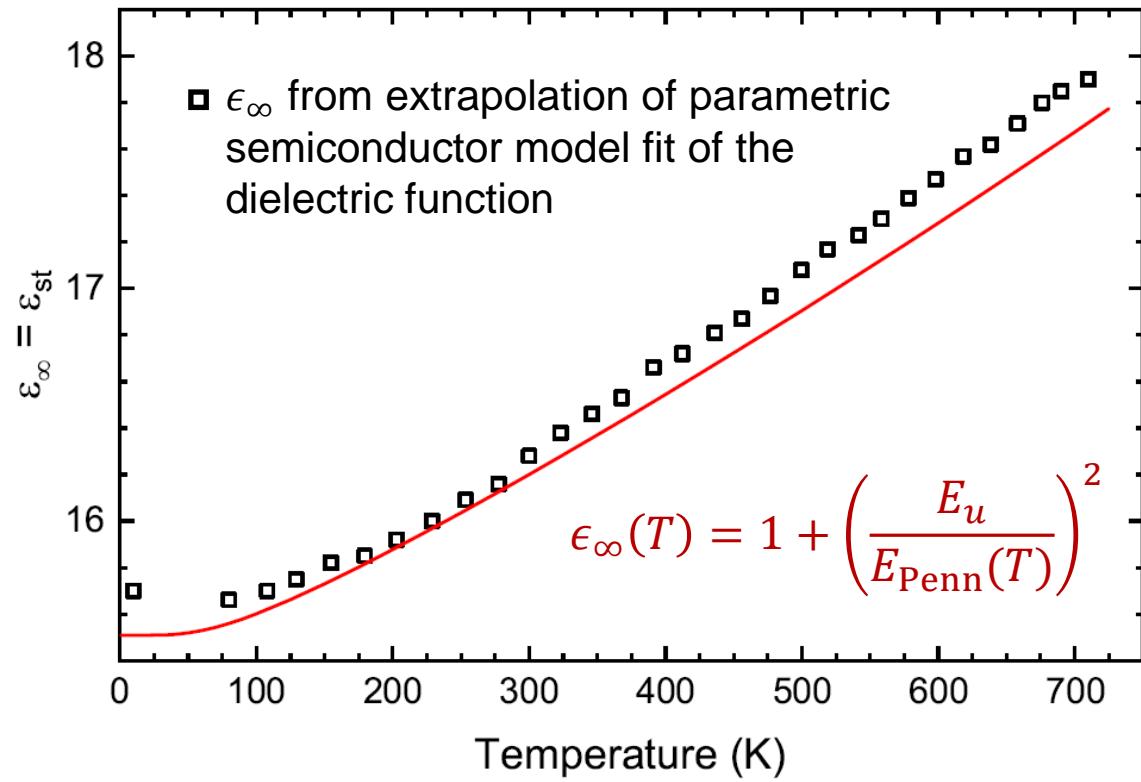
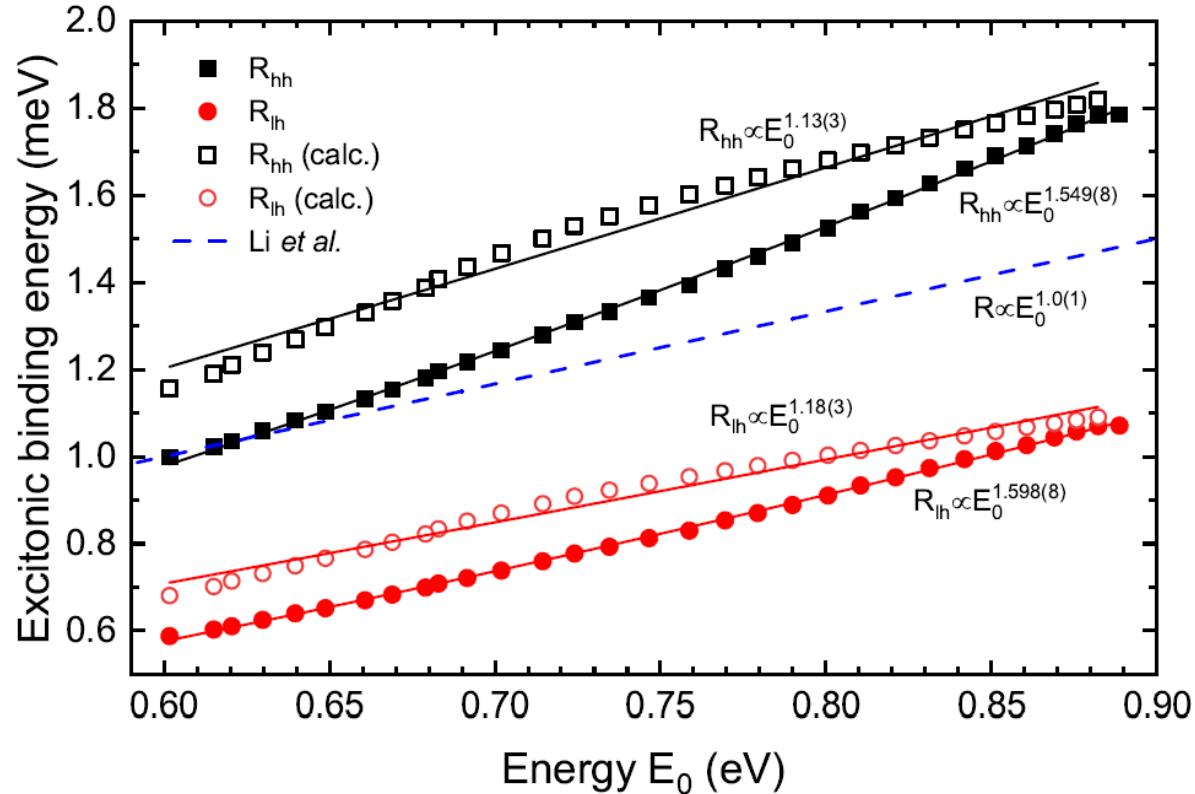
$$F(T) = -\frac{E_{P,4K} \left( \frac{a_{4K}}{a(T)} \right)}{E_0(T)}$$

$$M(T) = -\frac{E_{Q,4K} \left( \frac{a_{4K}}{a(T)} \right)}{E'_0(T)}$$

$$G(T) = -G_{4K} \left( \frac{a_{4K}}{a(T)} \right)$$

=>  $T$  dependence stems mainly from  $E_0(T)$  and  $E'_0(T)$  (and  $\epsilon_{st}$ )

# Excitonic binding energy and high-frequency dielectric constant



Excitonic binding energy depends on  $\epsilon_{st} = \epsilon_{\infty}$ :

$$R_{hh/lh} \propto \epsilon_{st}^{-2}$$

$$E_u = \hbar\omega_u = 15.6 \text{ eV} \quad (\omega_u: \text{Plasma frequency})$$

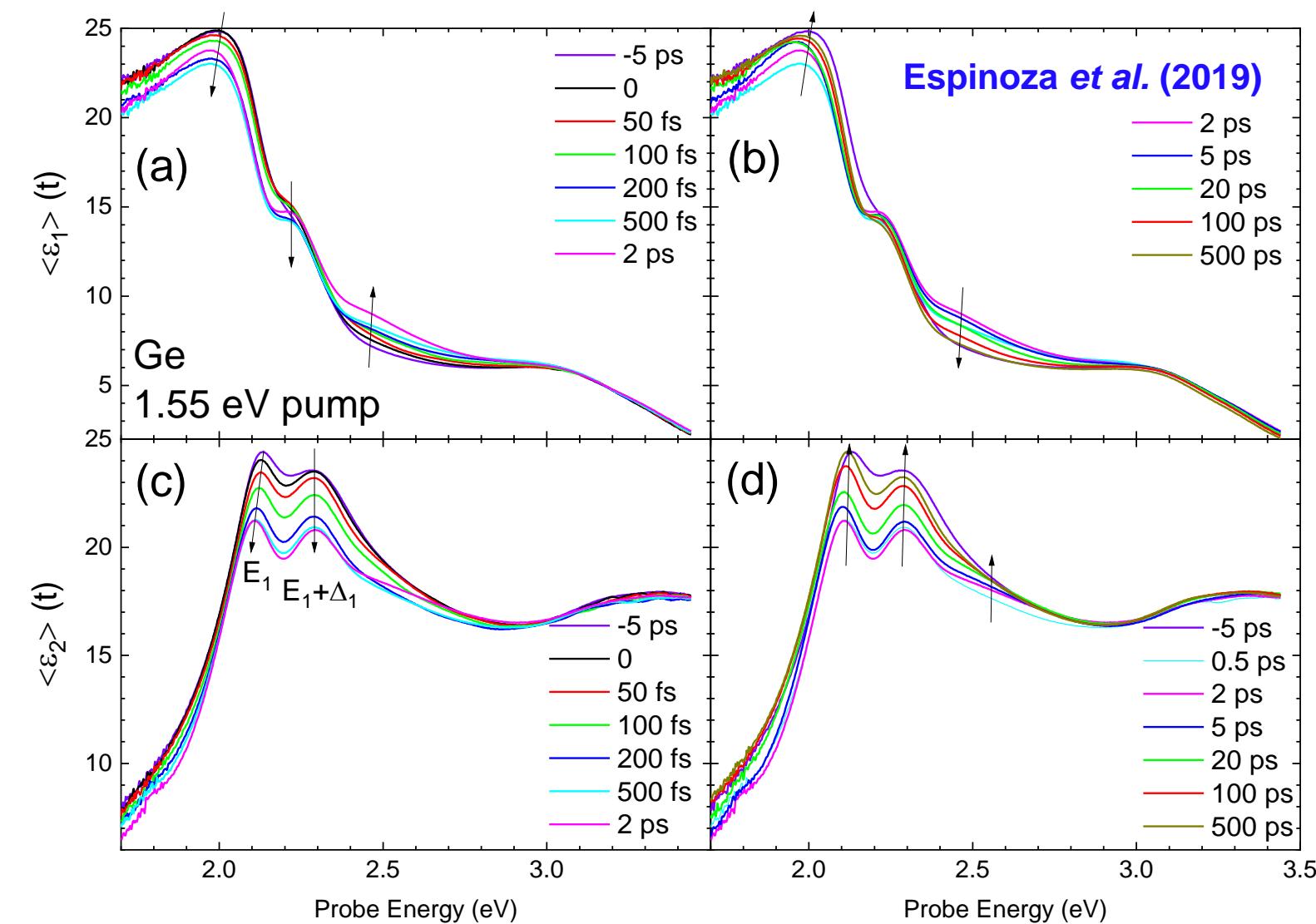
$T$  dependence of Penn gap similar to  $E'_0(T)$

$$E_{Penn}(T) = 4.146 \text{ eV} - 0.05 \text{ eV} \left( \frac{2}{e^{217 \text{ K}/T} - 1} + 1 \right)$$

## **Part 2:** Transient critical point parameters of Ge and Si from femtosecond pump-probe ellipsometry

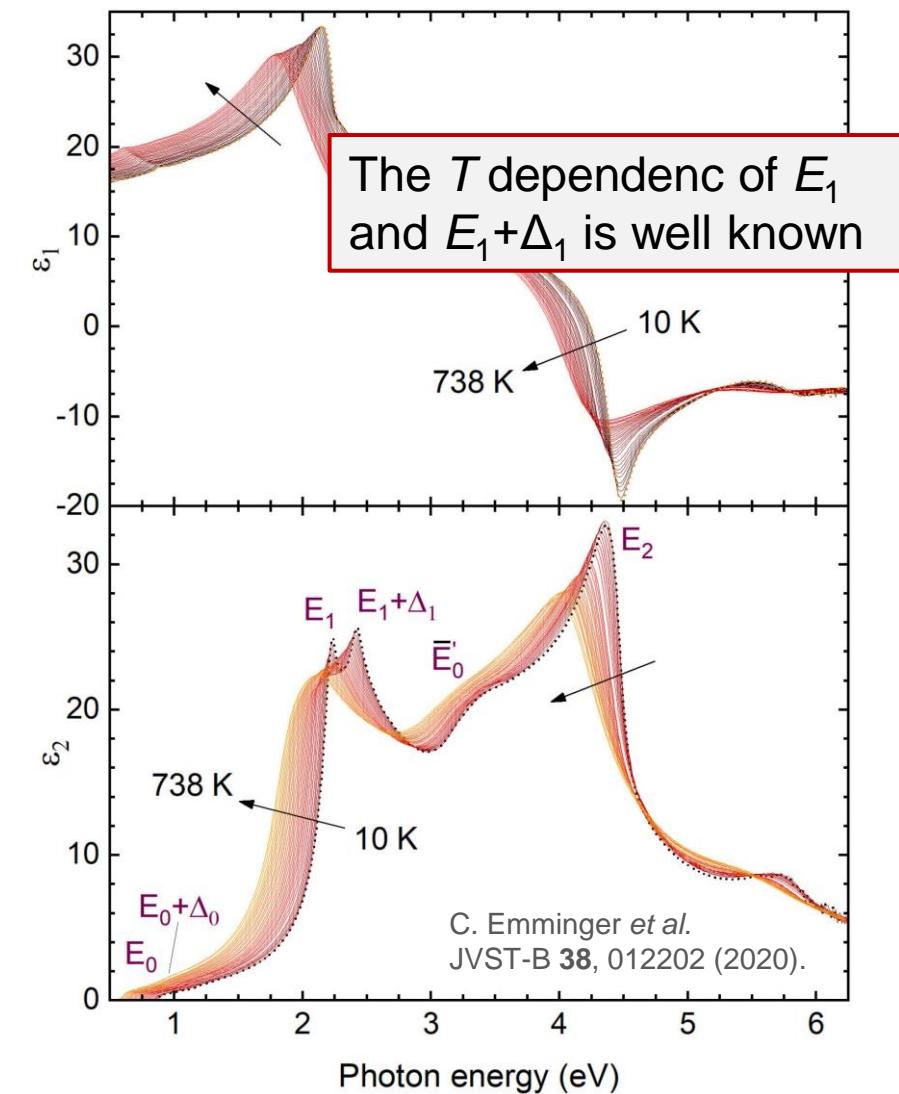
## Transient pseudodielectric function from pump-probe spectroscopic ellipsometry

## Temperature dependent dielectric function from spectroscopic ellipsometry



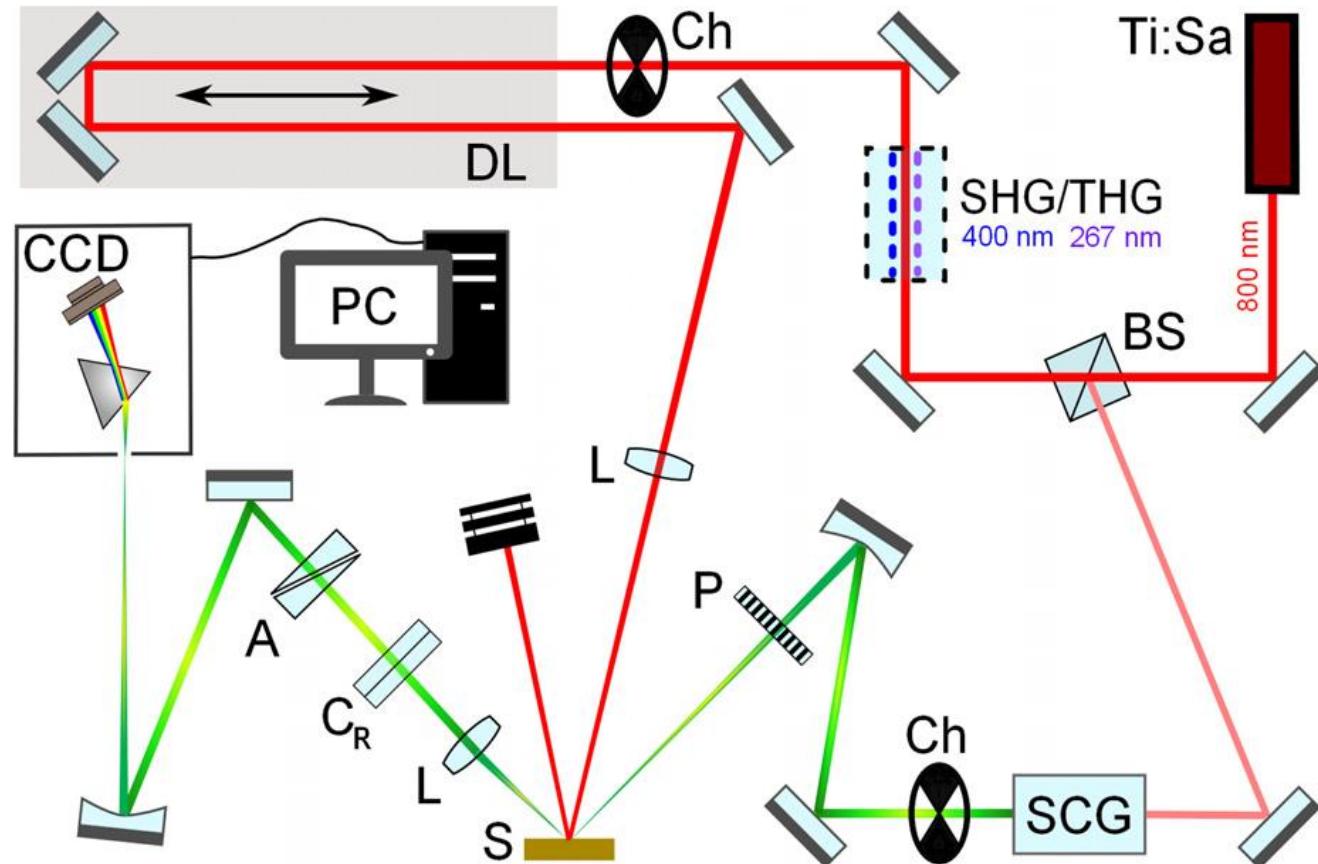
S. Espinoza, S. Richter, M. Rebarz, O. Herrfurth, R. Schmidt-Grund,  
J. Andreasson, and S. Zollner, Appl. Phys. Lett. **115**, 052105 (2019).

L. Viña, S. Logothetidis, and M. Cardona, Phys. Rev. B **30**, 1979 (1984).  
N. S. Fernando et al., Appl. Surf. Sci. **421**, 905 (2017).

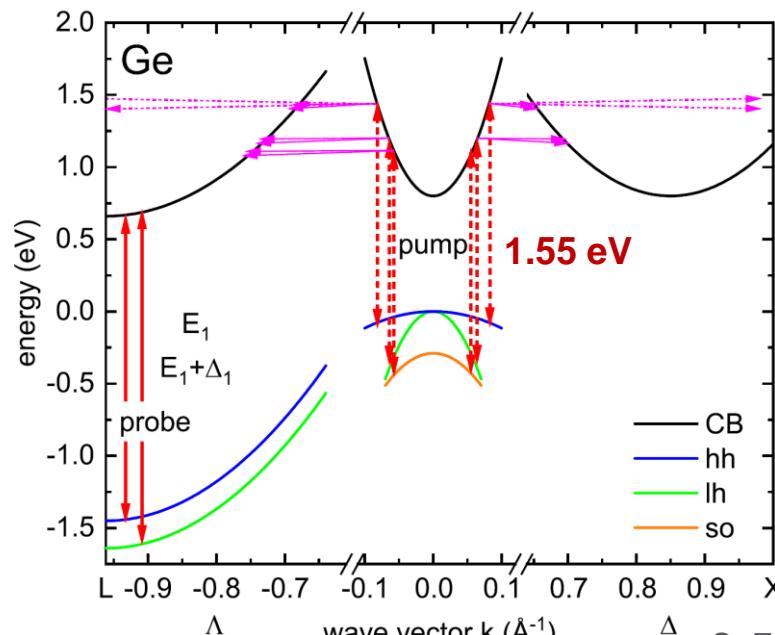
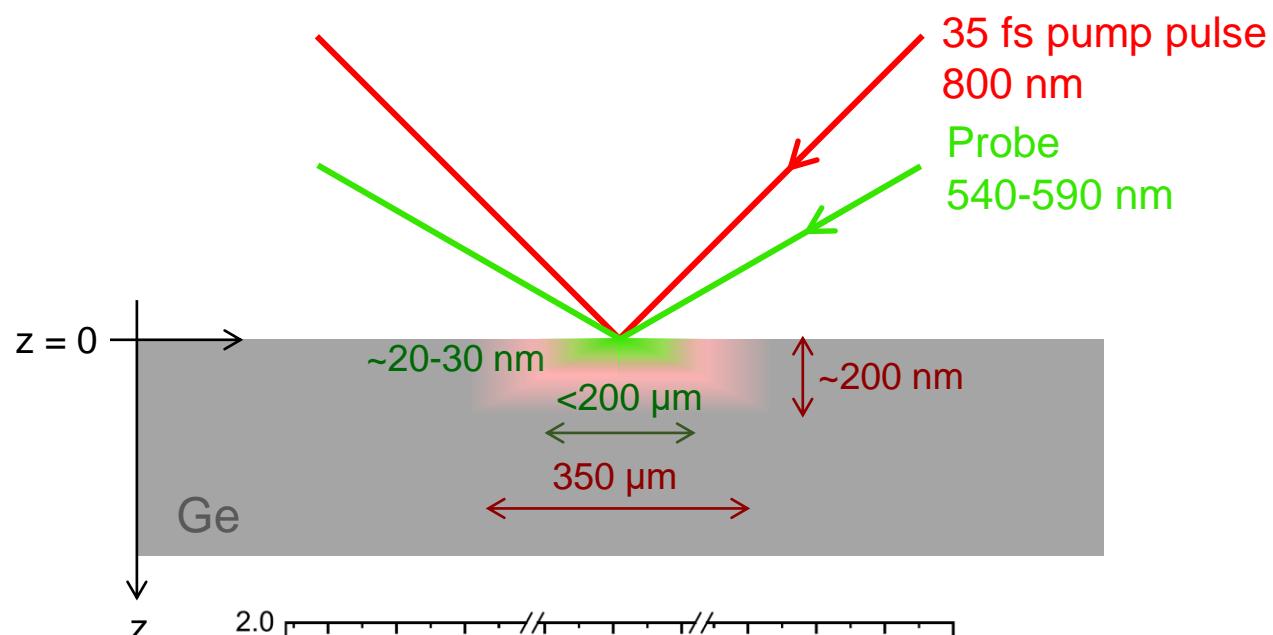


# Pump-probe spectroscopic ellipsometry setup

- Pump pulse: 266, 400, and 800 nm
- 35 fs laser pulses
- Repetition rate: 1 kHz
- Pulse energy: up to 6 mJ
- Carrier density:  $10^{20} \text{ cm}^{-3}$
- Time resolution: 120 fs (oblique incidence)
- Spectral range: 1.7 – 3.5 eV
- Probe beam diameter <200  $\mu\text{m}$
- Pump beam diameter ~350  $\mu\text{m}$

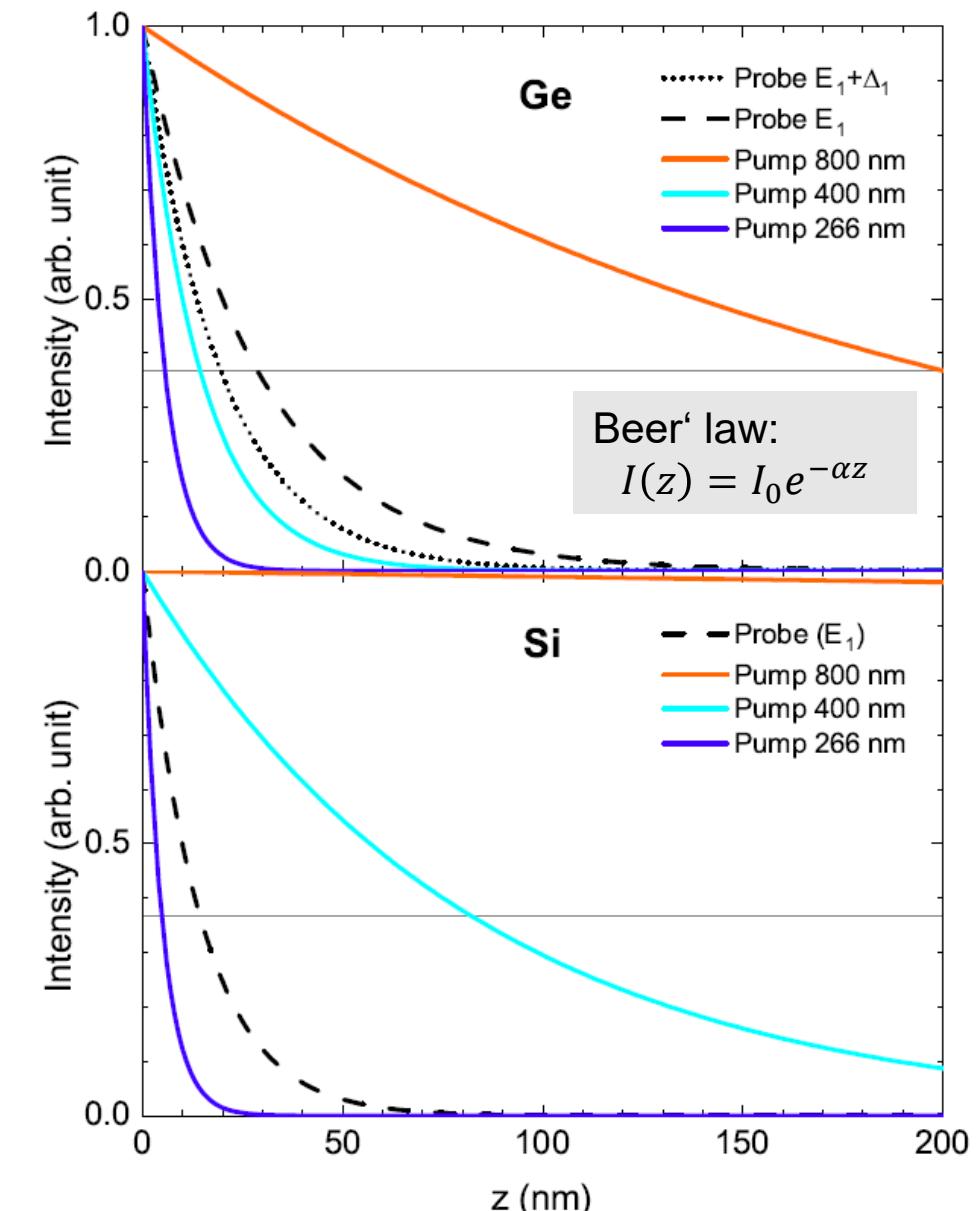


# Penetration depth of probe and pump beams



Carrier density:  
 $10^{20} \text{ cm}^{-3}$

Electrons  
scatter from  $\Gamma$   
to X and L



# Calculation of the second derivatives

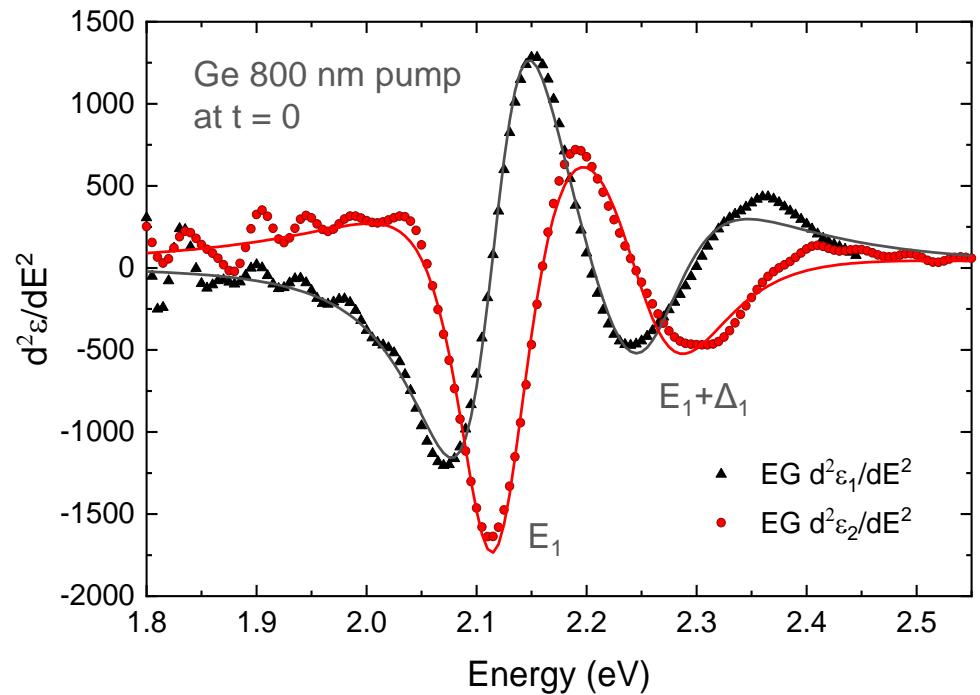
Second derivative of the DF using EG-filters for  $M = 4$

- for data sets with equidistant energy steps  $\Delta E$ :

$$\frac{d^2\bar{\epsilon}(E)}{dE^2} \approx \frac{\Delta E'}{49152\sqrt{\pi}\Delta E^{13}} \sum_{j=-\infty}^{\infty} \epsilon(E_j) \left( (E - E_j)^{10} - 106(E - E_j)^8 \Delta E^2 + 3608(E - E_j)^6 \Delta E^4 - 45936(E - E_j)^4 \Delta E^6 + 188496(E - E_j)^2 \Delta E^8 - 110880 \Delta E^{10} \right) e^{-\frac{(E-E_j)^2}{4\Delta E^2}}$$

- for data sets with nonconstant energy steps:

$$\frac{d^2\bar{\epsilon}(E)}{dE^2} \approx \frac{1}{49152\sqrt{\pi}\Delta E^{13}} \sum_{j=-\infty}^{\infty} \epsilon(E_j) \left( (E - E_j)^{10} - 106(E - E_j)^8 \Delta E^2 + 3608(E - E_j)^6 \Delta E^4 - 45936(E - E_j)^4 \Delta E^6 + 188496(E - E_j)^2 \Delta E^8 - 110880 \Delta E^{10} \right) \frac{E_{j+1} - E_{j-1}}{2} e^{-\frac{(E-E_j)^2}{4\Delta E^2}}$$



# Critical point analysis: Second derivatives from linear filters

Second derivatives calculated using a digital linear filter method (Le et al. 2019)

Ge:  $E_1$  and  $E_1 + \Delta_1$

- EG filter width: 12-15 meV
- Fit: 2D-lineshape

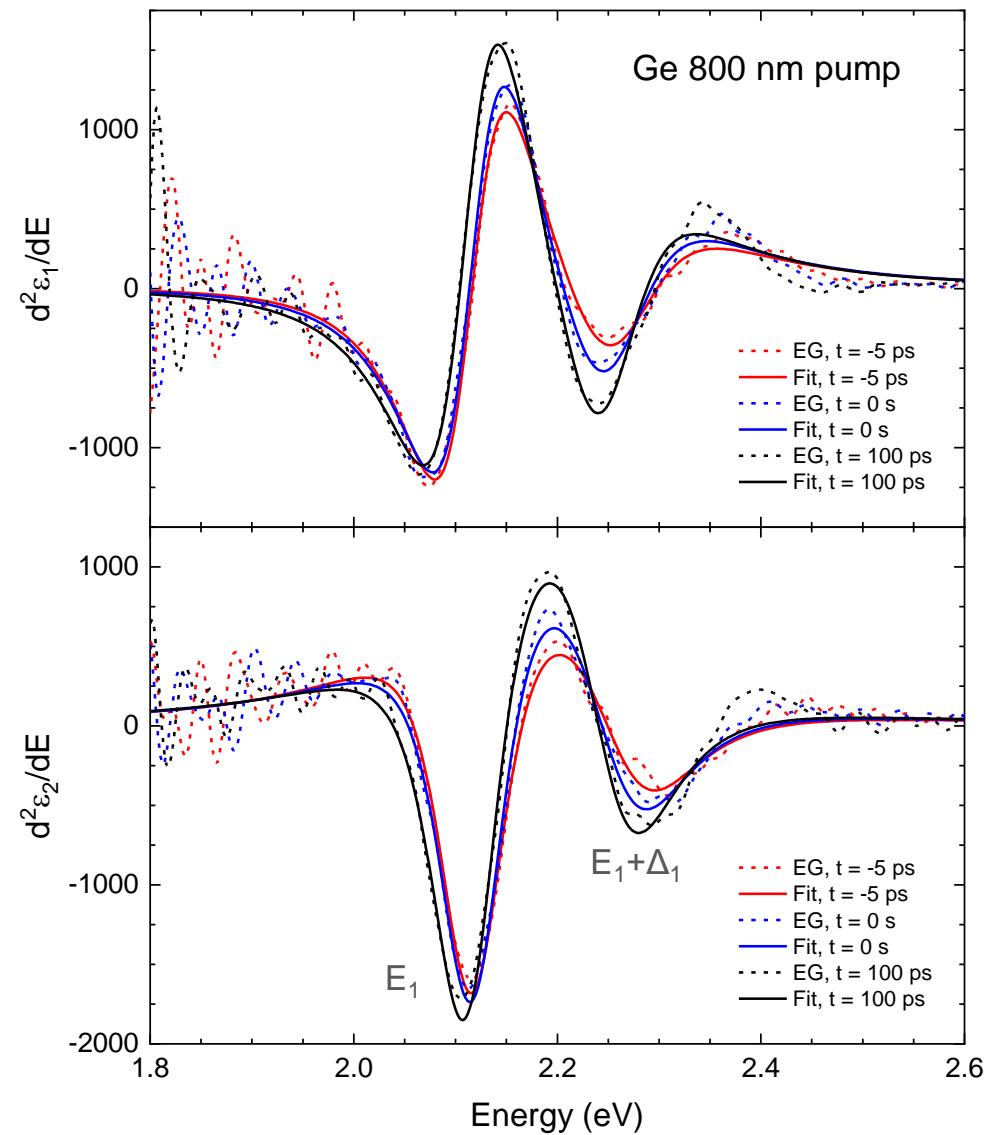
$$\epsilon_{2D}(E) = B - Ae^{i\varphi} \ln(E - E_g + i\Gamma)$$

Si:  $E_1$

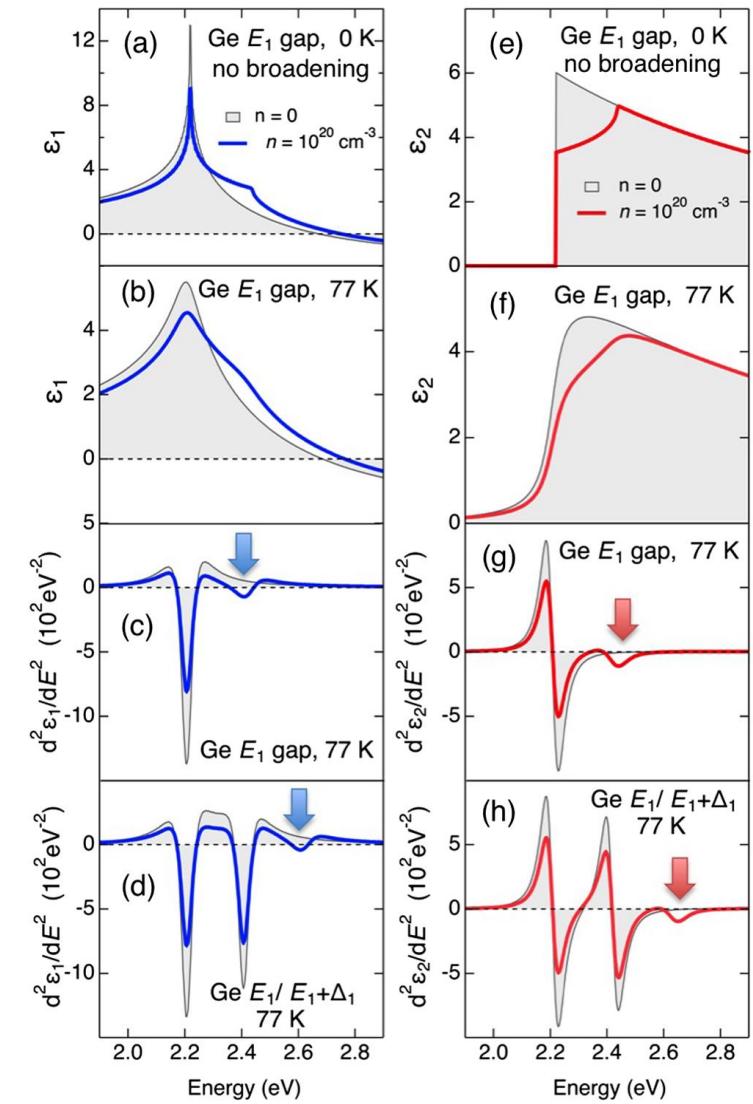
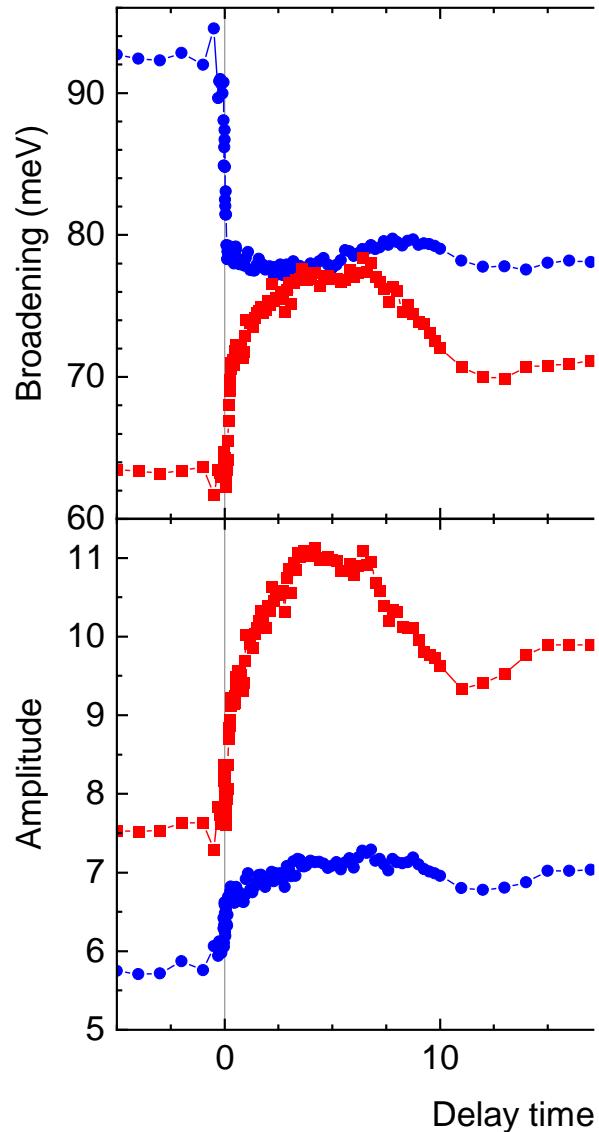
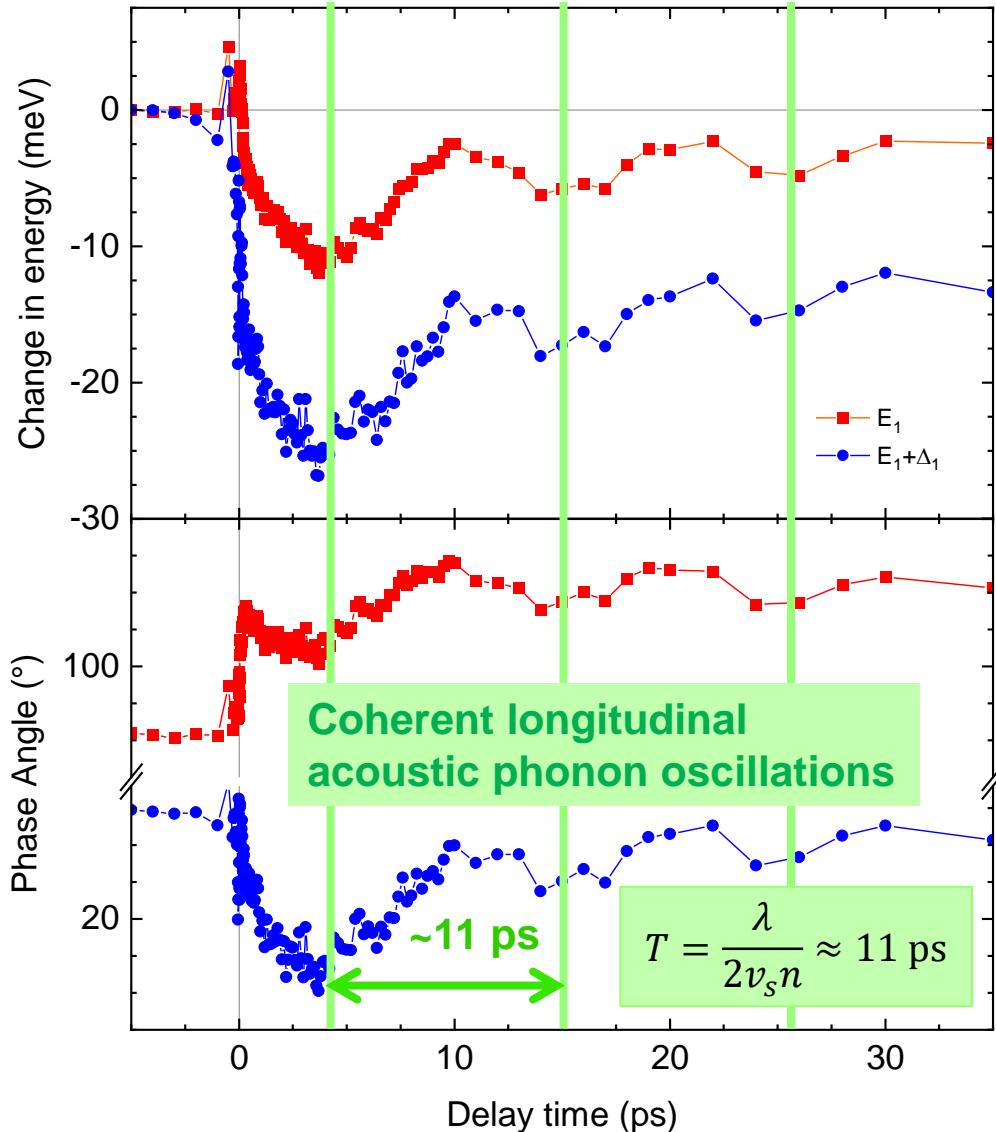
- EG filter width: 20 meV
- Fit: 0D-lineshape

$$\epsilon_{0D}(E) = B - \frac{Ae^{i\varphi}}{E - E_g + i\Gamma}$$

=> Better: Lineshape considering bandfilling effects



# Critical point parameters as functions of delay time – Ge 800 nm pump



C. Xu, N. S. Fernando, S. Zollner, J. Kouvetsakis, and J. Menéndez, Phys. Rev. B 118, 267402 (2017).

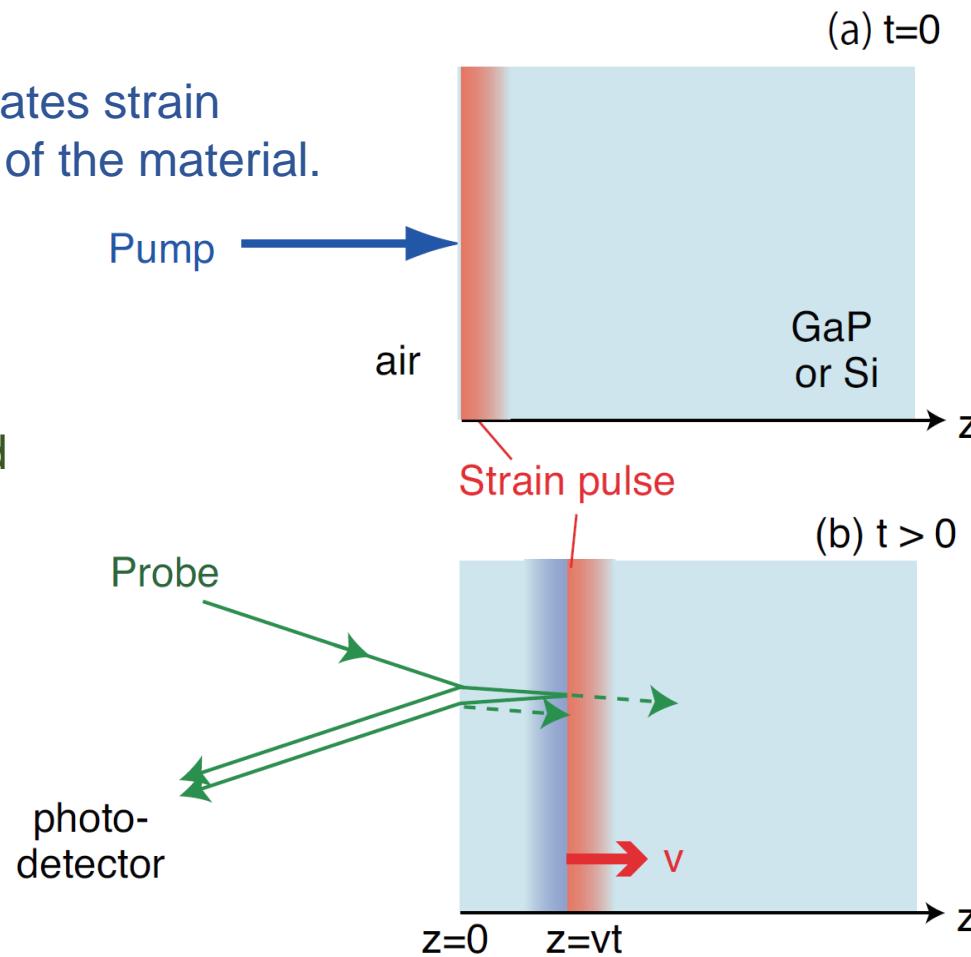
# Creation and propagation of a strain pulse

The pump pulse creates strain close to the surface of the material.

The probe pulse gets reflected by the strain pulse, which moves through the crystal.

$$\text{Period: } T = \frac{\lambda}{2v_s n}$$

$\lambda$  .... probe wavelength  
 $v_s$  ... longitudinal sound velocity  
 $n$  .... refractive index



# Coherent phonon oscillations – energy shifts (Ge 800 nm pump)

The oscillations can be fitted with a damped oscillator and an exponential decay:

$$\Delta E(t) = \Delta E_a(t) + \Delta E_b(t) = -E_a \cos\left(\frac{2\pi t}{T} - \delta\right) e^{\frac{t}{\tau_a}} - E_b e^{\frac{t}{\tau_b}}$$

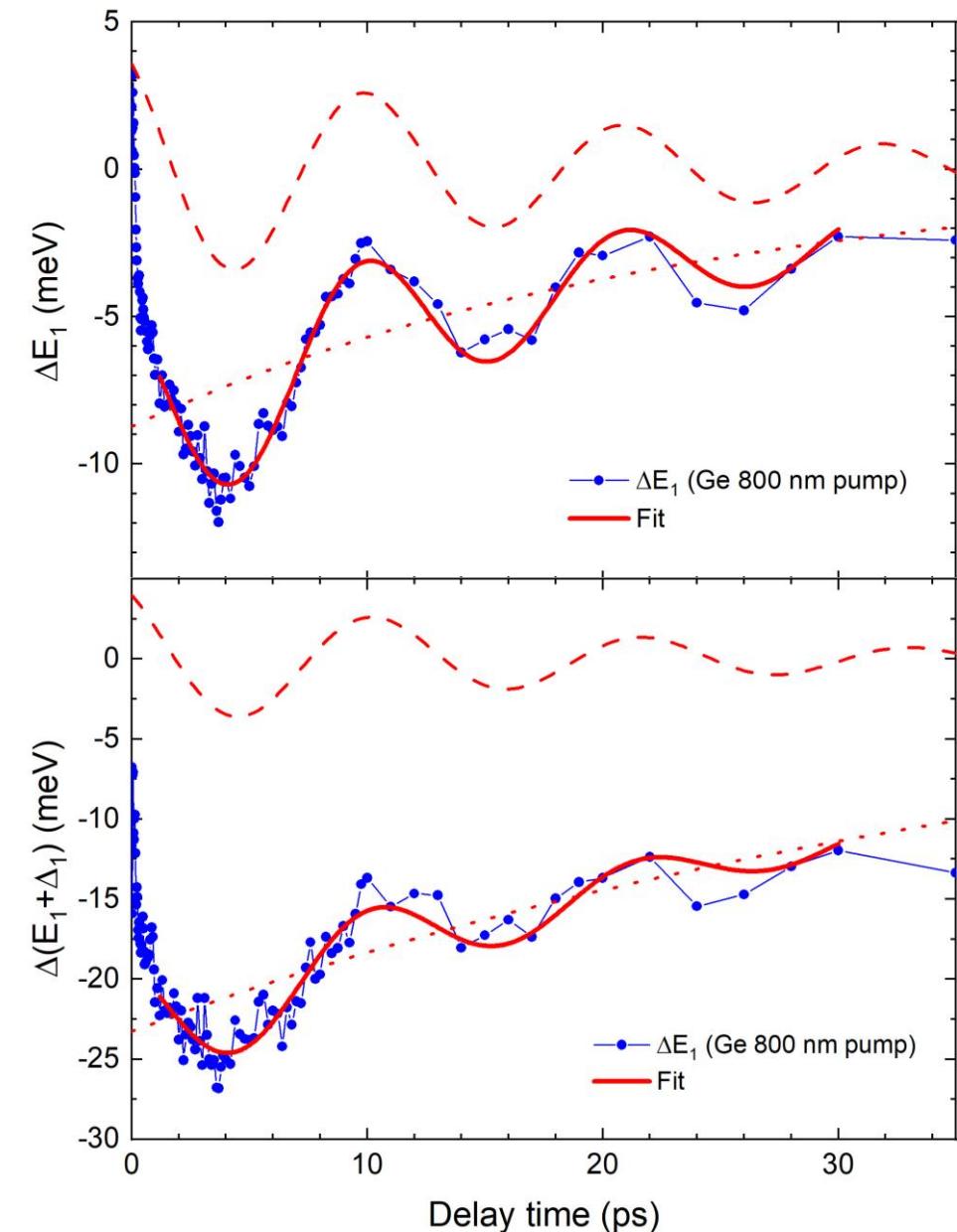
Fit result:

	$\Delta(E_1)$	$\Delta(E_1 + \Delta_1)$
$E_a$ (meV)	$4.2 \pm 0.4$	$4.7 \pm 0.8$
$E_b$ (meV)	$8.7 \pm 0.3$	$23.3 \pm 0.5$
$T$ (ps)	$11.0 \pm 0.2$	$11.4 \pm 0.4$
$\delta$	$2.58 \pm 0.06$	$2.6 \pm 0.1$
$\tau_a$ (ps)	$20 \pm 4$	$18 \pm 7$
$\tau_b$ (ps)	$23 \pm 2$	$42 \pm 3$

Temperature increase:

$$\Delta T \approx \frac{E(1-R)}{cV\rho} \approx 25 \text{ K}$$

$$\Delta E_1 \approx -10 \text{ meV} \Rightarrow \Delta T \approx 20 \text{ K}$$
$$\Delta(E_1 + \Delta_1) \approx -25 \text{ meV} \Rightarrow \Delta T \approx 40 \text{ K}$$



# Calculating strain and energy shifts (Ge 800nm pump)

Stress-strain relation:  $\epsilon_3 = (S_{11} + 2S_{12})\sigma = \frac{\sigma}{C_{11}+2C_{12}}$  (assuming:  $\sigma_{ii} = \sigma$  for all  $i$  and  $\sigma_{ij} = 0$  for  $i \neq j$ )

$$(C_{11} + 2C_{12})^{-1} = 4.44 \times 10^{-8} \frac{\text{cm}^2}{\text{N}}$$

Electron contribution:  $\sigma_{\text{el}} = -B \frac{\partial E_g}{\partial P} N \Rightarrow \epsilon_{\text{el}} = (C_{11} + 2C_{12})^{-1} \sigma_{\text{el}} = -6.4 \times 10^{-4}$

Phonon contribution:  $\sigma_{\text{ph}} = -\frac{3B\beta}{c}(E - E_g)N \Rightarrow \epsilon_{\text{ph}} = (C_{11} + 2C_{12})^{-1} \sigma_{\text{ph}} = -1.2 \times 10^{-4}$

Total stress/strain:  $\sigma_{33} = \sigma_{\text{el}} + \sigma_{\text{ph}} \Rightarrow \epsilon_{33} = (C_{11} + 2C_{12})^{-1} \sigma_{33} = -7.6 \times 10^{-4}$

In-plane and out-of-plane strain:  $\epsilon_{\perp} = \epsilon_{33}$  and  $\epsilon_{\parallel} = 0$

Hydrostatic and shear strain:  $\epsilon_H = \epsilon_S = 2.5 \times 10^{-4}$

Hydrostatic shift:  $\Delta E_H = \sqrt{3}D_1^1 \epsilon_H = -3.4 \text{ meV}$

Shear splitting:  $\Delta E_S = \sqrt{6}D_3^3 \epsilon_S = 1.6 \text{ meV}$

Critical point energy shift:  $\Delta E_1 = \frac{\Delta_1}{2} + \Delta E_H - \sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2} = -3.4 \text{ meV}$

$$\Delta(E_1 + \Delta_1) = -\frac{\Delta_1}{2} + \Delta E_H + \sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2} = -3.4 \text{ meV}$$

# Calculating strain from observed oscillations (Ge 800 nm pump)

	$\Delta(E_1)$	$\Delta(E_1 + \Delta_1)$
$E_a$ (meV)	$4.2 \pm 0.4$	$4.7 \pm 0.8$
$E_b$ (meV)	$8.7 \pm 0.3$	$23.3 \pm 0.5$
$T$ (ps)	$11.0 \pm 0.2$	$11.4 \pm 0.4$
$\delta$	$2.58 \pm 0.06$	$2.6 \pm 0.1$
$\tau_a$ (ps)	$20 \pm 4$	$18 \pm 7$
$\tau_b$ (ps)	$23 \pm 2$	$42 \pm 3$

- Adding energy shifts (data):

$$\Delta E_1 + \Delta(E_1 + \Delta_1) = 2\Delta E_H \approx 9 \text{ meV}$$

$$\Rightarrow \Delta E_H \approx 4.5 \text{ meV}$$

$$\Rightarrow \epsilon_H = \frac{\Delta E_H}{\sqrt{3}D_1^1} \approx -3.3 \times 10^{-4}$$

$$\Rightarrow \epsilon_{\perp} = 3\epsilon_H \approx -1 \times 10^{-3}$$

- Subtracting energy shifts (data):

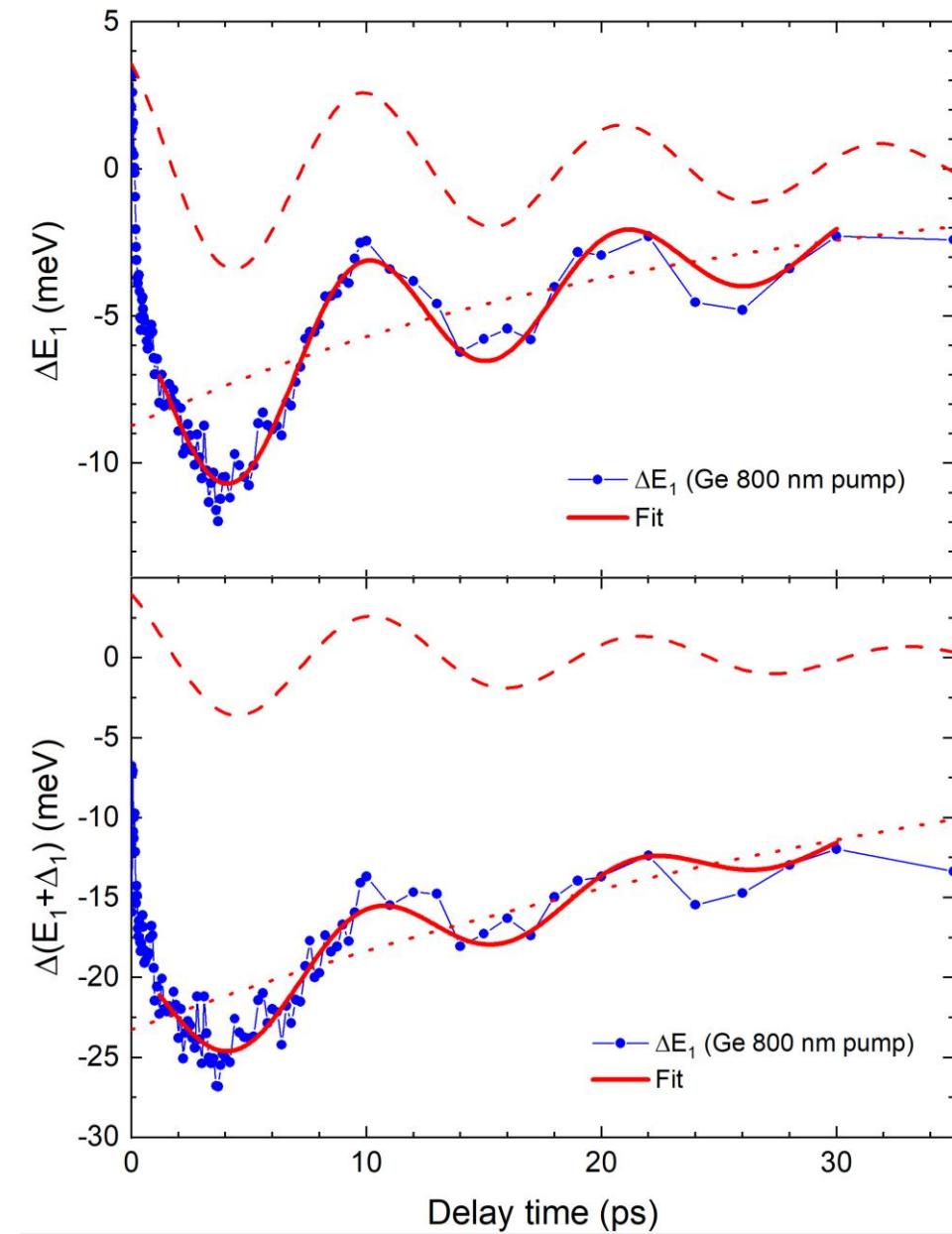
$$|\Delta E_1^S - \Delta(E_1 + \Delta_1)^S| = \left| \Delta_1 - 2\sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2} \right| \approx 0.5 \text{ meV}$$

$$\Rightarrow |\Delta E_S| \approx 7.0 \text{ meV}$$

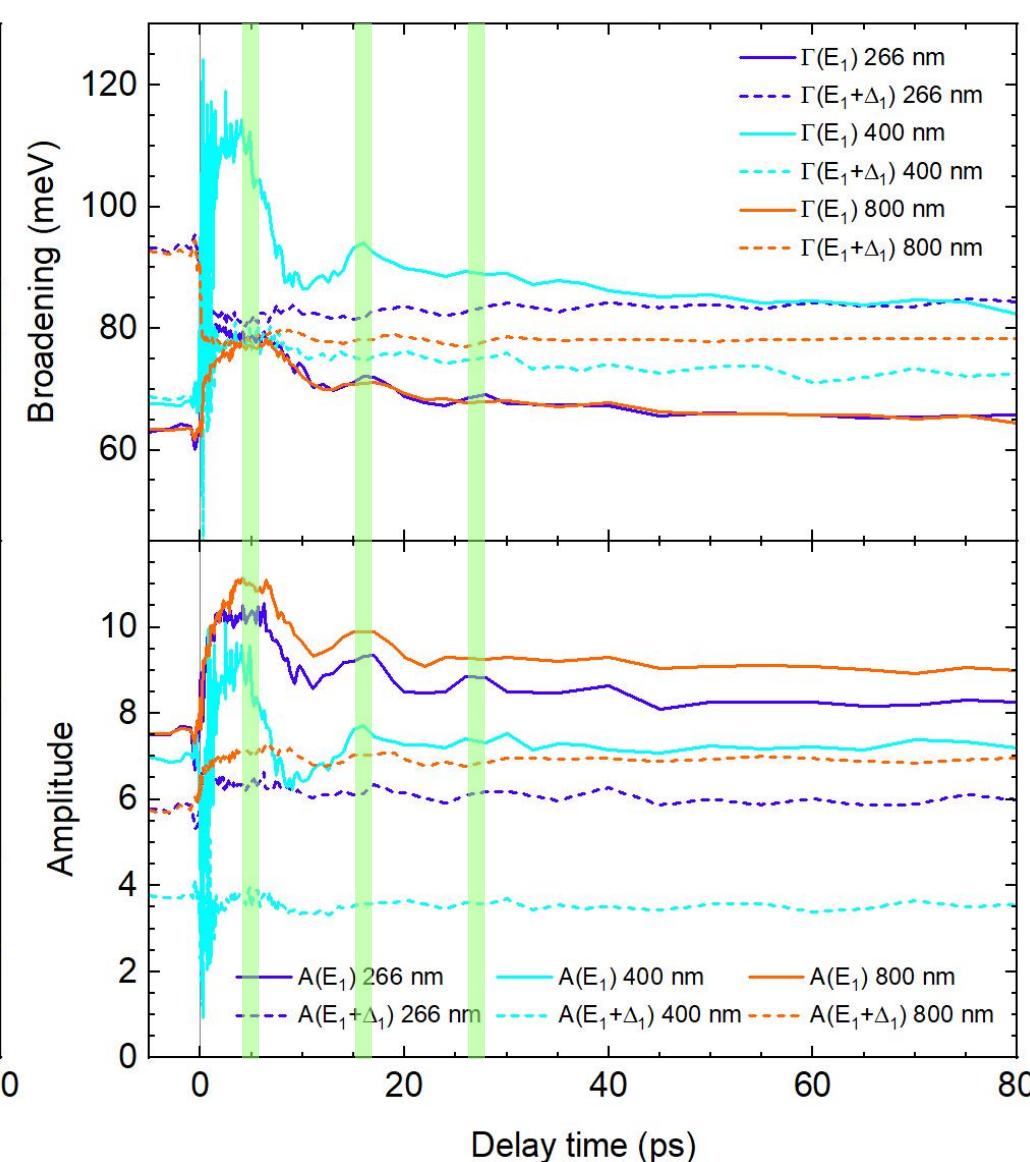
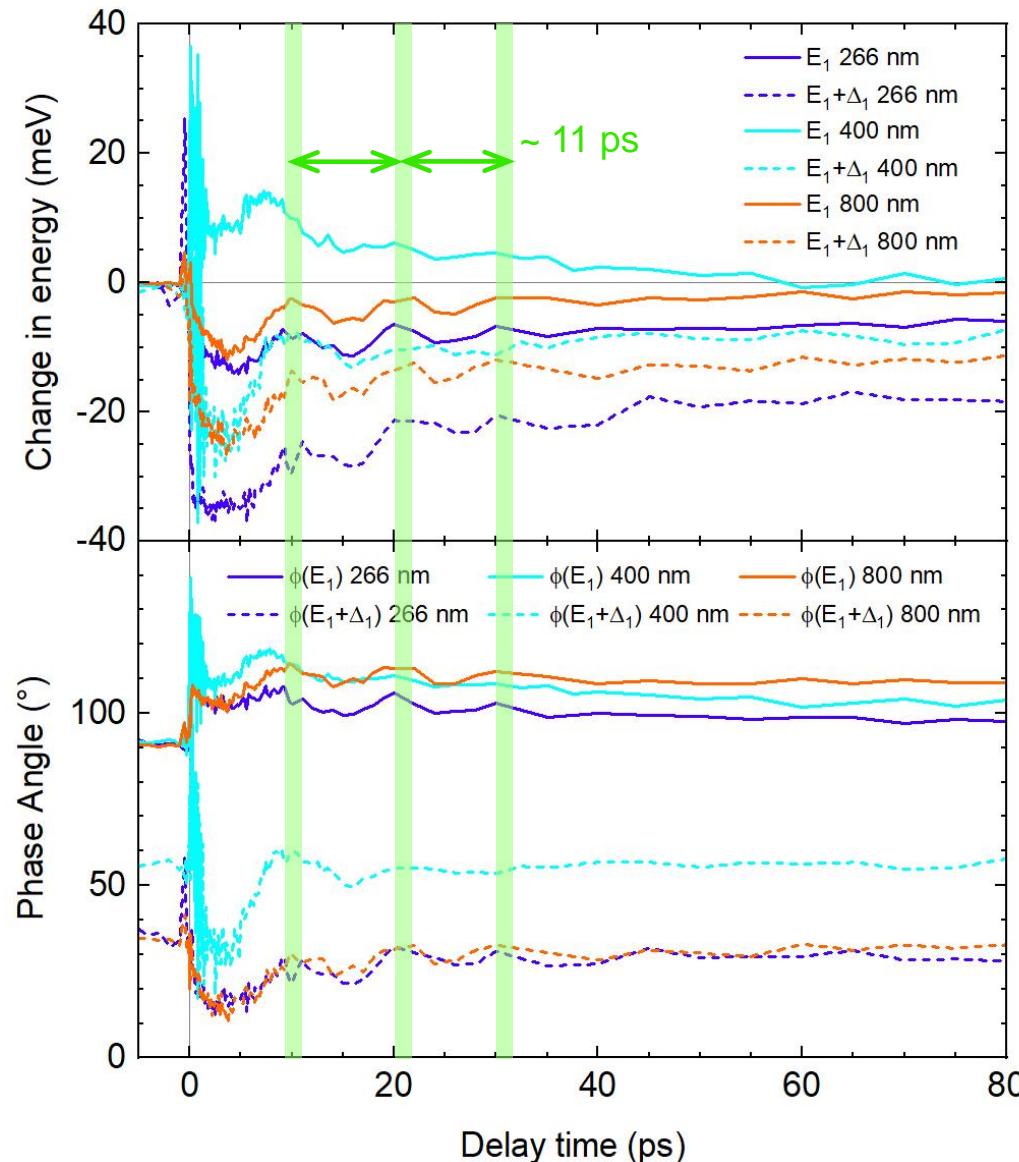
$$\Rightarrow |\epsilon_S| = \frac{|\Delta E_S|}{\sqrt{6}D_3^3} \approx 1.1 \times 10^{-3}$$

$$\Rightarrow \epsilon_{\perp} = 3\epsilon_S \approx -3.3 \times 10^{-3}$$

Compares well with calculated strain:  
 $\epsilon_{33} = -7.6 \times 10^{-4}$

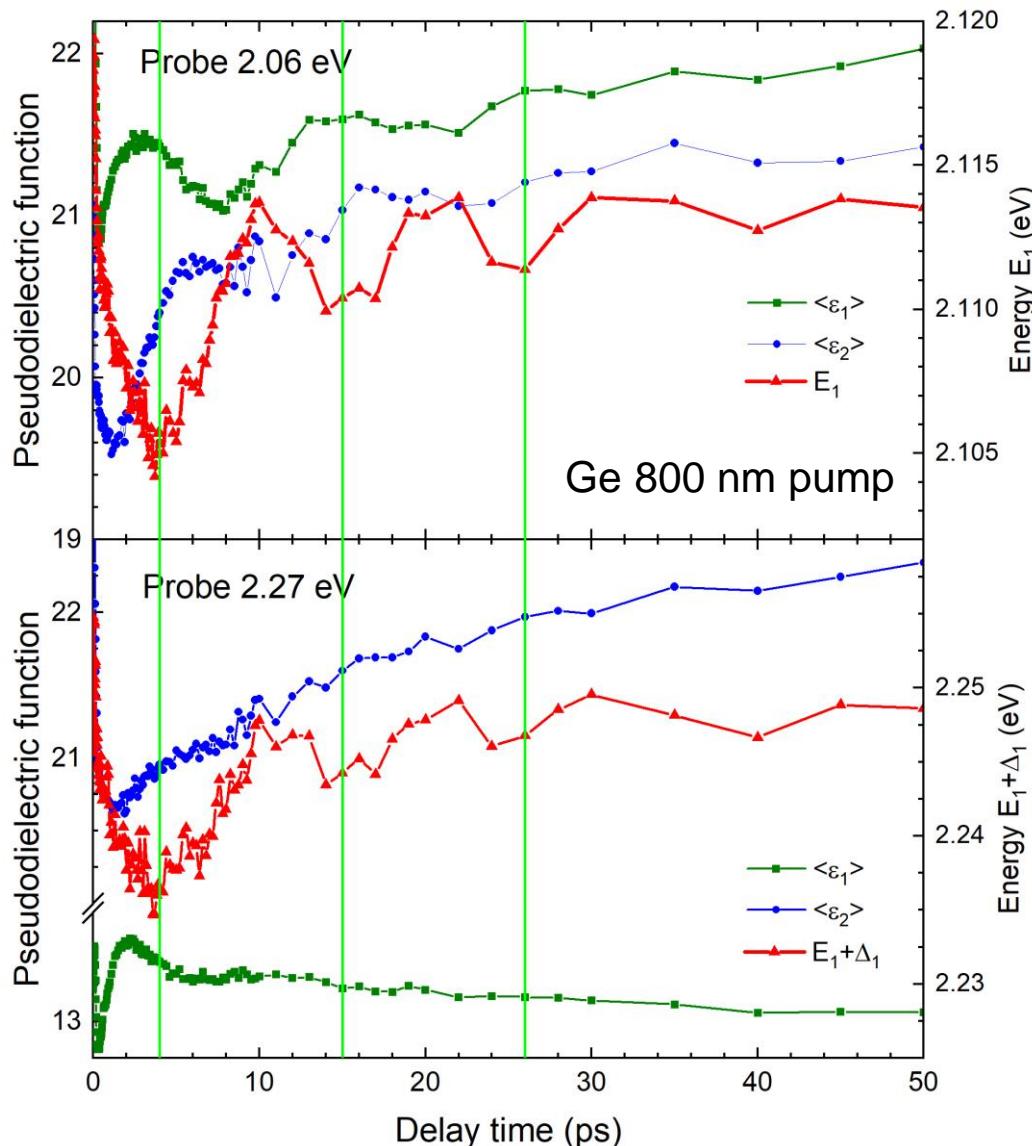


# Critical point parameters of Ge (266, 400, and 800 nm pump)



=> Oscillations present in all Ge data sets (266, 400, and 800 nm pump)

# Coherent longitudinal acoustic phonon oscillations



Oscillations in the CP parameters more pronounced than in the dielectric function

## Ge

$$E_1$$

$$\lambda = 585 \text{ nm}$$

$$n = 5.65$$

$$v_s = 4.87 \times 10^5 \text{ cm/s}$$

$$T = \frac{\lambda}{2v_s n} \approx 11 \text{ ps}$$

## Si

$$E_1$$

$$\lambda = 365 \text{ nm}$$

$$n = 6.52$$

$$v_s = 8.43 \times 10^5 \text{ cm/s}$$

$$T = \frac{\lambda}{2v_s n} \approx 3.3 \text{ ps}$$

## GaSb

$$E_1$$

$$\lambda = 620 \text{ nm}$$

$$n = 5.24$$

$$v_s = 4 \times 10^5 \text{ cm/s}$$

$$T = \frac{\lambda}{2v_s n} \approx 15 \text{ ps}$$

## InP

$$E_1 + \Delta_1$$

$$\lambda = 550 \text{ nm}$$

$$n = 5.16$$

$$v_s = 4.87 \times 10^5 \text{ cm/s}$$

$$T = \frac{\lambda}{2v_s n} \approx 11 \text{ ps}$$

$$E_1$$

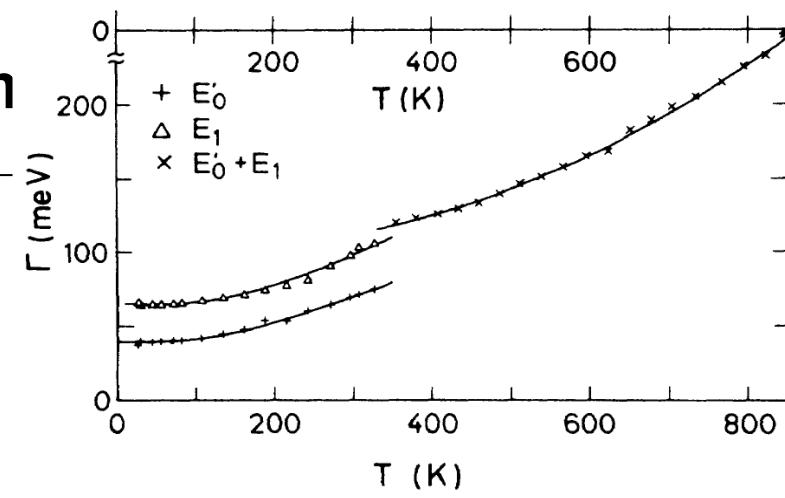
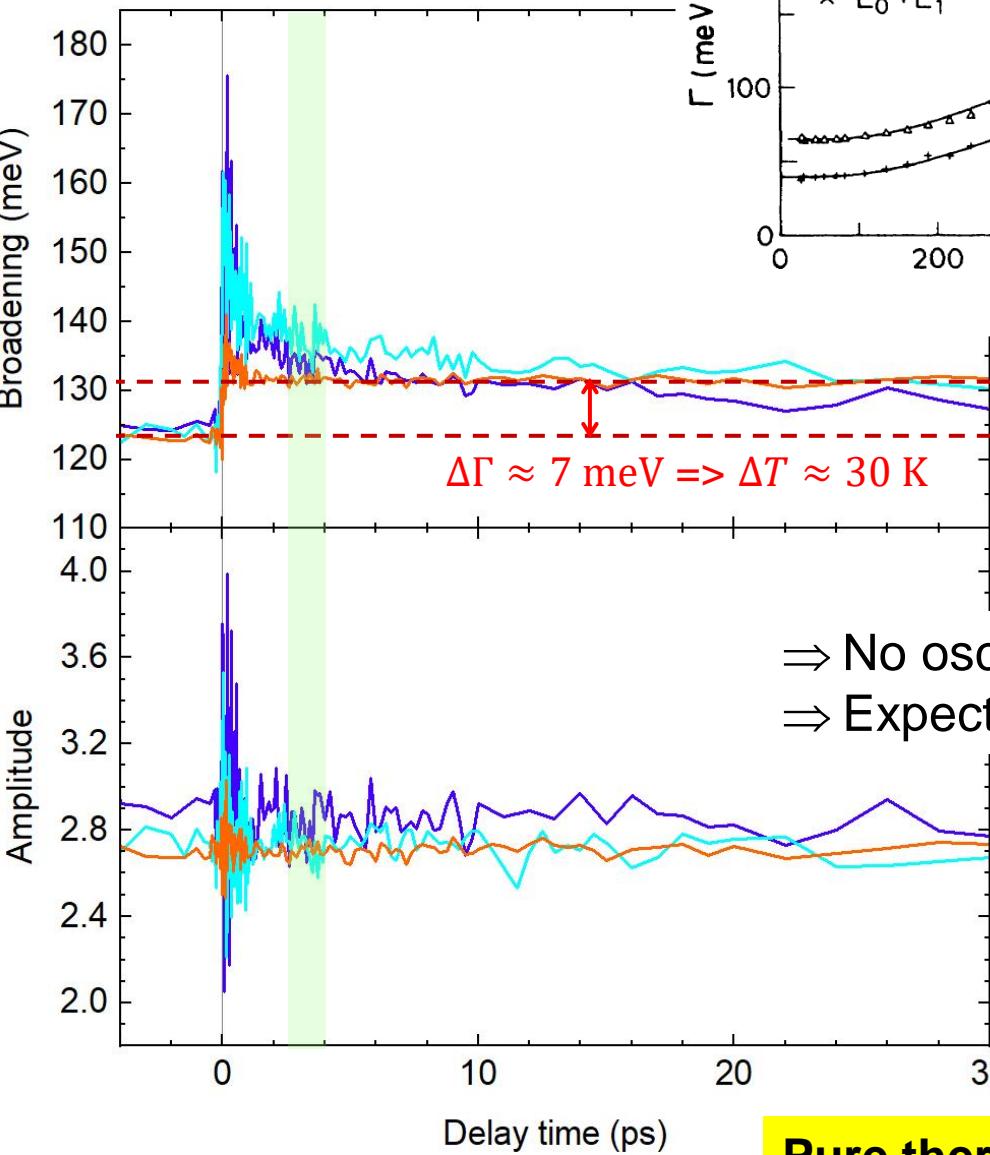
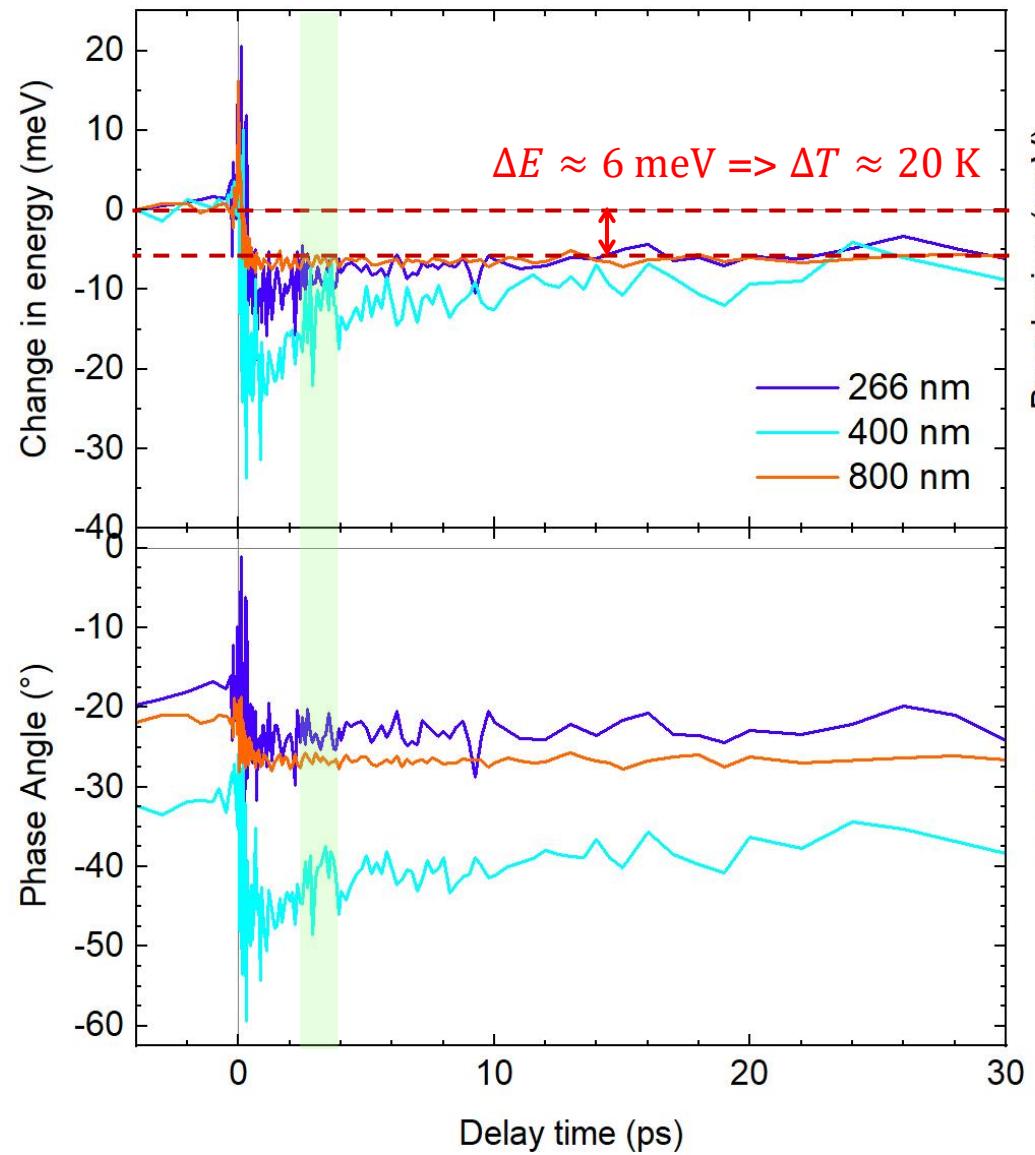
$$\lambda = 390 \text{ nm}$$

$$n = 3.98$$

$$v_s = 4.58 \times 10^5 \text{ cm/s}$$

$$T = \frac{\lambda}{2v_s n} \approx 11 \text{ ps}$$

# Critical point parameters of Si (266, 400, and 800 nm pun

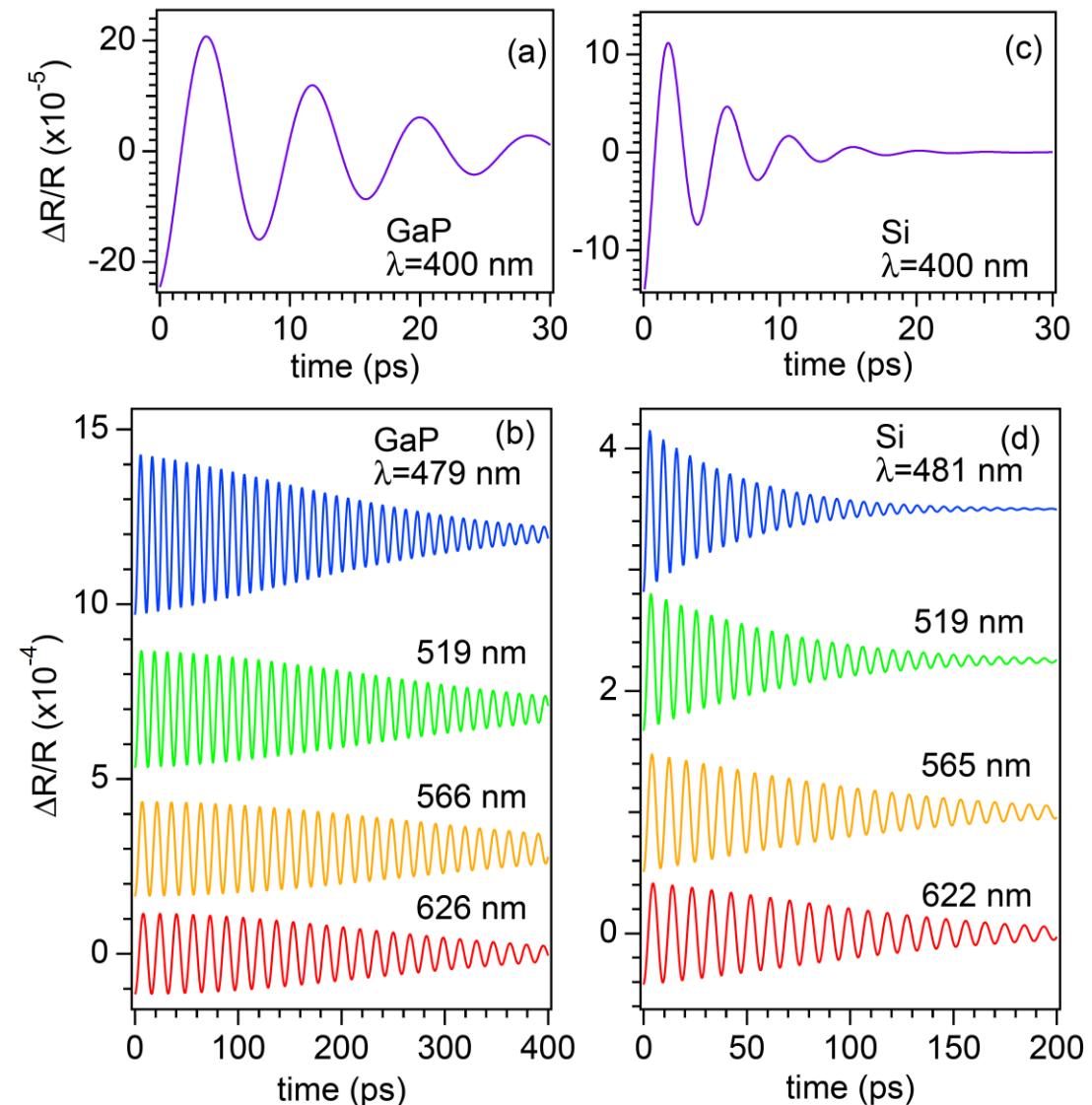
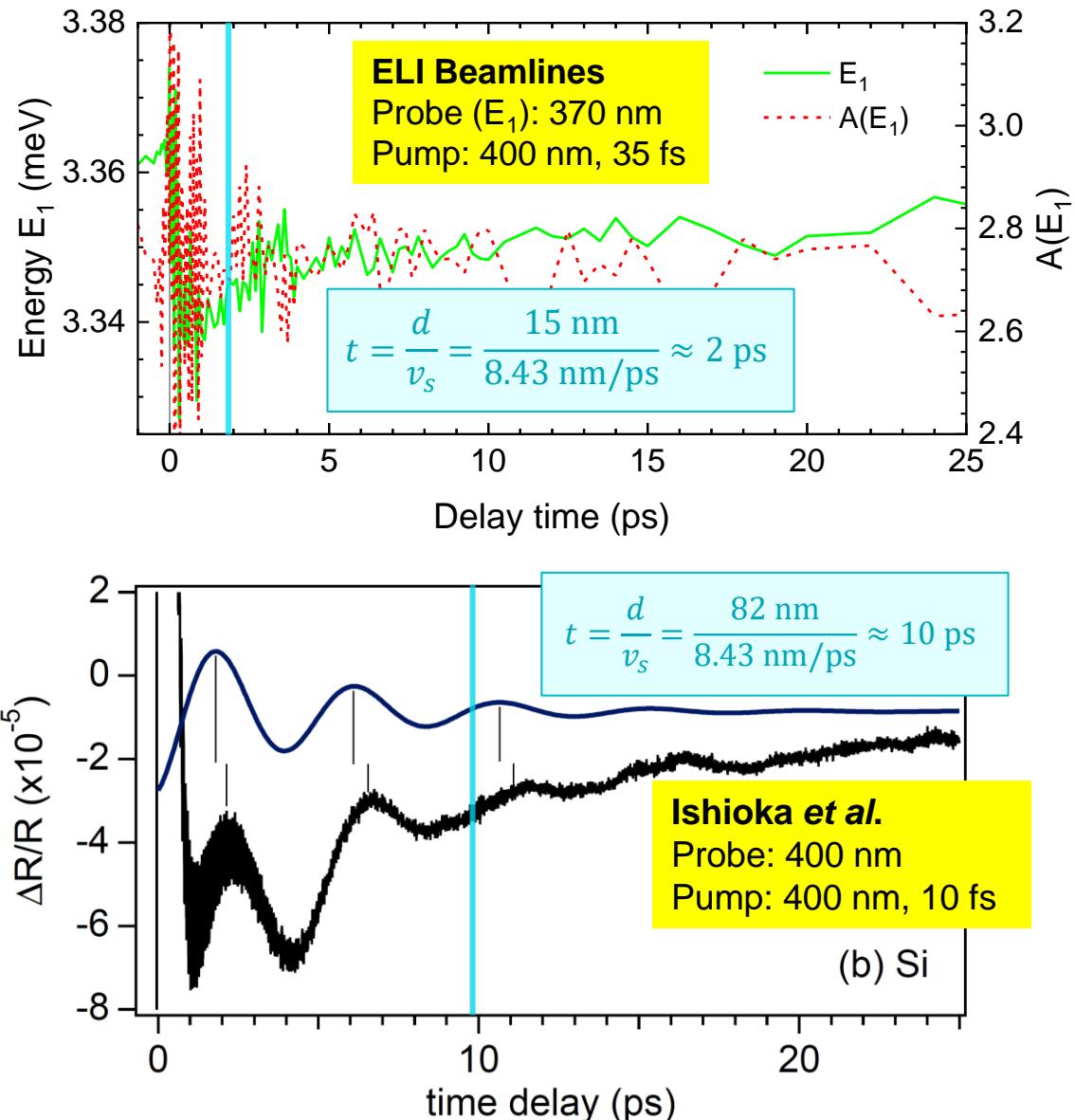


⇒ No oscillations detected  
⇒ Expected period:

$$T = \frac{\lambda}{2\nu_s n} \approx 3 \text{ ps}$$

Pure thermal effect

# Coherent longitudinal acoustic phonon oscillations in Si



# SUMMARY & OUTLOOK

## Part 1: Excitonic effects at the direct band gap $E_0$ of Ge

- **Temperature dependence of  $E_0$  obtained from spectroscopic ellipsometry**
  - Good agreement between model and data despite having only two fit parameters (energy and broadening).
- **Outlook & future work**
  - Application to other semiconductors
  - Consider non-parabolicity and warping

## Part 2: Analysis of femtosecond pump-probe ellipsometry data

- **Temporal evolution of  $E_1$  and  $E_1+\Delta_1$  in Ge**
  - Oscillations in CP parameters due to coherent longitudinal acoustic phonons.
- **Temporal evolution of CP parameters in Si**
  - No phonon oscillations detected.
- **Outlook & future work**
  - Taking new data with time steps targeted to resolve phonon oscillations.
  - Investigating bandfilling effects.

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FA9550-20-1-0135

M U N I

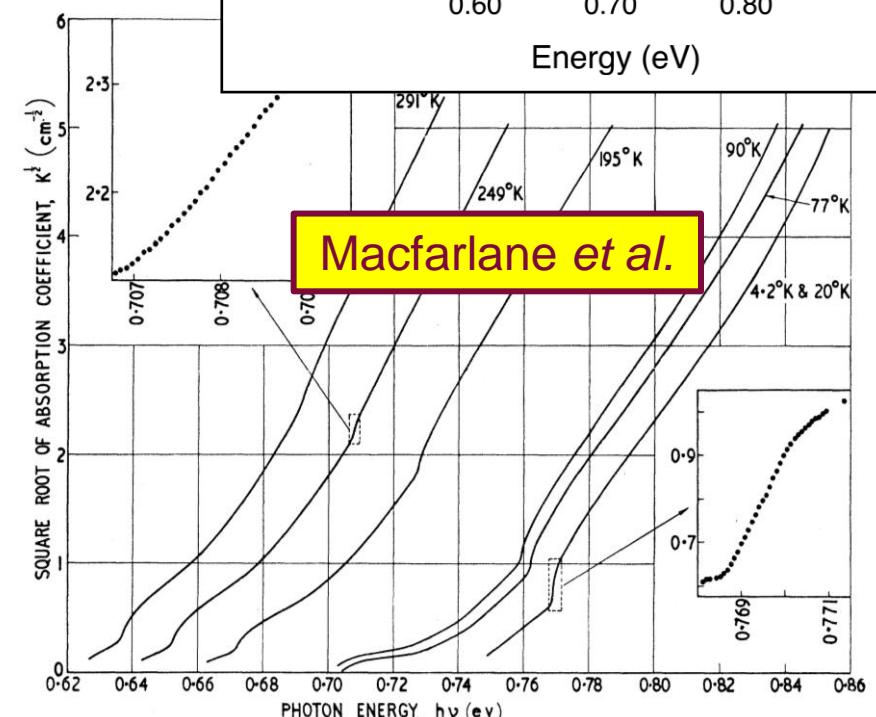
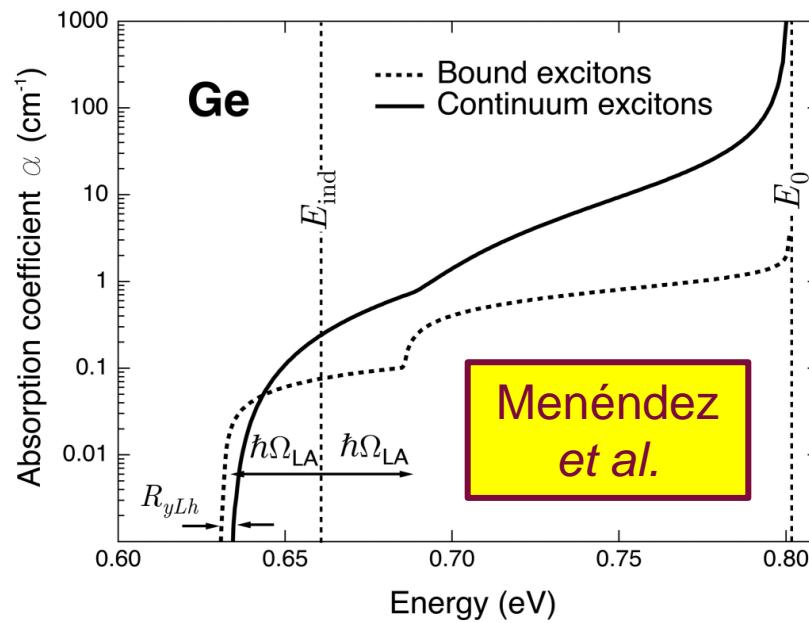
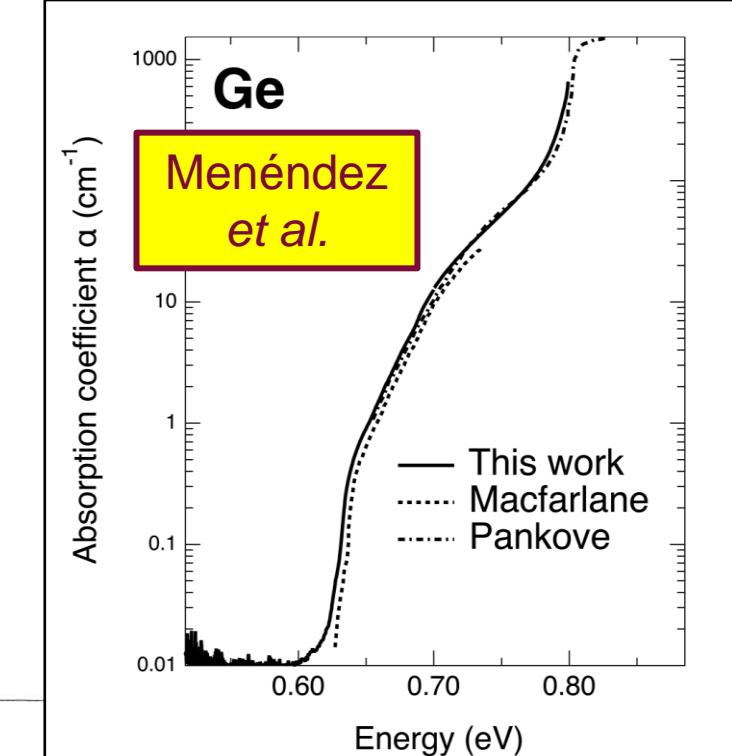
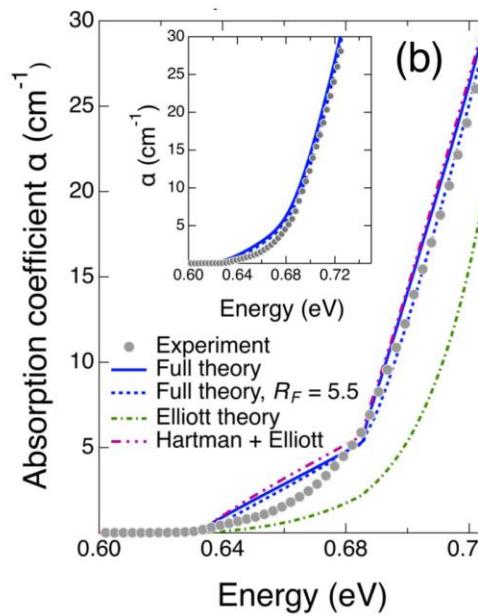
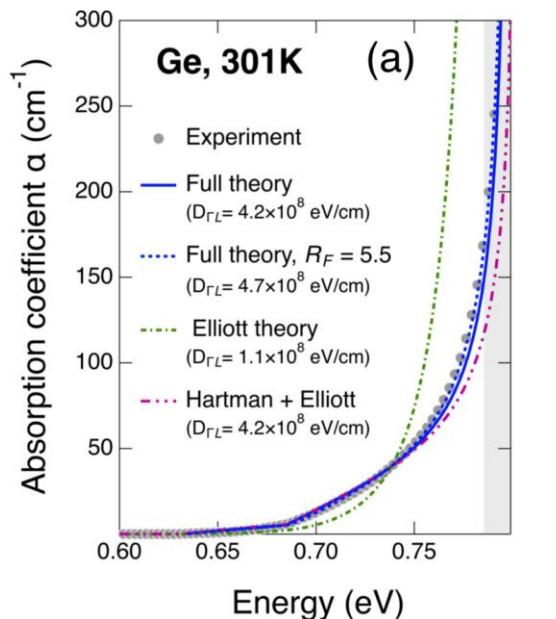
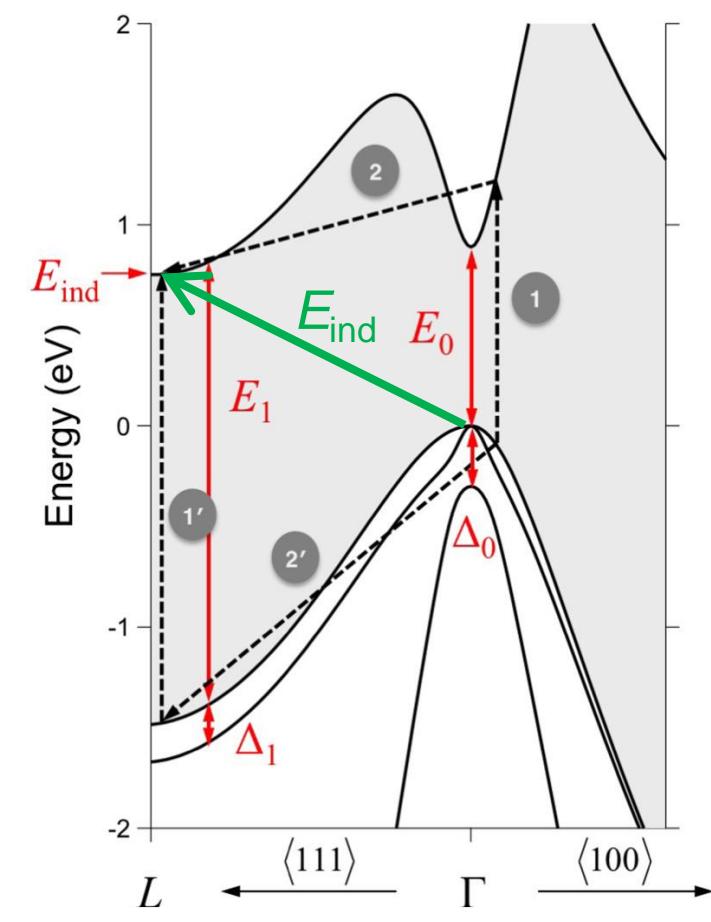


2017 AVS 64<sup>th</sup> International Symposium and Exhibition  
Left to right: Cesy Zamarripa, Rigo Carrasco, Carola Emminger, Prof. John Woollam, Dr. Stefan Zollner, Farzin Abadizaman, Nuwanjula Samarasingha and Pablo Paradis



# **Backup slides**

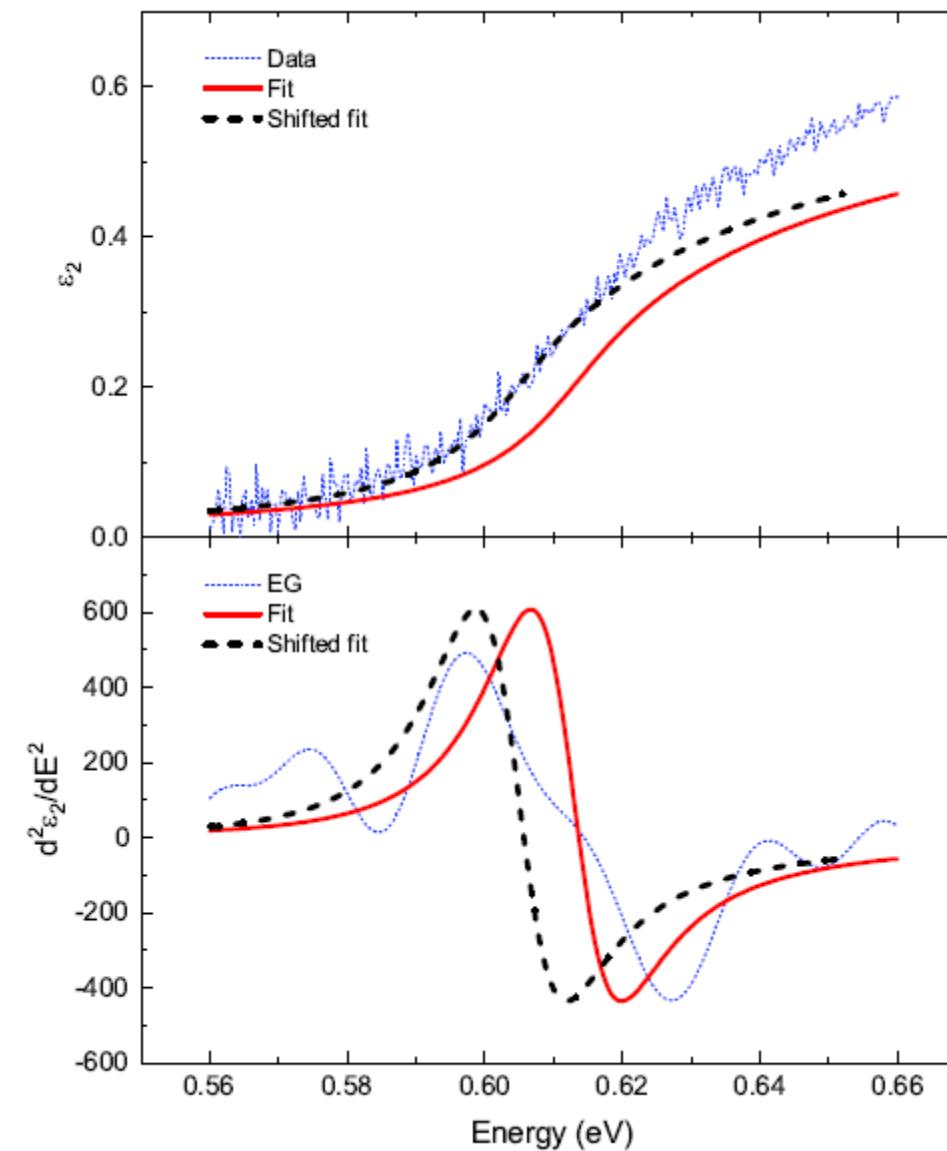
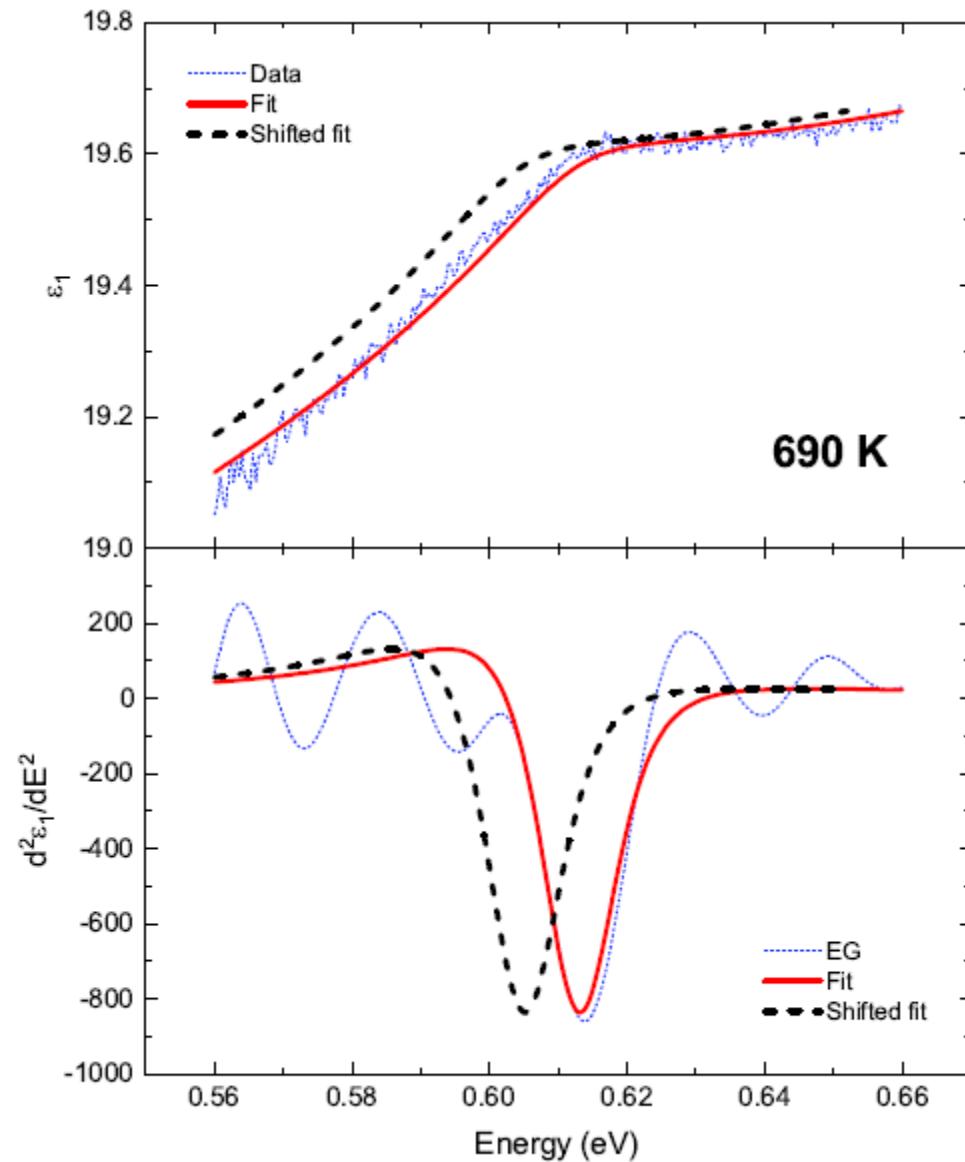
# Indirect and direct band gap of Ge



J. Menéndez, D.J. Lockwood, J.C. Zwinkels, and M. Noël, Phys. Rev. B **98**, 165207 (2018).

J. Menéndez, D.C. Poweleit, and S.E. Tilton, Phys. Rev. B **101**, 195204 (2020).

G.G. Macfarlane, T.P. McLean, J.E. Quarrington, and V. Roberts, Phys. Rev. **108**, 1377 (1957).



# Broadening theory

$$\eta_c(\epsilon) = \eta_c^+(\epsilon) + \eta_c^-(\epsilon)$$

$$\eta_c^\pm(\epsilon)$$

$$= \frac{2}{\sqrt{2}\pi\rho} \left( \frac{D_{\text{LA}}^2}{\hbar^2\Omega_{\text{LA}}} \right) m_\perp \sqrt{m_\parallel} \left( n_{\text{LA}} + \frac{1}{2} \pm \frac{1}{2} \right) \sqrt{E_0 + \epsilon - E_{\text{ind}} \mp \hbar\Omega_{\text{LA}}}$$

$$+ \frac{2\sqrt{2}}{3\pi\rho} \left( \frac{d'_{\text{LO}}^2}{\hbar^4\Omega_{\text{LO}}} \right) m_\perp m_\parallel^{\frac{3}{2}} \left( n_{\text{LO}} + \frac{1}{2} \pm \frac{1}{2} \right) (E_0 + \epsilon - E_{\text{ind}} \mp \hbar\Omega_{\text{LO}})^{3/2}$$

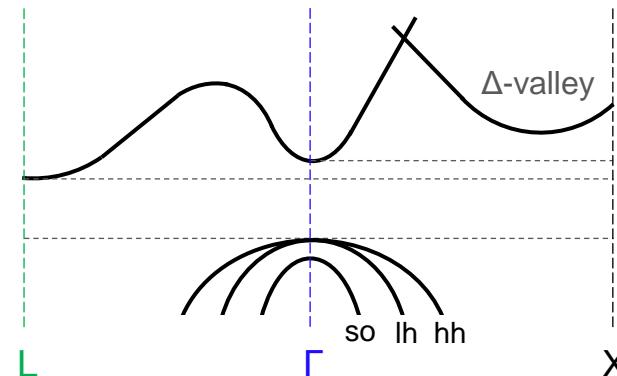
$$+ \frac{4\sqrt{2}}{3\pi\rho} \left( \frac{d'_{\text{TA}}^2}{\hbar^4\Omega_{\text{TA}}} \right) m_\perp m_\parallel^{\frac{3}{2}} \left( n_{\text{TA}} + \frac{1}{2} \pm \frac{1}{2} \right) (E_0 + \epsilon - E_{\text{ind}} \mp \hbar\Omega_{\text{TA}})^{3/2}$$

$$+ \frac{2\sqrt{2}}{\pi\rho} \left( \frac{d'_{\text{TA}}^2}{\hbar^4\Omega_{\text{TA}}} \right) m_c m_\perp \sqrt{m_\parallel} \left( n_{\text{TA}} + \frac{1}{2} \pm \frac{1}{2} \right) \epsilon \sqrt{E_0 + \epsilon - E_{\text{ind}} \mp \hbar\Omega_{\text{TA}}}$$

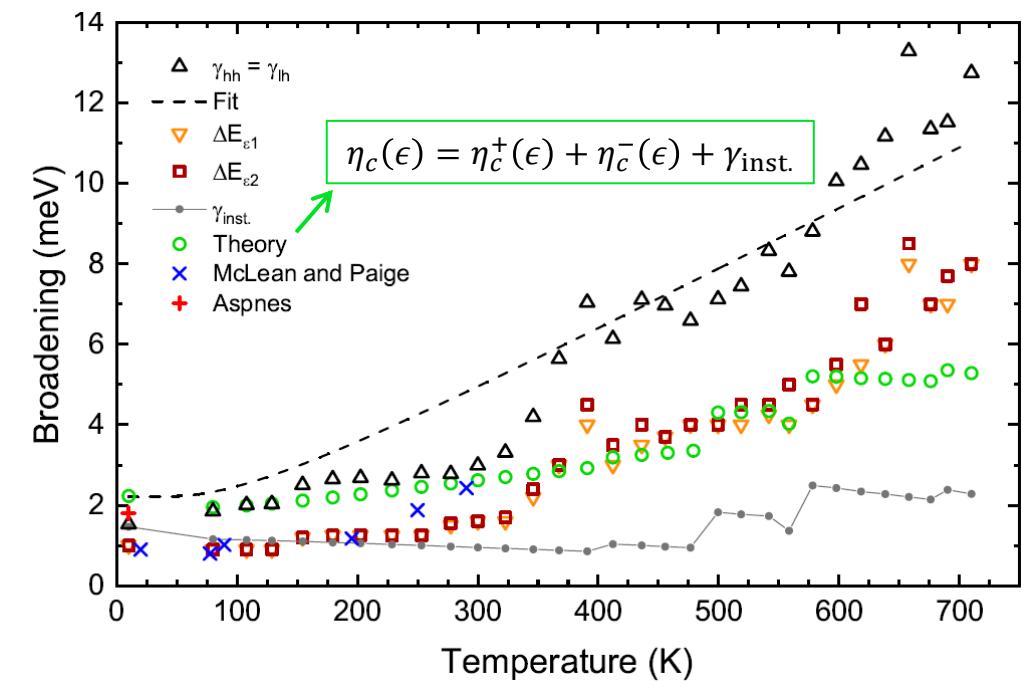
$$+ \frac{2}{\sqrt{2}\pi\rho} \left( \frac{D_{\Delta\Gamma}^2}{\hbar^2\Omega_\Delta} \right) m_\Delta^{\frac{3}{2}} \left( n_\Delta + \frac{1}{2} \pm \frac{1}{2} \right) \sqrt{E_0 + \epsilon - E_\Delta \mp \hbar\Omega_\Delta}$$

= 0, because conduction band minimum at  $\Gamma$  is below the  $\Delta$  minimum

Conwell's expression  
(LA-phonon intervalley scattering)

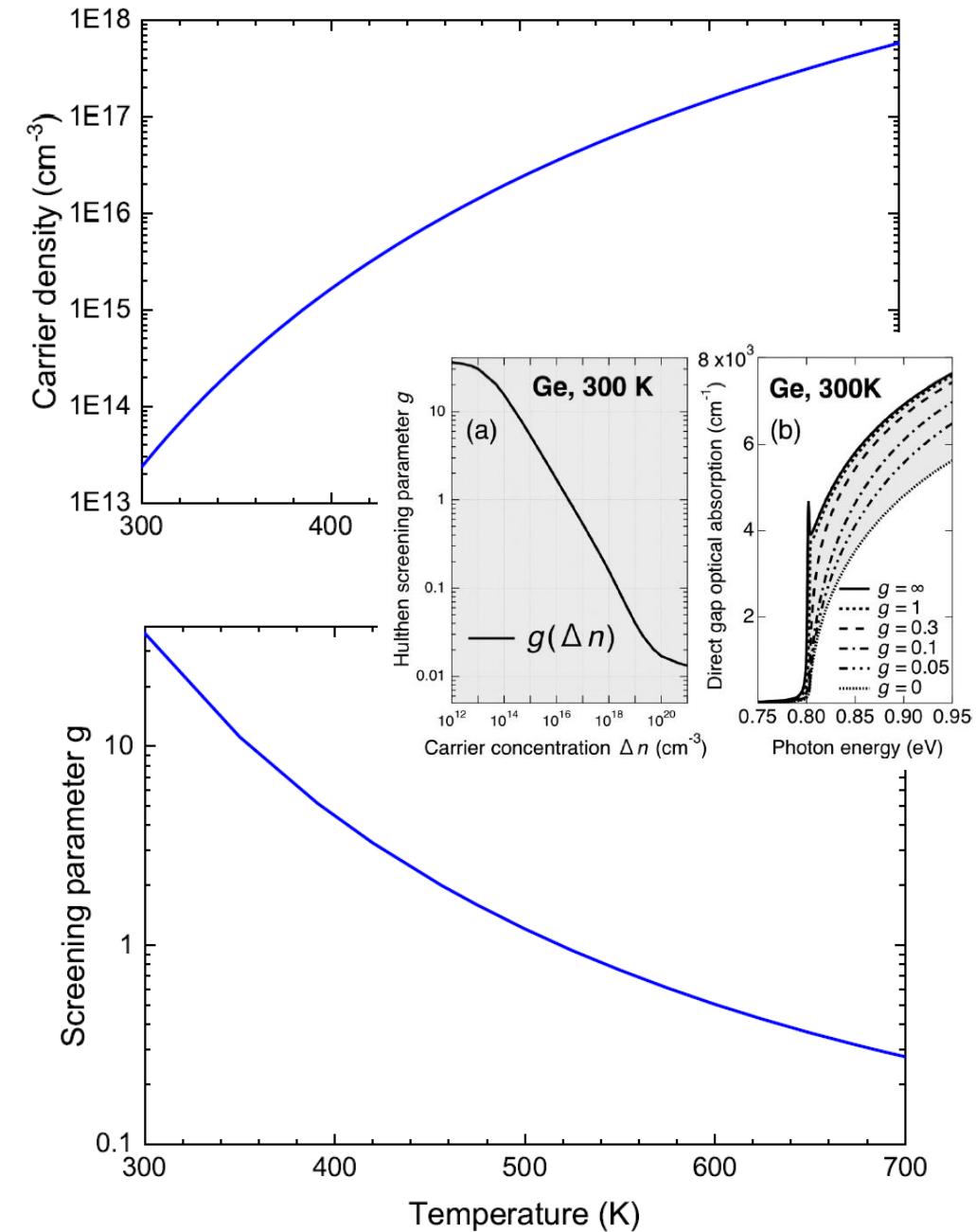
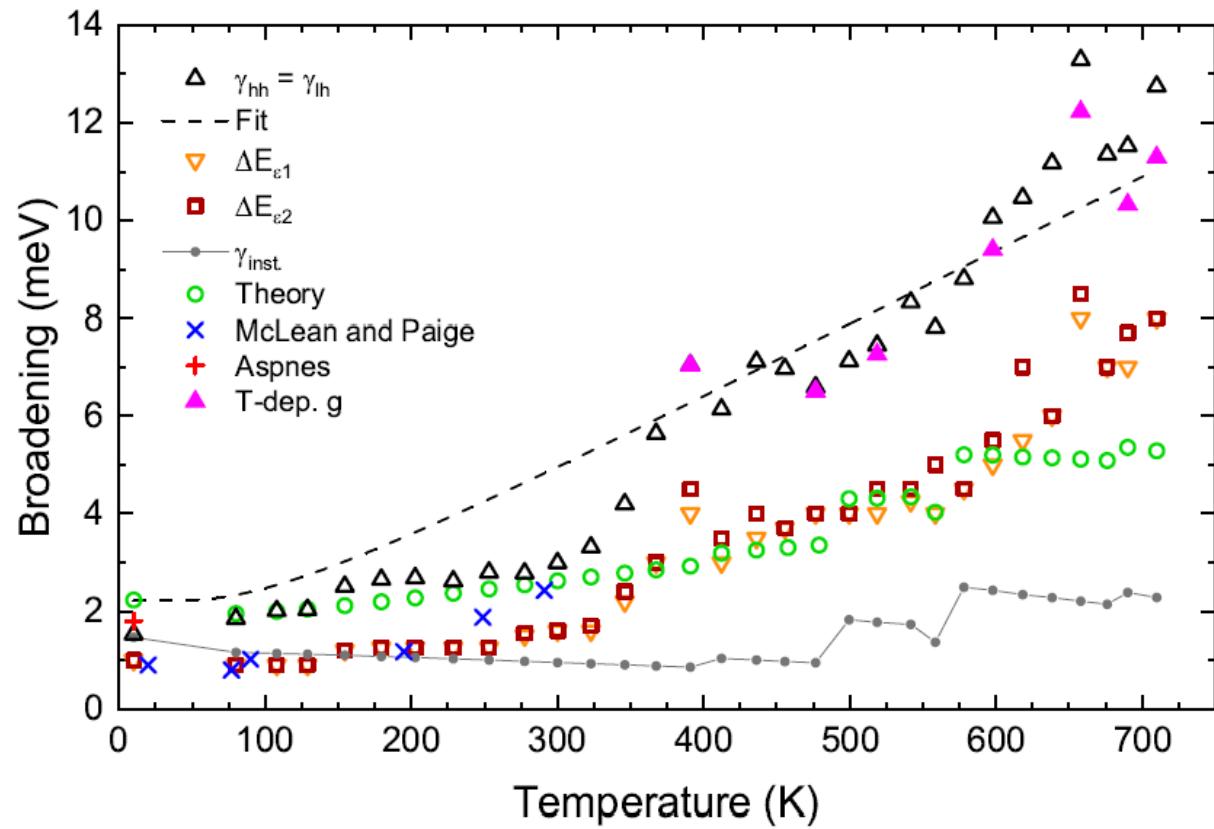


→ Forbidden LO scattering from “around L to  $\Gamma$ ”



# Screening

Considering the temperature dependence of the screening parameter affects the broadening at higher temperatures ( $\blacktriangle$ ):



$$A = 1 - 1/3 \left[ \frac{E_P}{E_0} + \frac{2E_Q}{E'_0} \right]$$

$$B = 1/3 \left[ -\frac{E_P}{E_0} + \frac{E_Q}{E'_0} \right]$$

$$C^2 = \frac{4E_P E_Q}{3E_0 E'_0} + \Delta$$

## DKK parameters and effective masses

M. Cardona, J. Phys. Chem. Solids **24**, 1543 (1963):

$$A = \frac{1}{3}(F + 2G + 2M) + 1$$

$$B = \frac{1}{3}(F + 2G - M)$$

$$C^2 = \frac{1}{3}[(F - G + M)^2 - (F + 2G - M)^2]$$

$$F(T) = -\frac{E_{P,4K} \left( \frac{a_{4K}}{a(T)} \right)}{E_0(T)}$$

$$M(T) = -\frac{E_{Q,4K} \left( \frac{a_{4K}}{a(T)} \right)}{E'_0(T)}$$

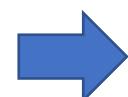
$$G(T) = -G_{4K} \left( \frac{a_{4K}}{a(T)} \right)$$

For A = -13.38, B = -8.48, and |C| = 13.14 at 4 K (also used in J. Menendez et al., Phys. Rev. B **98**, 165207 (2018)):

$$E_{P,4K} = 26.0 \text{ eV}$$

$$E_{Q,4K} = 18.5 \text{ eV}$$

$$G_{4K} = -1.04$$



$$m_{hh,4K} = 0.326 m_0$$

$$m_{lh,4K} = 0.0422 m_0$$

# Generation of strain pulse

Thomsen *et al.* (1986):  $\sigma_{33} = -B \frac{\partial E_g}{\partial P} N - \frac{3B\beta}{c} (E - E_g)N$

Wright *et al.* (2002):  $\sigma_{33} = -B \frac{\partial E_g}{\partial P} N - 3B\beta\Delta T$

$$\epsilon_{ij} = \sum_{kl} S_{ijkl} \sigma_{kl}$$

$$\hat{S} = \begin{pmatrix} S_{11} & S_{12} & S_{12} & 0 & 0 & 0 \\ S_{21} & S_{11} & S_{12} & 0 & 0 & 0 \\ S_{21} & S_{21} & S_{11} & 0 & 0 & 0 \\ 0 & 0 & 0 & S_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & S_{44} & 0 \\ 0 & 0 & 0 & 0 & 0 & S_{44} \end{pmatrix}$$

$$\epsilon_3 = S_{21}(\sigma_1 + \sigma_2) + S_{11}\sigma_3$$

$$\sigma_1 = \sigma_2 = \sigma_3 = \sigma$$

$$\epsilon_3 = (S_{11} + 2S_{12})\sigma$$

$$S_{11} + 2S_{12} = \frac{1}{C_{11} + 2C_{12}} = 0.444 \frac{\text{cm}^2}{\text{N}}$$

$$\epsilon_3 = \left( 4.44 \times 10^{-8} \frac{\text{cm}^2}{\text{N}} \right) \sigma.$$

# Calculating strain and energy shifts (Ge 800nm pump)

$$\frac{\partial E_g}{\partial P} = 5 \text{ eV} \text{ (indirect gap)}$$

Stress-strain relation:  $\epsilon_3 = (S_{11} + 2S_{12})\sigma = \frac{\sigma}{C_{11} + 2C_{12}}$  (assuming:  $\sigma_{ii} = \sigma$  for all  $i$  and  $\sigma_{ij} = 0$  for  $i \neq j$ )

$$(C_{11} + 2C_{12})^{-1} = 4.44 \times 10^{-8} \frac{\text{cm}^2}{\text{N}}$$

Electron contribution:  $\sigma_{\text{el}} = -B \frac{\partial E_g}{\partial P} N \Rightarrow \epsilon_{\text{el}} = (C_{11} + 2C_{12})^{-1} \sigma_{\text{el}} = -6.4 \times 10^{-4}$

Phonon contribution:  $\sigma_{\text{ph}} = -\frac{3B\beta}{c}(E - E_g)N \Rightarrow \epsilon_{\text{ph}} = (C_{11} + 2C_{12})^{-1} \sigma_{\text{ph}} = -1.2 \times 10^{-4}$

Total stress/strain:  $\sigma_{33} = \sigma_{\text{el}} + \sigma_{\text{ph}} \Rightarrow \epsilon_{33} = (C_{11} + 2C_{12})^{-1} \sigma_{33} = -7.6 \times 10^{-4}$

In-plane and out-of-plane strain:  $\epsilon_{\perp} = \epsilon_{33}$  and  $\epsilon_{\parallel} = 0$

Hydrostatic and shear strain:  $\epsilon_H = \epsilon_S = 2.5 \times 10^{-4}$

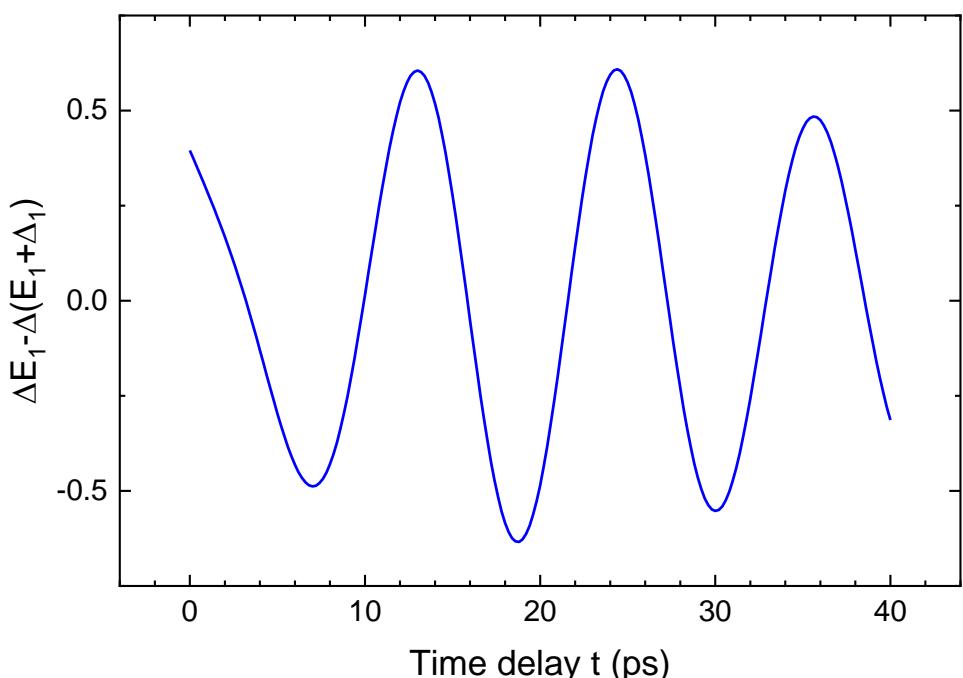
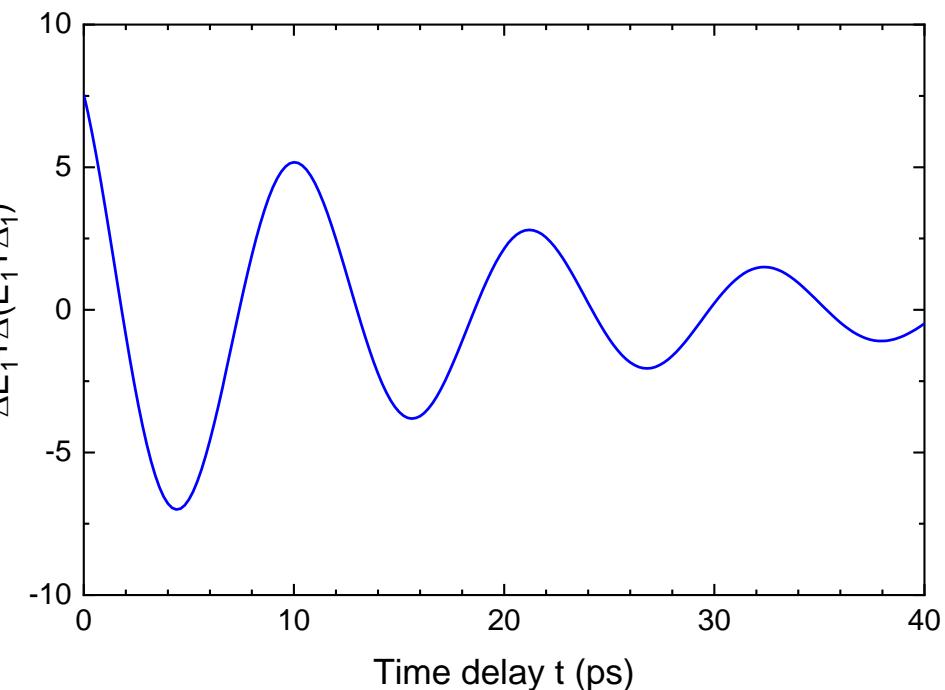
Hydrostatic shift:  $\Delta E_H = \sqrt{3}D_1^1 \epsilon_H = -3.4 \text{ meV}$

Shear splitting:  $\Delta E_S = \sqrt{6}D_3^3 \epsilon_S = 1.6 \text{ meV}$

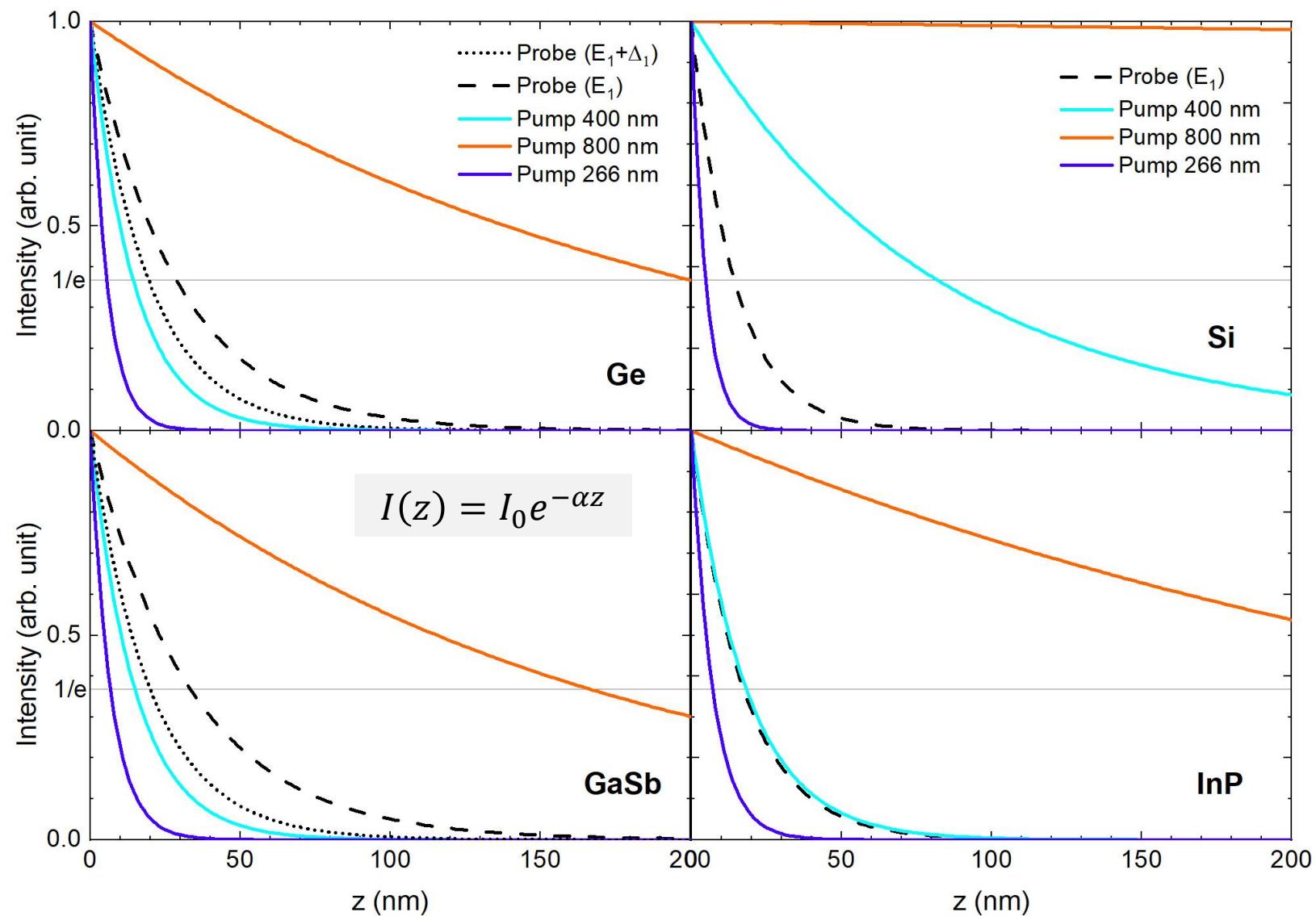
Critical point energy shift:  $\Delta E_1 = \frac{\Delta_1}{2} + \Delta E_H - \sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2} = -3.4 \text{ meV}$

$$\Delta(E_1 + \Delta_1) = -\frac{\Delta_1}{2} + \Delta E_H + \sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2} = -3.4 \text{ meV}$$

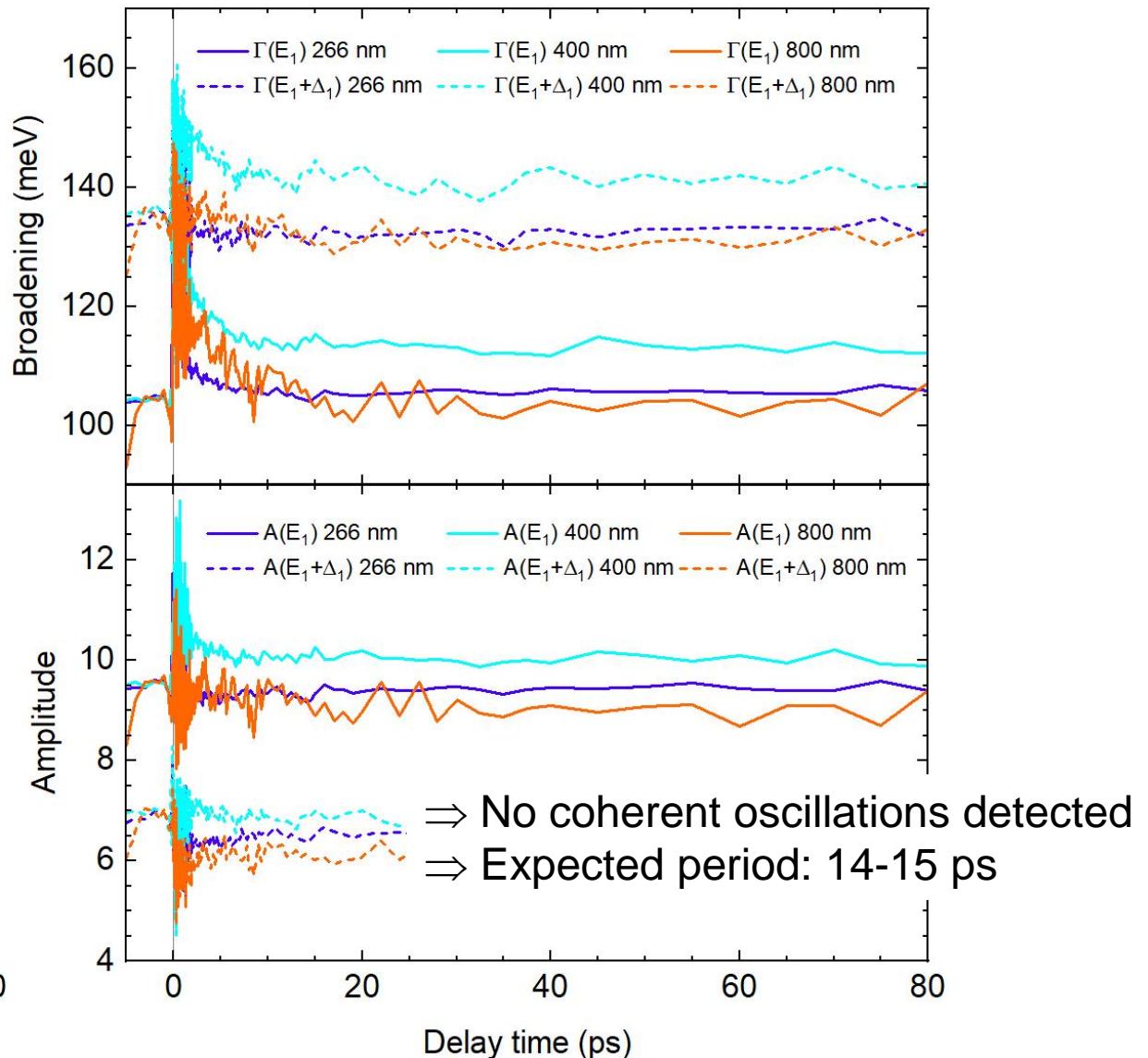
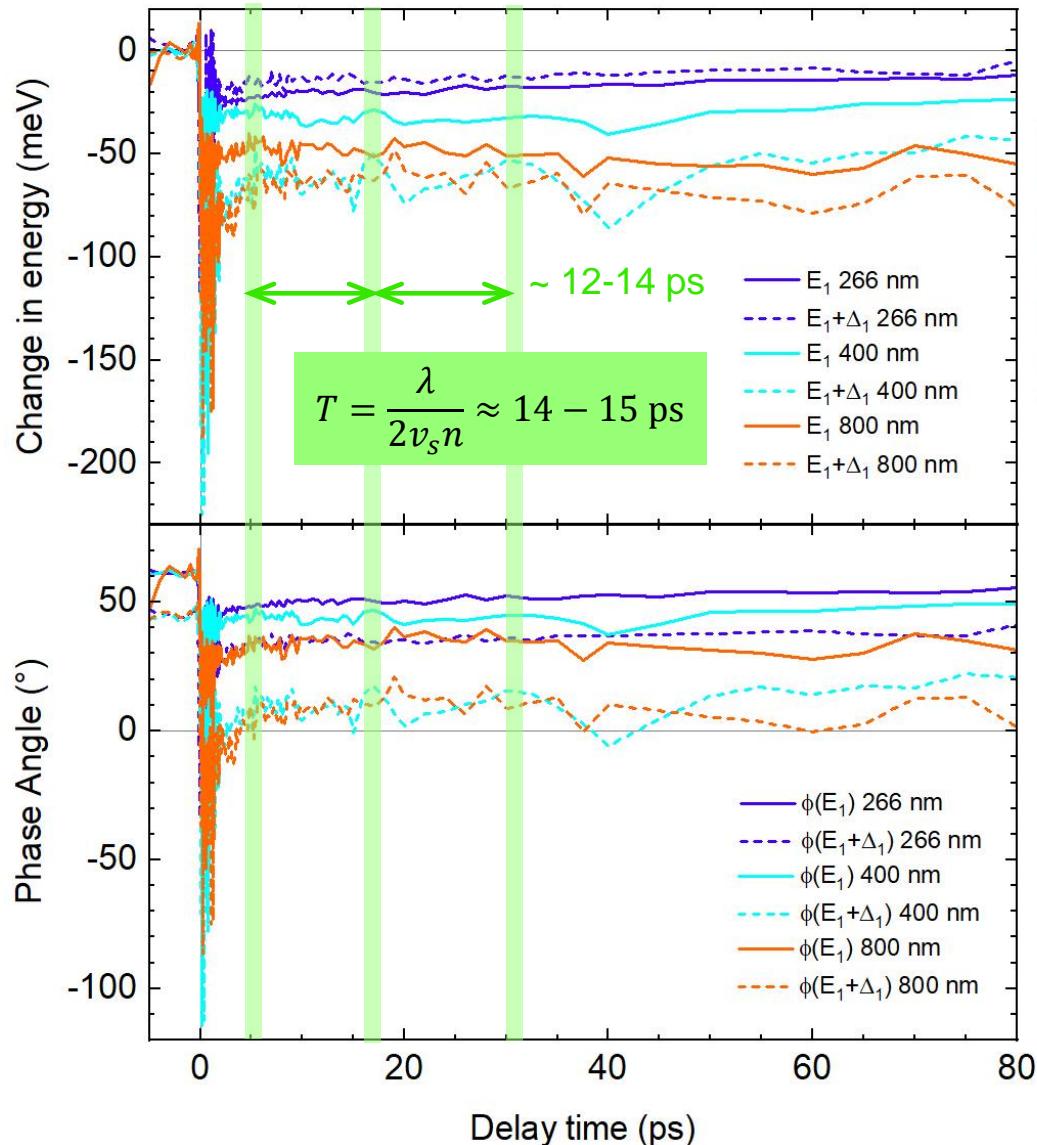
- Hydrostatic strain:  $\epsilon_H = \frac{\epsilon_{\perp} + 2\epsilon_{\parallel}}{3}$
- Shear strain:  $\epsilon_S = \frac{\epsilon_{\perp} - \epsilon_{\parallel}}{3}$
- Hydrostatic shift:  $\Delta E_H = \sqrt{3}D_1^1\epsilon_H$
- Shear splitting:  $\Delta E_S = \sqrt{6}D_3^3\epsilon_S$
- Shift:  $\Delta E_1 = E_1^s - E_1^0 = \frac{\Delta_1}{2} + \Delta E_H - \sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2}$   
 $\Delta(E_1 + \Delta_1) = (E_1 + \Delta_1)^s - (E_1^0 + \Delta_1) = -\frac{\Delta_1}{2} + \Delta E_H + \sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2}$
- **Adding energy shifts (data):**  
 $\Delta E_1 + \Delta(E_1 + \Delta_1) = 2\Delta E_H \approx 9 \text{ meV}$   
 $\Rightarrow \Delta E_H \approx 4.5 \text{ meV}$   
 $\Rightarrow \epsilon_H = \frac{\Delta E_H}{\sqrt{3}D_1^1} \approx -3.3 \times 10^{-4}$   
 $\Rightarrow \epsilon_{\perp} = 3\epsilon_H \approx -1 \times 10^{-3}$
- **Subtracting energy shifts (data):**  
 $|\Delta E_1^s - \Delta(E_1 + \Delta_1)^s| = \left| \Delta_1 - 2\sqrt{\frac{(\Delta_1)^2}{4} + (\Delta E_S)^2} \right| \approx 0.5 \text{ meV}$   
 $\Rightarrow |\Delta E_S| \approx 7.0 \text{ meV}$   
 $\Rightarrow |\epsilon_S| = \frac{|\Delta E_S|}{\sqrt{6}D_3^3} \approx 1.1 \times 10^{-3}$   
 $\Rightarrow |\epsilon_{\perp}| = 3|\epsilon_S| \approx 3.3 \times 10^{-3}$



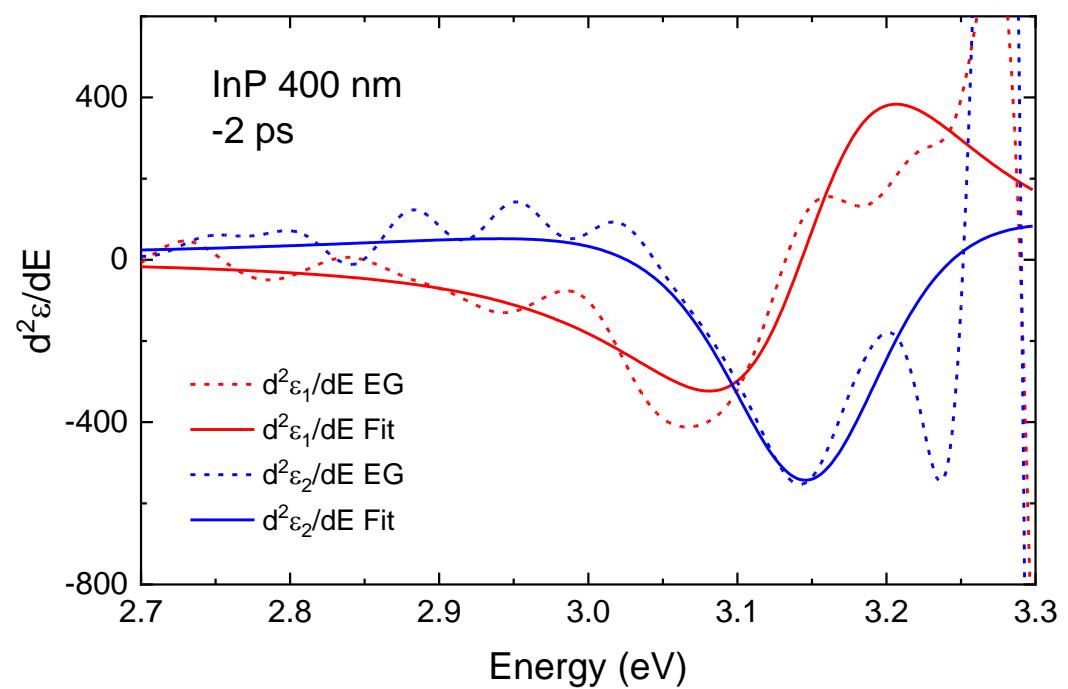
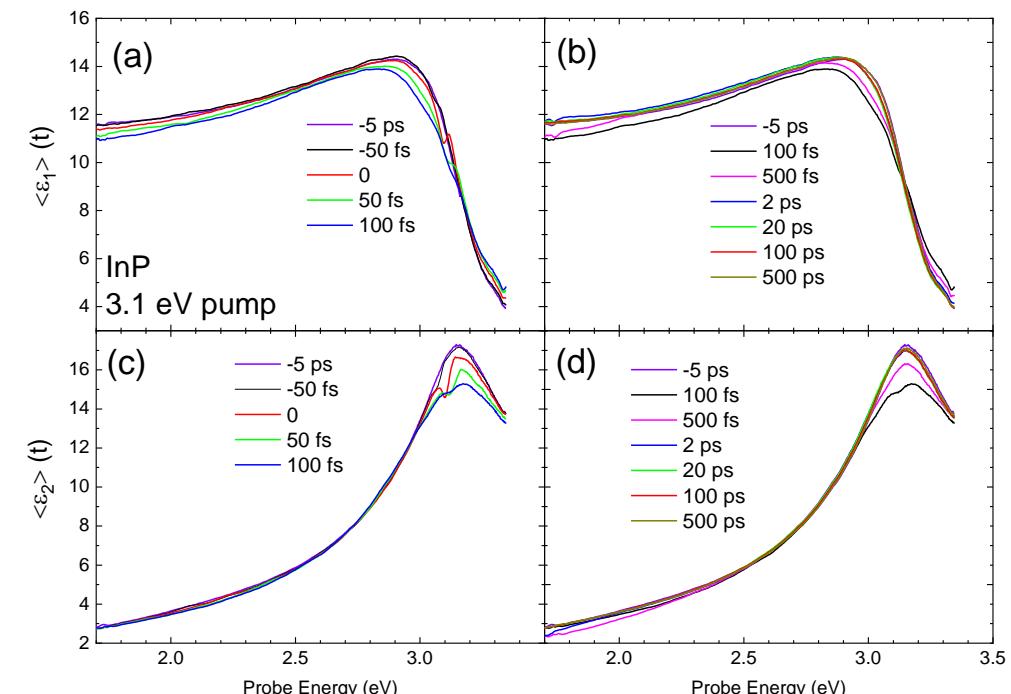
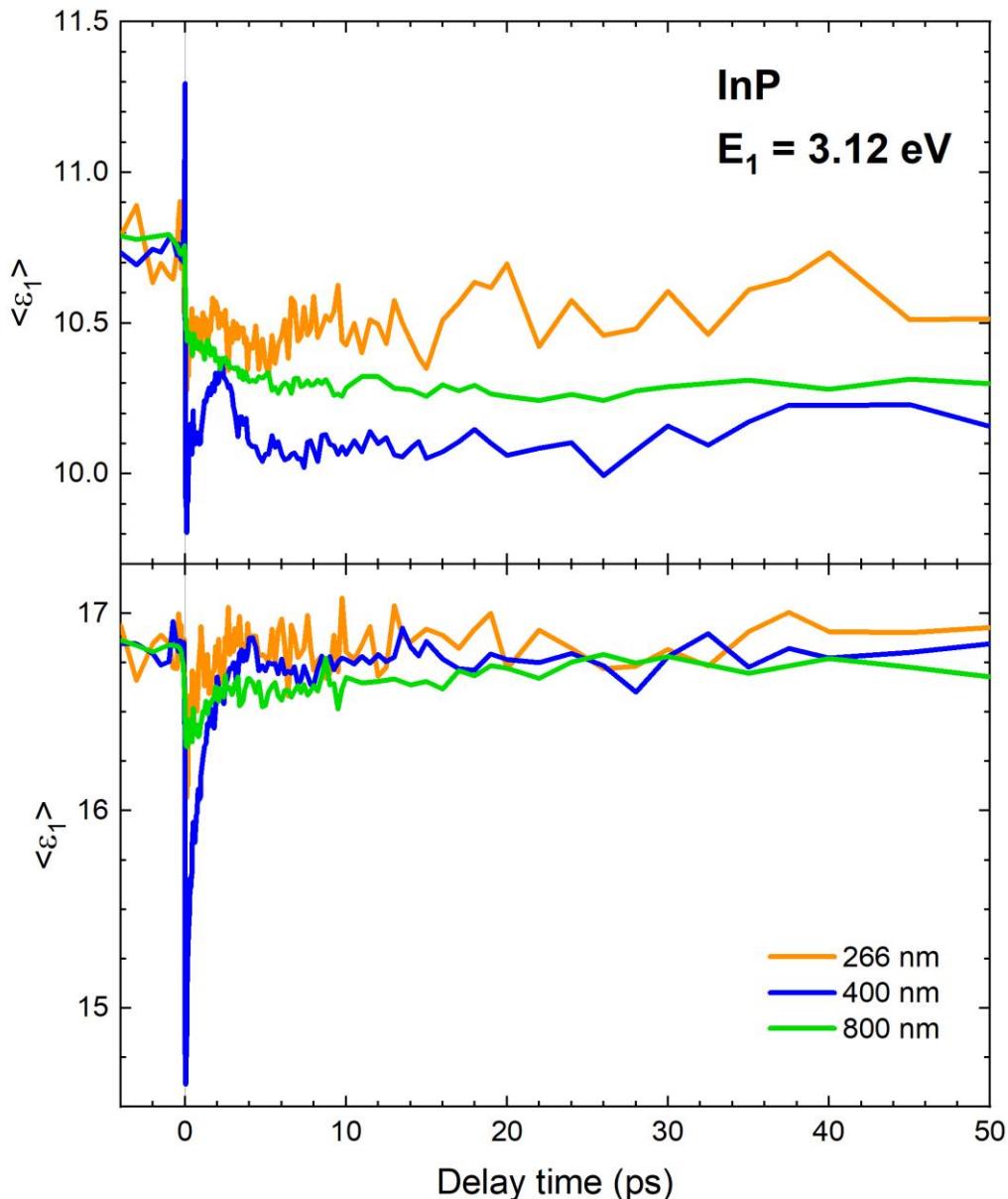
# Beer's law and penetration depth for different pump wavelengths



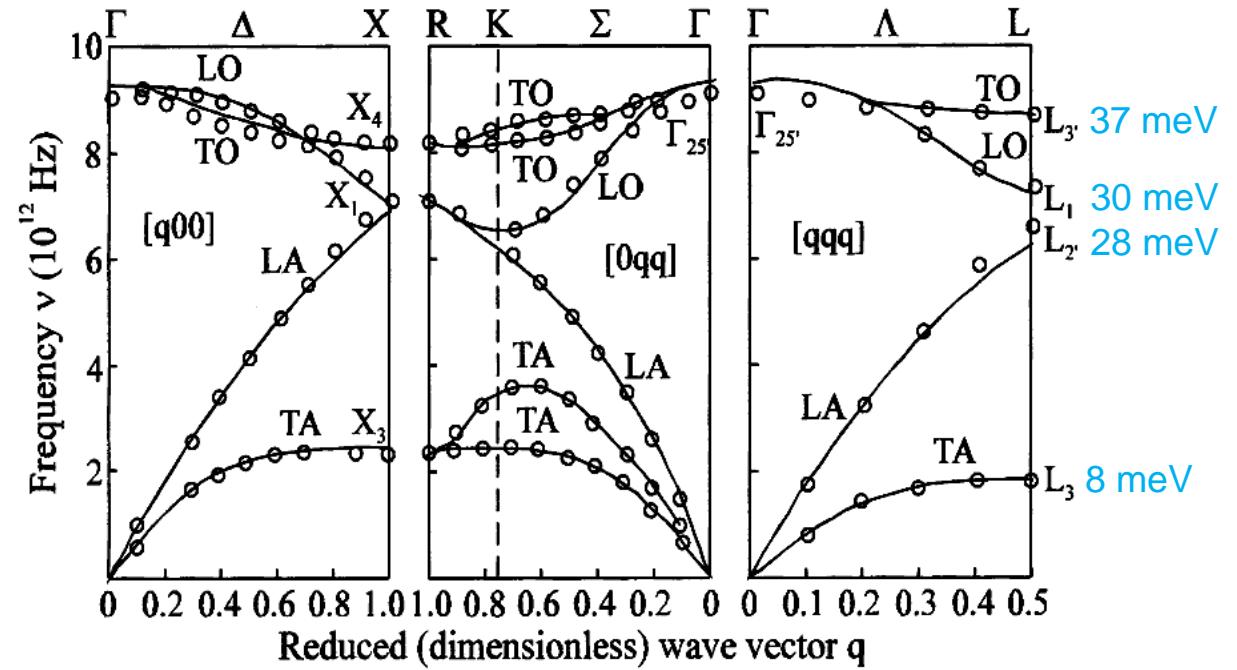
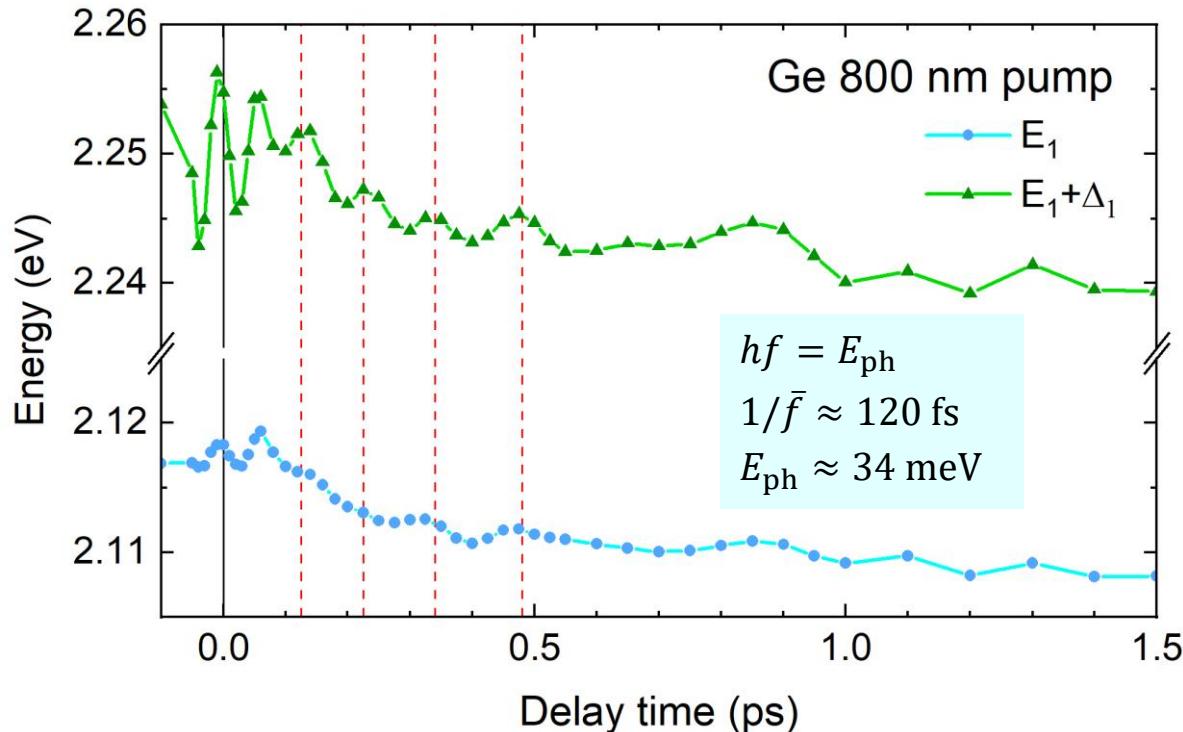
# Critical point parameters of GaSb (266, 400, and 800 nm pump)



# Problem with InP: Data only up to 3.34 eV



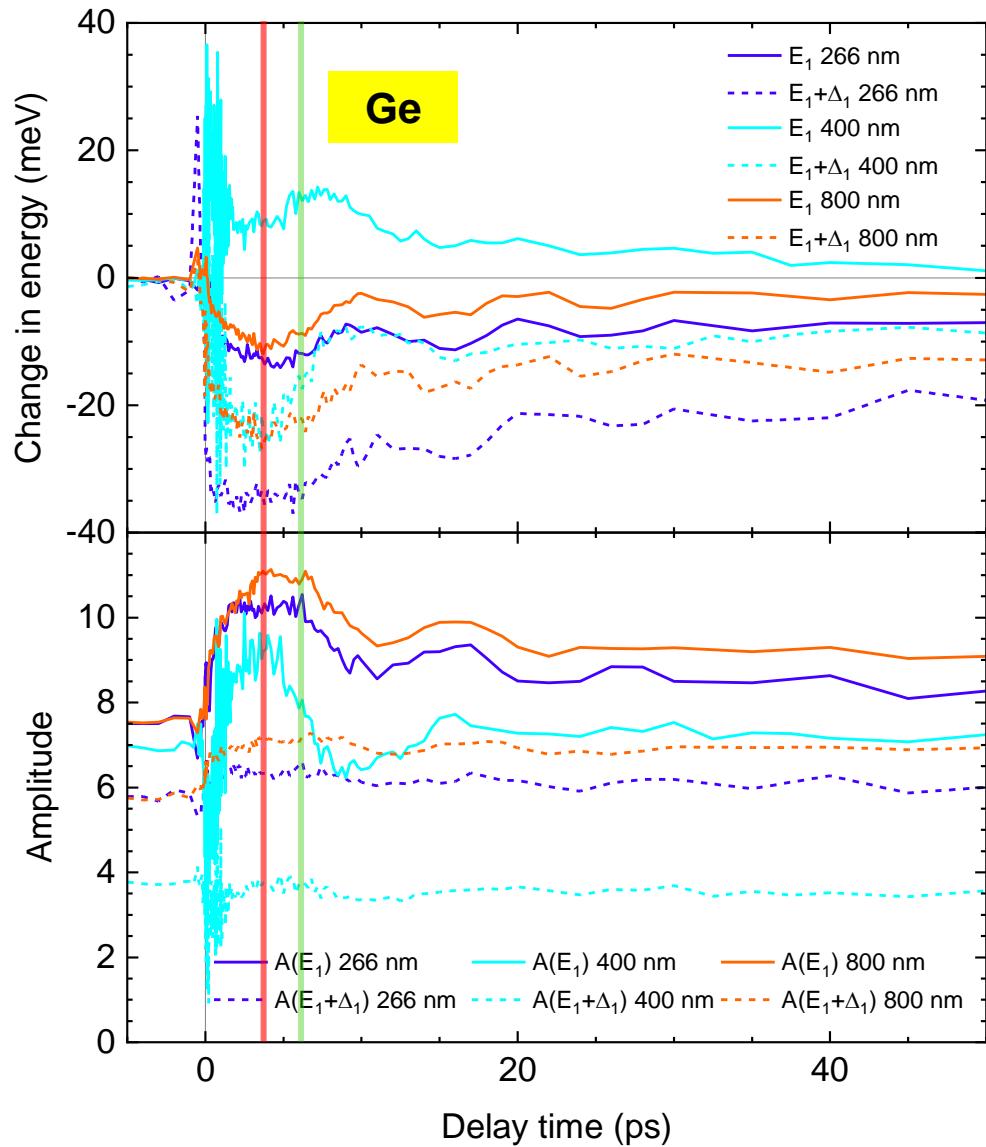
# Coherent optical phonon oscillations?



Weber W., Phys. Rev. B15, 10 (1977) 4789-4803.

- Are these oscillations due to coherent optical phonons?
- Period about 100-150 fs ( $E_{ph} \approx 28 - 40$  meV)
- The temporal bandwidth is  $\sim 120$  fs (limited by oblique incidence and probe spot size)

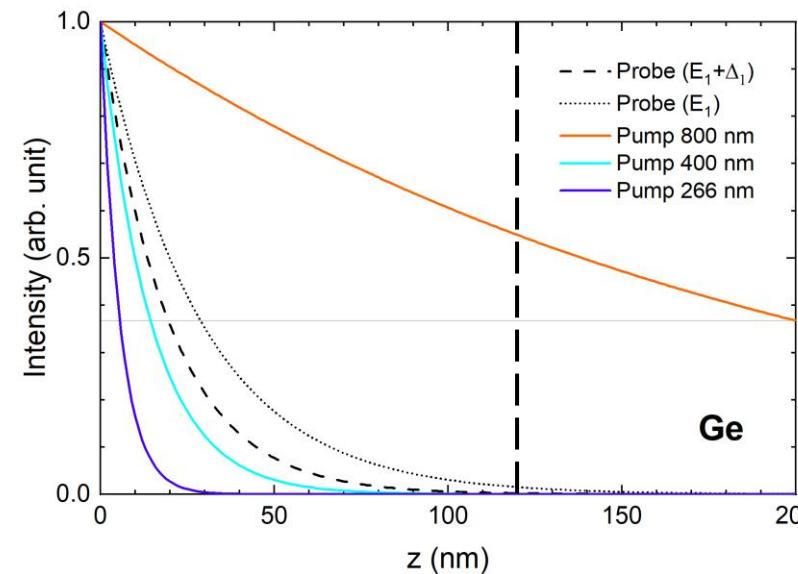
# Propagation of strain pulses in Ge



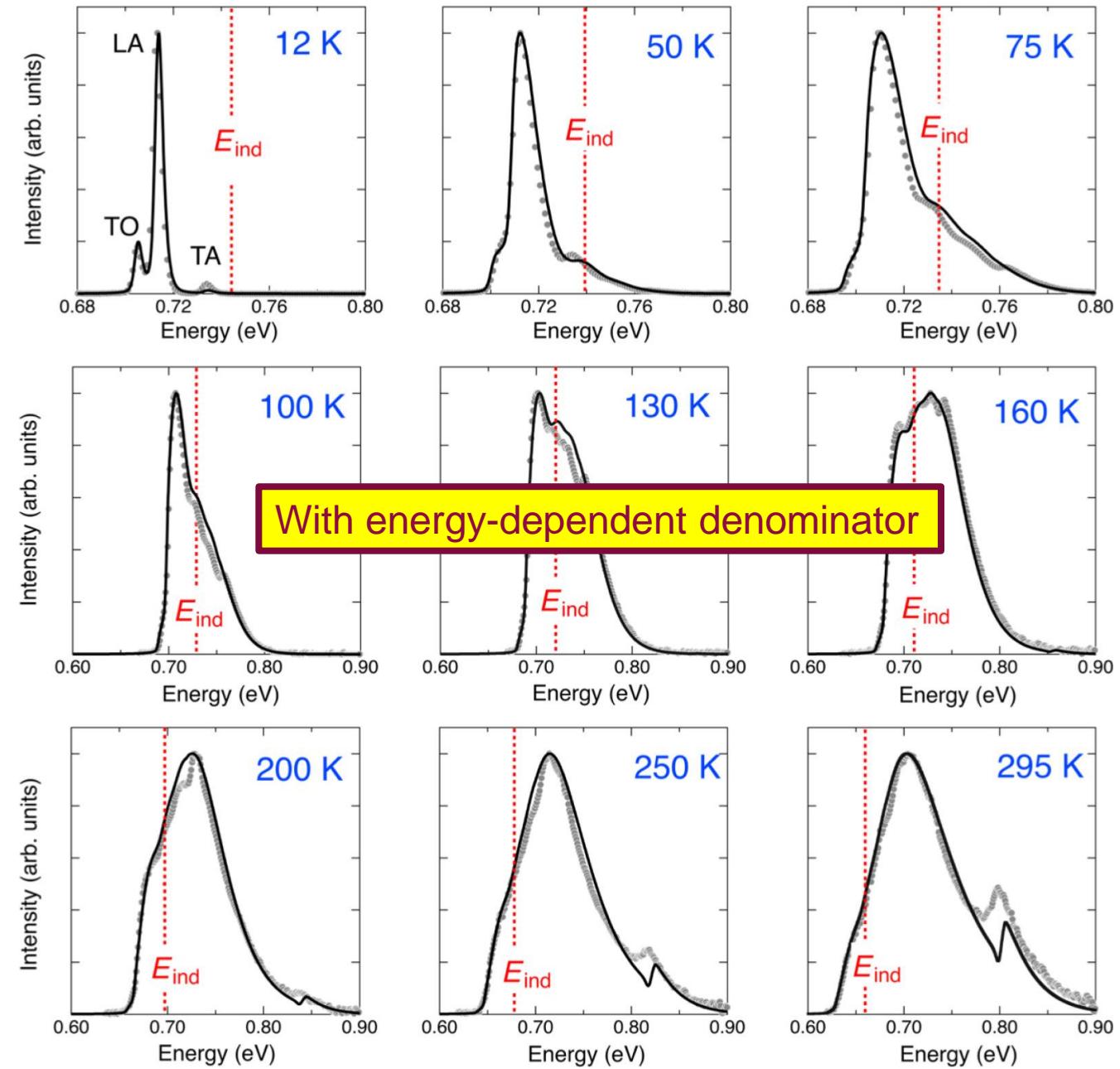
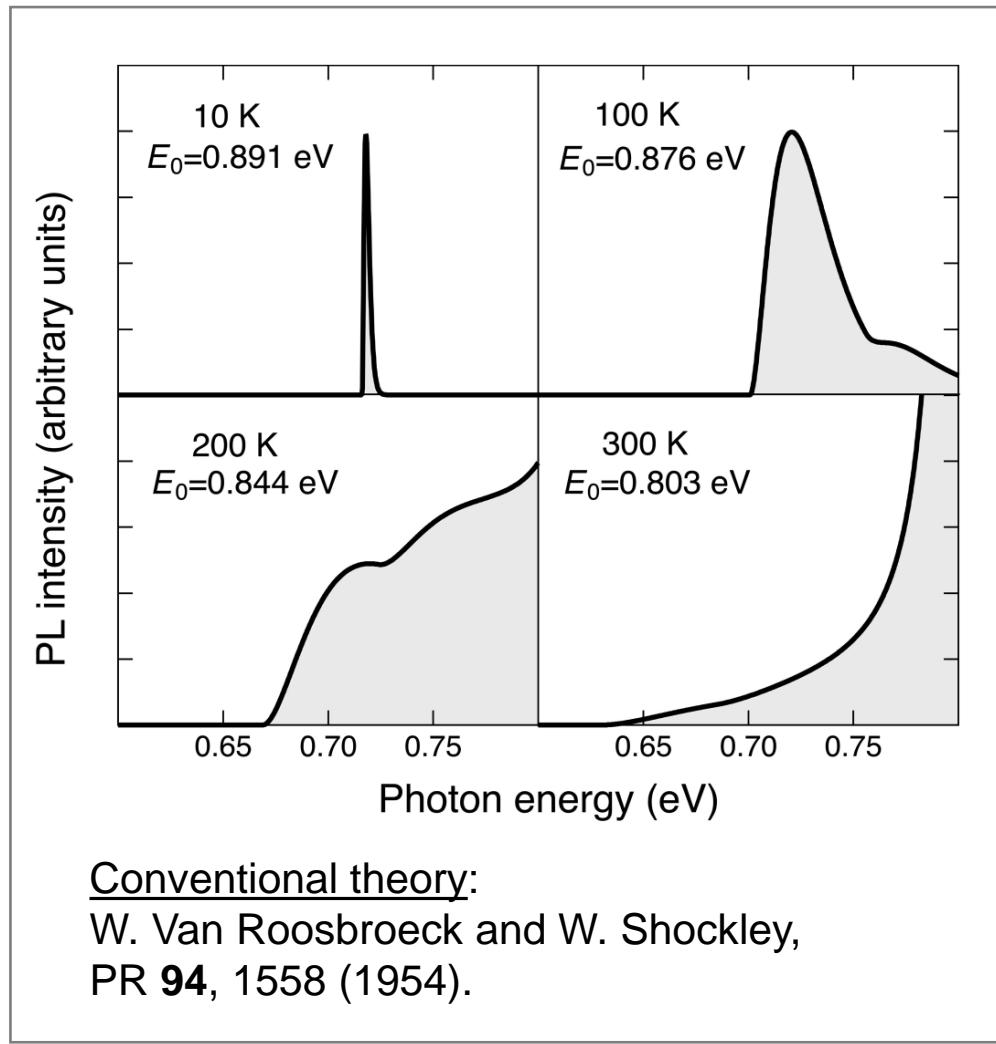
$$t = \frac{d}{v_s} = \frac{18 \text{ nm}}{4.87 \text{ nm/ps}} \approx 4 \text{ ps}$$

$$t = \frac{d}{v_s} = \frac{29 \text{ nm}}{4.87 \text{ nm/ps}} \approx 6 \text{ ps}$$

$$d = 25 \text{ ps} \cdot 4.87 \frac{\text{nm}}{\text{ps}} \approx 120 \text{ nm}$$



# Temperature-dependent photoluminescence in Ge



Menéndez et al.